

ws2022_exam

Student Group

First Name	Surname	Matrikel Nr.

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Exercise E1 Resistance of a Wire by Resistivity**(written test, approx. 6 % of a 60-minute written test, WS2022)**

A heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 is used for electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Determine the current I needed to operate the heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \text{and } R = \\ 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity**(written test, approx. 6 % of a 60-minute written test, WS2022)**

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Exercise E1 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, which has a temperature coefficient of performance of 2.5, has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

$$R = 6.5 \text{ k}\Omega$$

The power transfer resistor P is the product of the current and the voltage. Therefore, a solution is to increase the heat flow up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot \left((1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2) \right)$$

Exercise E2 Temperature-dependent Resistance**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. A refrigerator, which has a temperature coefficient of performance of 2.5, has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

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The power transfer resistor P is the product of the current and the voltage. Therefore, a solution is to increase the heat flow up the refrigeration system.

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Exercise E1 Pure Resistor Network Simplification

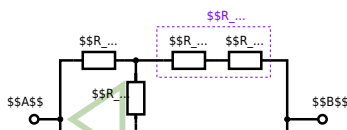
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be closed and integrated, $R_2 = R_3 = 100 \Omega$ and the switch between R_1 and R_2 shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{\text{eq}} = 133.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

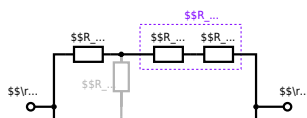
$$R_Y = \frac{R_2 \cdot R_3}{R_2 + R_3} = \frac{100 \cdot 100}{100 + 100} = 50 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_1 + (R_Y + R_4) \parallel (R_Y + R_2 + R_3) = 100 + (50 + 400) \parallel (50 + 100 + 100)$$

.. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$\begin{aligned} R_{\text{eq}} &= (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \\ R_{\text{eq}} &= (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \\ R_{\text{eq}} &= (500 \, \Omega) \parallel (200 \, \Omega) \\ R_{\text{eq}} &= \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \end{aligned}$$

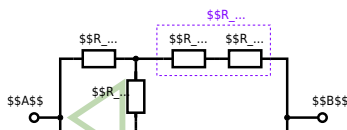
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved with \$R_1 = 200 \, \Omega\$, \$R_2 = 100 \, \Omega\$, \$R_3 = 150 \, \Omega\$ and the voltage source \$U = 10 \, \text{V}\$.

Solution

$$R_{\text{eq}} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.



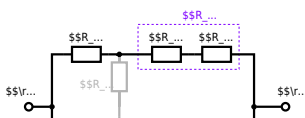
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



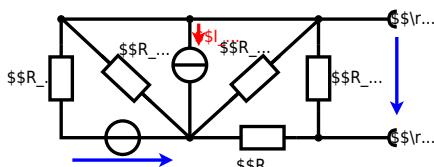
The equivalent resistor is given by a parallel configuration of resistors in series:

$$\begin{aligned} R_{\text{eq}} &= (R_2 + R_1 || R_3) || (R_4 + R_5) || R_L \\ R_{\text{eq}} &= (100 \, \Omega + 200 \, \Omega || 200 \, \Omega) || (100 \, \Omega + 100 \, \Omega) || \\ R_{\text{eq}} &= (500 \, \Omega) || (200 \, \Omega) || R_{\text{eq}} = \{ \{ 500 \, \Omega \cdot 200 \, \Omega \} \over {500 \, \Omega + 200 \, \Omega} \} || \\ \end{aligned}$$

Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

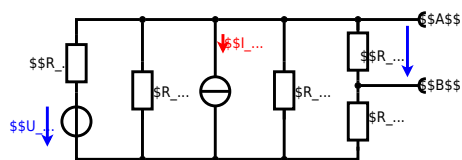
$$\begin{aligned} U_s &= U_{\text{AB}} = 4.5 \, \text{V} \\ R_i &= R_{\text{AB}} = 6 \, \Omega \end{aligned}$$



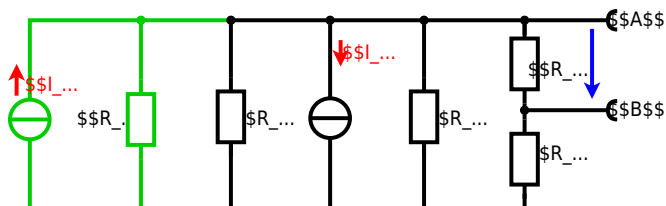
Calculate the internal resistance R_{int} and the source voltage U_{S} of an equivalent linear voltage source on the connectors A and B . $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_{24} and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_{24} - I_4 = \frac{U_{24}}{R_1} - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_2 \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} - I_4 \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} - \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

