

Exam Winter Semester 2022

Student Group

First Name	Surname	Matrikel Nr.

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

Tasks

Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wire even to a temperature of 1800°C . Electric power dissipation (= heat flow) of $P=40\text{ W}$ is necessary.

Calculate the current I needed to operate for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6}\text{ }\Omega\text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40\text{ W}}{0.33\text{ }\Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad | \text{ with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad \& \quad R = 1.10 \cdot 10^{-6}\text{ }\Omega\text{ m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wire even to a temperature of 1800°C . Electric

Result power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Calculate the current I linked to the power P for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

2. Calculate the resistance R (W) needed for the element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad | \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad | \quad R = \\ 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator is equipped with a thermistor to monitor the temperature inside the refrigerator. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha=0.01 \text{ } \frac{1}{\text{K}}$ and $\beta=71 \cdot 10^{-6} \text{ } \frac{1}{\text{K}^2}$.

Result The temperature inside the refrigeration system can reach down to -40°C .

1. Calculate the resistance of the thermistor at -40°C .

$$R = 6.5 \text{ k}\Omega$$

Solution The resistance of the thermistor decreases as the temperature decreases. Therefore, a thermistor can be used to monitor the temperature inside the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$\begin{aligned} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} \quad | \quad R = 10 \text{ k}\Omega \cdot \\ \left(1 + 0.01 \cdot (-40^\circ \text{C} - 25^\circ \text{C}) + 71 \cdot 10^{-6} \cdot (-40^\circ \text{C} - 25^\circ \text{C})^2\right) \end{aligned}$$

Exercise E2 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, which has a temperature coefficient of performance of 2.5, has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ } ^\circ\text{C}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ } ^\circ\text{C}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: Calculate the resistance of the thermalistor at -40°C .

$$R = 6.5 \text{ k}\Omega$$

The power transferred to the load is $P = \frac{U^2}{R}$. Therefore, a solution is to increase the heat flow up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot \left((1 + 0.01 \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2) \right)$$

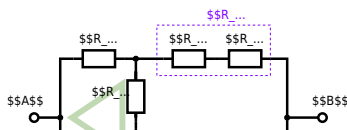
Exercise E1 Pure Resistor Network Simplification**(written test, approx. 13 % of a 60-minute written test, WS2022)**

The following shall hold: $R_1 = 200 \text{ }\Omega$, $R_2 = 100 \text{ }\Omega$, $R_3 = 100 \text{ }\Omega$, and $U = 10 \text{ V}$. Result: $R_{\text{eq}} = 132.8 \text{ }\Omega$.

Solution

$$R_{\text{eq}} = 132.8 \text{ }\Omega$$

Now a wye-delta transformation is necessary.



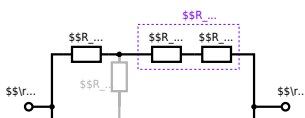
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega) \parallel (500 \, \Omega \cdot 200 \, \Omega) / (500 \, \Omega + 200 \, \Omega)$$

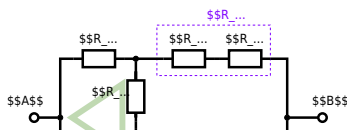
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved with \$R_1=200 \, \Omega\$, \$R_2=R_3=150 \, \Omega\$, \$R_4=R_5=100 \, \Omega\$ and the voltage \$U_{SV}=10 \, \text{V}\$.

Solution

$$R_{eq} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.

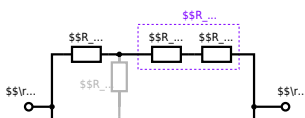


Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:
$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega) \parallel$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



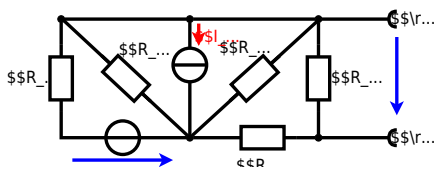
The equivalent resistor is given by a parallel configuration of resistors in series:

$$\begin{aligned} R_{\text{eq}} &= (R_2 + R_1 + R_3) \parallel (R_2 + R_3) \parallel R_4 \parallel R_5 \\ R_{\text{eq}} &= (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel 100 \, \Omega \parallel 500 \, \Omega \\ R_{\text{eq}} &= (500 \, \Omega) \parallel (200 \, \Omega) \parallel 100 \, \Omega \parallel 500 \, \Omega \\ R_{\text{eq}} &= \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \parallel 100 \, \Omega \parallel 500 \, \Omega \end{aligned}$$

Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

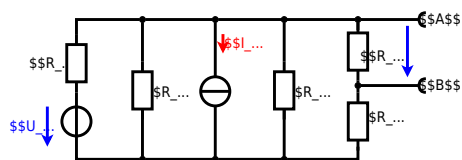
$$\begin{aligned} U_s &= U_{AB} = 4.5 \, \text{V} \\ R_i &= R_{AB} = 6 \, \Omega \end{aligned}$$



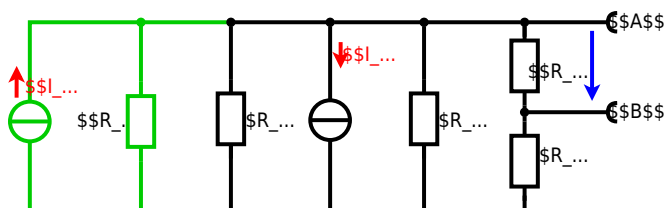
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_{23} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

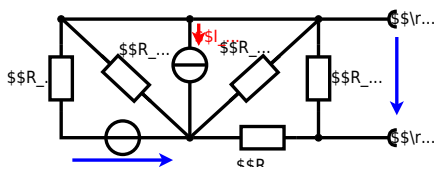
with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \quad R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

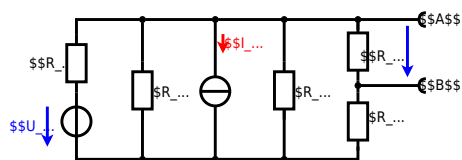
$$U_s = U_{AB} = 4.5\text{V} \quad R_i = R_{AB} = 6\Omega$$



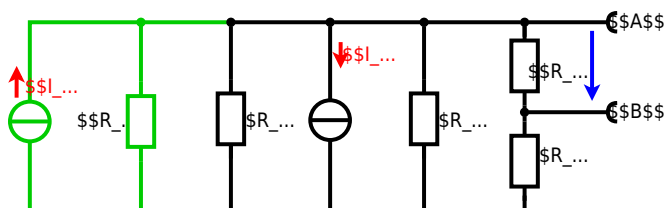
Calculate the internal resistance R_s and the source voltage U_s of an equivalent linear voltage source on the connectors A and B.
$$\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$$
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{AB} = U_{24} \cdot \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \left(\frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} \right) \cdot \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \left(\frac{6.0\text{V}}{5.0\Omega} - 4.2\text{A} \right) \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \parallel R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E1 Charging Capacitors

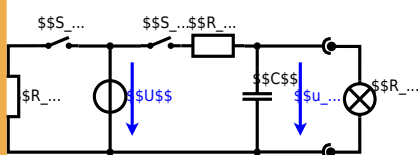
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit below is a simplified model of a power supply unit. It consists of a voltage source U , a switch S_1 , a resistor R_1 , a capacitor C , and a load resistor R_2 . The voltage across the capacitor is again 0V at the moment $t_0=0\text{s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ms}$ after closing the switch.

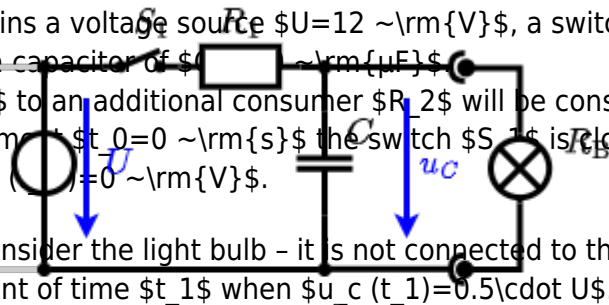
Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 . Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

Solution: The equivalent circuit is shown below. The ideal voltage source U is in series with the resistor R_1 . The load resistor R_2 is in parallel with the capacitor C . The voltage across the capacitor is $u_c(t_2)$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

