

# task\_nyniewamxfshpuwt\_with\_calculation

## Student Group

| First Name | Surname | Matrikel Nr. |
|------------|---------|--------------|
|            |         |              |
|            |         |              |
|            |         |              |

## Table of Contents

Exercise E19 Resonant Circuit (written test, approx. 4 % of a 120-minute written test,  
SS2021) .....

2

## resonance, resonant circuit, RMS, exam ee2 SS2021

**Exercise E19 Resonant Circuit****(written test, approx. 4 % of a 120-minute written test, SS2021)**

5) Given a resonant RLC circuit that is fed by a sine wave of the voltage  $U_{\text{rms}} = 12 \text{ V}$  (see the diagram on the right). The internal resistance  $R_i$  and the capacitance  $C$  are fixed. The resistance  $R$  can be varied.

$$U_{\text{rms}} = 12 \text{ V} \cdot \sin(2\pi \cdot f_0 \cdot t)$$

$$R_i = 200 \text{ m}\Omega$$

$$C = 205.5 \text{ nF}$$

$$C = 30 \text{ }\mu\text{F}$$

For the following calculation, the internal resistance  $R_i$  and the resistance  $R$  have to be combined: 
$$R_{\Sigma} = R_i + R$$

Here, either one knows that the gain factor  $Q$  stands for  $Q = \frac{U_C}{U_{\text{rms}}}$  and therefore can directly use the following formula: 
$$Q = \frac{U_C}{U_{\text{rms}}} = \frac{1}{R_{\Sigma}} \sqrt{\frac{L}{C}}$$
 
$$R_{\Sigma} = \frac{U_{\text{rms}}}{U_C} \sqrt{\frac{L}{C}}$$

When the gain factor is not known, one has to derive it:

The voltage  $I$  at resonance is only given by the total ohmic resistance  $R_{\Sigma}$  and the source voltage  $U_{\text{rms}}$ : 
$$I = \frac{U_{\text{rms}}}{R_{\Sigma}}$$

This current flow also through the impedance of the capacitor 
$$U_C = Z_C \cdot I = \frac{1}{\omega C} \cdot I = \frac{U_{\text{rms}}}{\omega C R_{\Sigma}}$$

At resonance, the angular frequency  $\omega$  is given by  $\omega = \frac{1}{\sqrt{LC}}$

$$U_C = \frac{U_{\text{rms}}}{\frac{1}{\sqrt{LC}} R_{\Sigma}} = \frac{U_{\text{rms}} \sqrt{LC}}{R_{\Sigma}}$$

$$R_{\Sigma} = \frac{U_{\text{rms}} \sqrt{LC}}{U_C}$$

What is the resonance frequency  $f_0$ ?

Path

In both cases, we end up with the same formula, where we have to insert the physical values: 
$$R_{\Sigma} = \frac{U_{\text{rms}}}{U_C} \sqrt{\frac{L}{C}}$$
 
$$R_{\Sigma} = \frac{1}{4} \sqrt{\frac{20 \cdot 10^{-3} \text{ H}}{30 \cdot 10^{-6} \text{ F}}}$$

The resonant frequency  $f_0$  is given as 
$$f_0 = \frac{1}{2\pi \sqrt{LC}}$$

And so, the resistance  $R$  is: 
$$R = R_{\Sigma} - R_i$$

$$R = \frac{1}{4} \sqrt{\frac{20 \cdot 10^{-3} \text{ H}}{30 \cdot 10^{-6} \text{ F}}} - 200 \text{ m}\Omega = 205.4681 \text{ }\Omega$$

From:

<https://wiki.mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:

[https://wiki.mexle.te.hs-heilbronn.de/ee2/task\\_nyniewamxfshpuwt\\_with\\_calculation](https://wiki.mexle.te.hs-heilbronn.de/ee2/task_nyniewamxfshpuwt_with_calculation)

Last update: **2024/07/04 03:52**