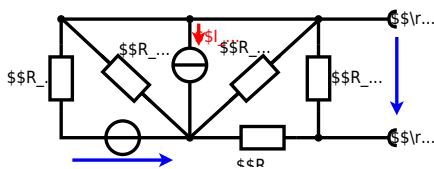
with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \\ R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

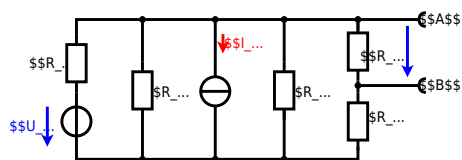
$$U_s = U_{AB} = 4.5\text{V} \quad R_i = R_{AB} = 6\Omega$$



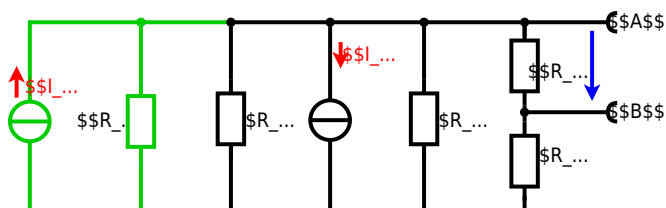
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



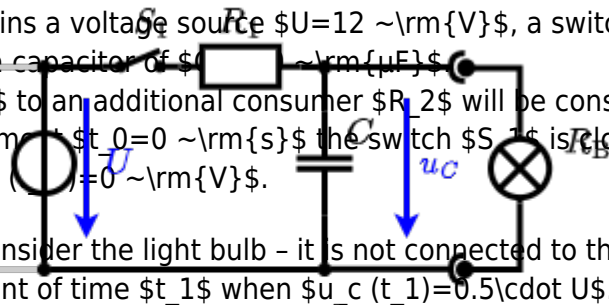
Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_{24} and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_{24} - I_4 = \frac{U_{24}}{R_1} - I_4$$
 The resulting circuit can again be transformed:



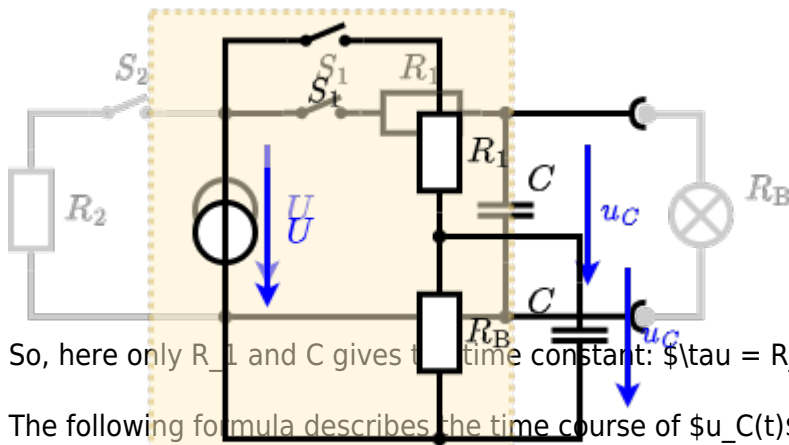
Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{135}$$

The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$

$$e^{-t/\tau} = 0.5 \quad t/\tau = \ln(0.5) \quad t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$
 An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V DC voltage source U , a switch S_1 , a resistor $R_1=20\text{ }\Omega$, a capacitor $C=100\text{ }\mu\text{F}$, and a light bulb $R_B=20\text{ }\Omega$. The voltage across the capacitor is again 0 V at the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution