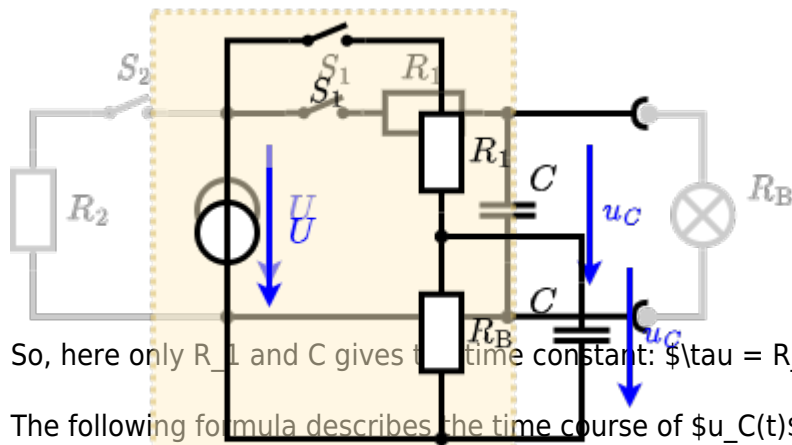


The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$

$$e^{-t/\tau} = 0.5 \quad t/\tau = \ln(0.5) \quad t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$
 An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V DC voltage source, a switch S_1 and a switch S_2 connected to a $20\text{ }\Omega$ resistor, a $100\text{ }\mu\text{F}$ capacitor and a light bulb R_B . The voltage across the capacitor is again 0 V at the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

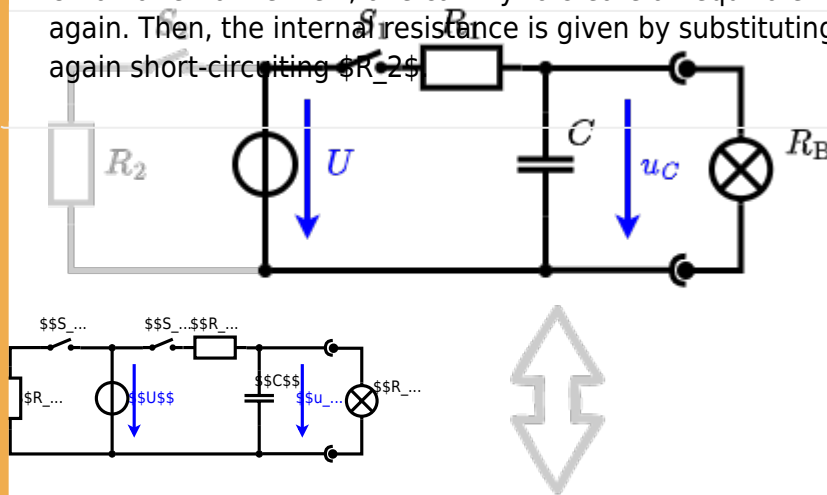
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

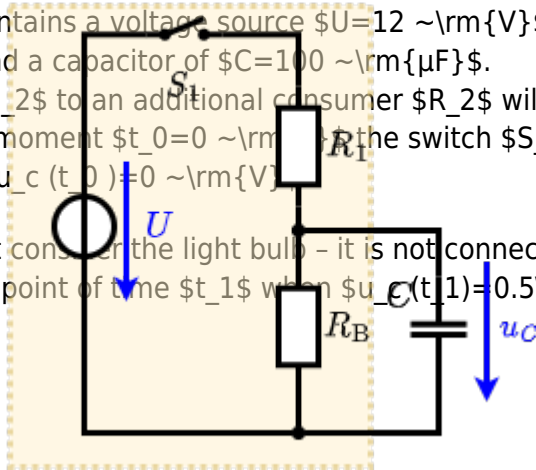


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) \implies t = R_1 \cdot C \cdot \ln(0.5)$$

Exercise E1 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. ($\$R\$$ and $\underline{X}_L$) shall be given.

After analysis, the full bridge dimensioned impedance can be extracted and the phase angle φ in phase (calculated) is $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$.

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.4 \angle 10.9^\circ$ A

The current and voltage are in phase since the impedance is purely real (no imaginary part). The resulting impedance is $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 0.24Ω is a resistor with the same absolute value of 0.24Ω and the component $-j4.68 \Omega$ is an inductor with the same absolute value of 4.68Ω .

Impedance $\underline{Z} = R + jX_L = 0.24 - j4.68 \Omega$

Phase angle $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$

The absolute value of the impedance is $|\underline{Z}| = \sqrt{0.24^2 + 4.68^2} = 4.69 \Omega$

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$

With the complex part (complex value) $\underline{Z} = 0.24 - j4.68 \Omega$

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.4 \angle 10.9^\circ$ A

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$

Exercise E6 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. ($\$R\$$ and $\underline{X}_L$) shall be given.

After analysis, the full bridge dimensioned impedance can be extracted and the phase angle φ in phase (calculated) is $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$.

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.4 \angle 10.9^\circ$ A

The current and voltage are in phase since the impedance is purely real (no imaginary part). The resulting impedance is $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 0.24Ω is a resistor with the same absolute value of 0.24Ω and the component $-j4.68 \Omega$ is an inductor with the same absolute value of 4.68Ω .