To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

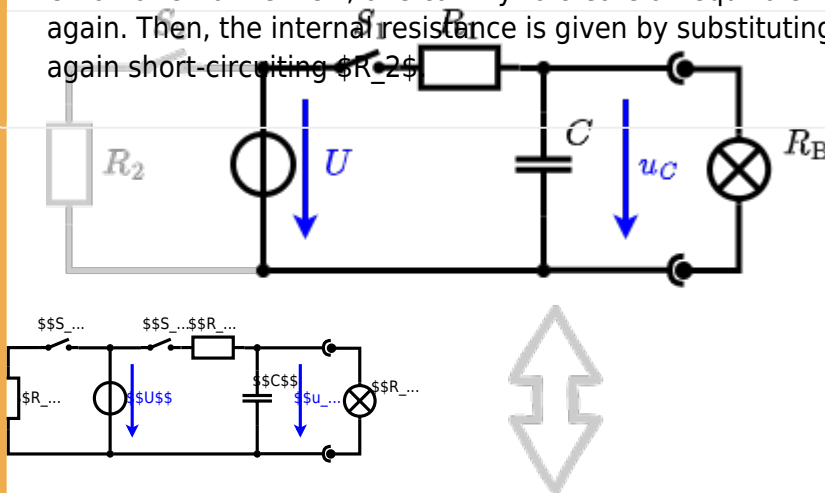
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

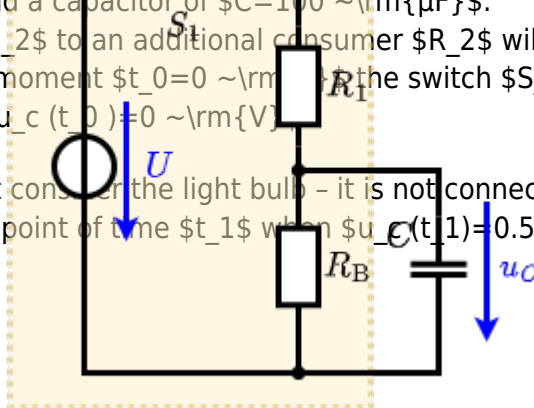


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$: $u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$. It has to be rearranged to t : $(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) \implies t = R_1 \cdot C \cdot \ln(0.5)$

Exercise E1 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (φ and $\varphi_{\underline{X}_1}$) shall be given.

After analysis, the full width of the component impedance can be extracted and the phase angle φ in phase $\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}}$ shall be given. $\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}}$ shall be given.

.. Calculate the physical values of the two components.

Solution $\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}} = 0^\circ - \arctan\left(\frac{-4.68}{0.24}\right) = 87.06^\circ$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.42 \angle 87.06^\circ$ A

The current and voltage are in phase with the voltage source $\underline{U}$ (pure real) resulting impedance $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 4.68Ω is a capacitor with the same absolute value of 4.68Ω impedance. $\underline{X}_C = -j4.68 \Omega$ and $\underline{X}_R = 0.24 \Omega$.

$\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}} = 0^\circ - \arctan\left(\frac{-4.68}{0.24}\right) = 87.06^\circ$

The phase angle φ can be calculated as $\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}} = 0^\circ - \arctan\left(\frac{-4.68}{0.24}\right) = 87.06^\circ$

With the complex part $\underline{Z} = 0.24 - j4.68 \Omega$ the physical values begin $\underline{X}_C = -j4.68 \Omega$ and $\underline{X}_R = 0.24 \Omega$.

The phase φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.06^\circ$

Exercise E6 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (φ and $\varphi_{\underline{X}_1}$) shall be given.

After analysis, the full width of the component impedance can be extracted and the phase angle φ in phase $\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}}$ shall be given. $\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}}$ shall be given.

.. Calculate the physical values of the two components.

Solution $\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}} = 0^\circ - \arctan\left(\frac{-4.68}{0.24}\right) = 87.06^\circ$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.42 \angle 87.06^\circ$ A

The current and voltage are in phase with the voltage source $\underline{U}$ (pure real) resulting impedance $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 4.68Ω is a capacitor with the same absolute value of 4.68Ω impedance. $\underline{X}_C = -j4.68 \Omega$ and $\underline{X}_R = 0.24 \Omega$.

$\varphi = \varphi_{\underline{Z}} = \varphi_{\underline{U}} - \varphi_{\underline{I}} = 0^\circ - \arctan\left(\frac{-4.68}{0.24}\right) = 87.06^\circ$

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.06^\circ$

The absolute value of the impedance is $\sqrt{(0.24 \sim \Omega)^2 + (4.68 \sim \Omega)^2} = 4.7 \sim \Omega$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 86.8^\circ$.
 With the complex part comes the physical value: $X_L = \omega L$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 86.8^\circ$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 86.8^\circ$.

Exercise E1 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.
 The equivalent impedance for R and C combined is given by $Z = \sqrt{R^2 + X_C^2}$.
 The equivalent impedance for R , L and C combined is given by $Z = \sqrt{R^2 + (X_L - X_C)^2}$.
 The equivalent impedance for R , L and C combined is given by $Z = \sqrt{R^2 + (X_L - X_C)^2}$.

Solution

$R_1 = 1.00 \sim \Omega$

$R_2 = 10.0 \sim \Omega$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.

Parallel circuit means that the voltage is the same on R_1 and C_1 .
 The equivalent impedance for R_1 and C_1 combined is given by $Z = \sqrt{R_1^2 + X_{C1}^2}$.
 The equivalent impedance for R_2 and C_2 combined is given by $Z = \sqrt{R_2^2 + X_{C2}^2}$.

The equivalent impedance for R_1 and C_1 combined is given by $Z = \sqrt{R_1^2 + X_{C1}^2}$.
 The equivalent impedance for R_2 and C_2 combined is given by $Z = \sqrt{R_2^2 + X_{C2}^2}$.

Therefore, the resulting current of the parallel circuit is given as:

$I = \frac{U}{Z}$

This can be simplified to $I = \frac{U}{\sqrt{R^2 + (X_L - X_C)^2}}$.

Back to the first formula: $R_3 \cdot I_3 = X_{L2} \cdot I_2$.

Back to the first formula: $R_3 \cdot I_3 = X_{L2} \cdot I_2$.
 The equivalent impedance for R_3 and C_3 combined is given by $Z = \sqrt{R_3^2 + X_{C3}^2}$.
 The equivalent impedance for R_3 and C_3 combined is given by $Z = \sqrt{R_3^2 + X_{C3}^2}$.

Exercise E7 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

Replaces the resistor value of $20 \pm 3\%$ with a variable AC voltage source of $35 \pm 3.0 \sim \text{V}$ with $B = 200 \sim 450 \text{ kHz}$. The high geneeescarcentes $2 = \$0 \{3R\} = 1A \sim \text{V}$ through $3A$.

A resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \sim \text{nF}$ at $f_1 = 4 \sim \text{MHz}$.

$$R_1 = 1.00 \sim \Omega$$
$$\text{begin}\{align*} R_2 \&= 10.0 \sim \Omega \end{align*}$$

Solution

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by \begin{align*}

[illegible]

\$\{ \mathbf{v}_1, \mathbf{v}_2 \}\$ can be simplified to: $\text{begin}(\text{angle}, \text{vert})$
 $\{ \mathbf{v}_1, \mathbf{v}_2 \} \perp \{ \mathbf{u}_1, \mathbf{u}_2 \}$ (It has to, since $\mathbf{R}_3$
 is perpendicular to $\{ \mathbf{v}_1, \mathbf{v}_2 \}$ and $\{ \mathbf{u}_1, \mathbf{u}_2 \}$ too)
 $\text{end}(\text{angle}, \text{vert})$

Therefore, the resulting current of the parallel circuit is given as: \begin{align*}

$$\underline{\{1\}} \{3\} \&= \underline{\{1\}} \{3R\} + \underline{\{1\}} \{3C\} \setminus$$
[illegible]
$$\right)^2 - (2\pi \cdot 450 \sim \{\rm kHz\} \cdot 4.7 \sim \{\rm \mu H\})^2 \} \\\end{align*}$$

Back to the first formula:
$$R_3 \cdot I_{3R} = X_{3C} \cdot$$

$$\{I\}_3 \subset \mathbb{R}^3 \cong \{X\}_3 \cdot \frac{\{I\}_3}{\{I\}_3} \cong$$
$$\frac{1}{2\pi \cdot f \cdot C_3} \cdot \sqrt{|I_3|^2 -$$
$$\frac{\{I\} \{3R\}^2}{\{I\} \{3R\}} \quad \text{\textbackslash\textbackslash end\{align*\}}$$

Exercise E1 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

2. Calculate the three (3) input base functions $\{Z\}$, $\{B\}$ and $\{Z\}$ and

Problem 5.7) A cylindrical capacitor of length $l = 1.0 \text{ m}$ and inner radius $a = 0.5 \text{ cm}$ is connected to a sinusoidal voltage source $u(t) = 3.0 \text{ V} \cdot \sin(2\pi \cdot 15 \text{ kHz} \cdot t)$. The capacitor is filled with a dielectric material with a permittivity $\epsilon = 2.0 \cdot \epsilon_0$. Calculate the maximum electric field strength E_{max} and the maximum magnetic field strength B_{max} inside the capacitor.

Solution
This linear source is connected with an inductor of $330 \sim \{\rm \mu H\}$ and a capacitor of $0.22 \sim \{\rm \mu F\}$, all in series.

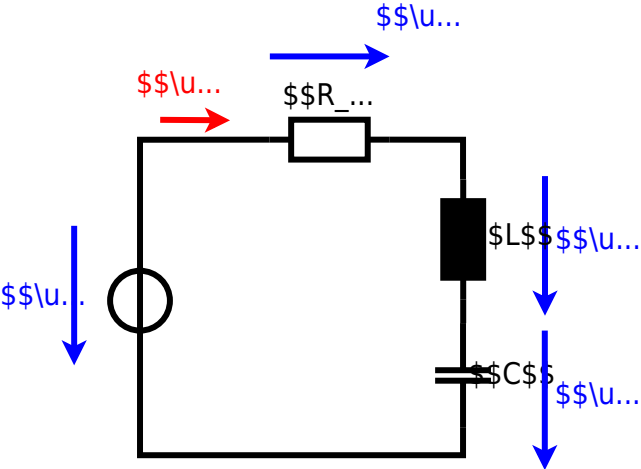
Result

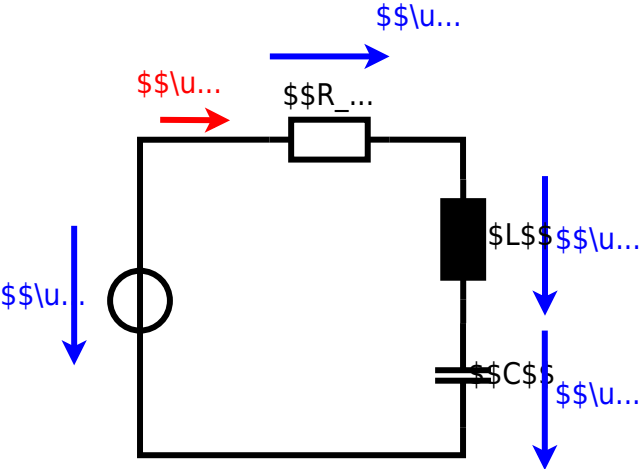
$$\begin{aligned} \begin{array}{l} \text{\tiny \rm \textit{begin{align*}}} \\ \text{\tiny \rm \textit{end{align*}}} \end{array} \quad Z = 107.31 \text{ (1 m \Omega) and } Z_{\text{CG}} = 48.2 \sim \Omega \quad Z = 19.8 \sim \Omega \end{aligned}$$

label all components, voltages, and currents.

$$\begin{aligned} Z &= \{ \{ \hat{U} \} \over \{ \hat{I} \} \} \} \parallel \hat{I} \quad \&= \{ \{ \hat{U} \} \over \{ Z \} \} \parallel \end{aligned}$$
$$\{Z \mid C \models \{1\} \text{ over } 2\pi \cdot f \cdot C\} \models \{1\} \text{ over } 2\pi \cdot 15$$
$$\text{result} \{\rm kHz\} \cdot 0.22 \sim \{\rm \mu F\}$$
$$\text{With } \left\| \frac{\partial}{\partial t} \right\|_{L^2(\Omega)} = \sqrt{\int_{\Omega} \left(\frac{\partial u}{\partial t} \right)^2 dx} \quad \text{and} \quad \left\| \frac{\partial u}{\partial t} \right\|_{L^2(\Omega)} = \sqrt{\int_{\Omega} \left(\frac{\partial u}{\partial t} \right)^2 dx}$$
$$\{\{1\}\over{\sqrt{2}}\}\cdot\{\{\hat{U}\}\over{Z}\} \parallel \&= \{\{1\}\over{\sqrt{2}}\}\cdot$$
[illegible]
$$\sim \{\mathrm{rm\ kHz}\} \cdot 330 \sim \{\mathrm{rm\ \mu H}\} \} \} \end{align*}$$
$$\underline{Z} \&= R + \underline{Z} \quad L + \underline{Z} \quad C \quad \&= R + i$$
$$\begin{aligned} & \begin{pmatrix} \text{begin}\{align\} \end{pmatrix} \quad \underline{\{Z\}} \&= R + \underline{\{Z\}_E} + \underline{\{Z\}_C} \quad \&= R \\ & \quad \cdot \{Z\}_E - i \cdot \{Z\}_C \quad \&= B + i \cdot (\{Z\}_E - \{Z\}_C) \quad \underline{\{Z\}} \&= \end{aligned}$$
$$\sqrt{R^2 + (\underline{Z}^L - \underline{Z}^C)^2}$$







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