Impedance $\underline{Z} = R + jX_L = 0.24 - j4.68 \Omega$

Phase angle $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$

The absolute value of the impedance is $|\underline{Z}| = \sqrt{0.24^2 + 4.68^2} = 4.69 \Omega$

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$

The absolute value of the impedance is $Z = \sqrt{(0.24 \sim \Omega)^2 + (4.68 \sim \Omega)^2} = 4.7 \sim \Omega$
 The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$
 With the complex part comes the physical value: $X_L = \omega L = 2\pi f L = 2\pi \cdot 4.7 \sim \Omega \cdot 10^{-6} \text{ s} = 29.4 \sim \mu\text{s}$
 The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$
 The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$

Exercise E1 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$
 Parallel circuit means that the voltage is the same on R_3 and C_2
 The equivalent impedance for R_3 and C_2 combined is given by $Z = \frac{R_3 \cdot X_C}{R_3 + X_C}$
 Back to the first formula: $R_3 \cdot X_C = Z^2 \cdot \omega C_3$
 Result: $R_3 = \frac{Z^2 \cdot \omega C_3}{X_C} = \frac{Z^2 \cdot 2\pi f C_3}{\frac{1}{\omega C_3}} = Z^2 \cdot \omega^2 C_3^2 = 10.0 \sim \Omega$
 Back to the first formula: $R_3 \cdot X_C = Z^2 \cdot \omega C_3$
 Result: $R_3 = \frac{Z^2 \cdot \omega C_3}{X_C} = \frac{Z^2 \cdot 2\pi f C_3}{\frac{1}{\omega C_3}} = Z^2 \cdot \omega^2 C_3^2 = 10.0 \sim \Omega$

Solution

$R_1 = 1.00 \sim \Omega$

$R_2 = 10.0 \sim \Omega$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$

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Therefore, the resulting current of the parallel circuit is given as: $I = \frac{U}{Z}$

$I = \frac{U}{Z} = \frac{10 \text{ V}}{10.0 \sim \Omega} = 1.0 \text{ A}$

Back to the first formula: $R_3 \cdot X_C = Z^2 \cdot \omega C_3$
 Result: $R_3 = \frac{Z^2 \cdot \omega C_3}{X_C} = \frac{Z^2 \cdot 2\pi f C_3}{\frac{1}{\omega C_3}} = Z^2 \cdot \omega^2 C_3^2 = 10.0 \sim \Omega$

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Back to the first formula: $R_3 \cdot X_C = Z^2 \cdot \omega C_3$
 Result: $R_3 = \frac{Z^2 \cdot \omega C_3}{X_C} = \frac{Z^2 \cdot 2\pi f C_3}{\frac{1}{\omega C_3}} = Z^2 \cdot \omega^2 C_3^2 = 10.0 \sim \Omega$

Exercise E7 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

Exercise E1 Complex Impedance Circuit
(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the following diagram (of 3S) 21.B.0
 $\sim \sqrt{R} \cdot \sin(2\pi \cdot 15 \cdot t)$ V. The high-pass filter consists of a resistor $R_1 = 10 \Omega$ and a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.
 The resistor R_1 shall have the same absolute value of the impedance as a capacitor

$C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution: $R_1 = 1.00 \text{ } \Omega$

Solution: $R_2 = 10.0 \text{ } \Omega$

Solution

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = R + j\omega L$

Parallel circuit means that the voltage is the same on R_1 and R_2 $V = I_1 R_1 = I_2 R_2$
 $I_1 = \frac{V}{R_1}$ and $I_2 = \frac{V}{R_2}$ Since V is the same, $I_1 R_1 = I_2 R_2$ $I_1 = \frac{I_2 R_2}{R_1}$
 $I = I_1 + I_2 = \frac{I_2 R_2}{R_1} + I_2 = I_2 \left(\frac{R_2}{R_1} + 1 \right)$ $I_2 = \frac{I}{\left(\frac{R_2}{R_1} + 1 \right)}$

$V = I_1 R_1 = I_2 R_2$ (It has to, since R_1 and R_2 are in parallel)
 $I_1 = \frac{V}{R_1}$ and $I_2 = \frac{V}{R_2}$ $I = I_1 + I_2 = \frac{V}{R_1} + \frac{V}{R_2} = V \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$
 $V = I \cdot Z$ $Z = \frac{V}{I} = \frac{1}{\left(\frac{1}{R_1} + \frac{1}{R_2} \right)}$

Therefore, the resulting current of the parallel circuit is given as:

$I = \frac{V}{Z} = \frac{V}{\frac{1}{\left(\frac{1}{R_1} + \frac{1}{R_2} \right)}} = V \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$

This can be simplified to $Z = \frac{R_1 R_2}{R_1 + R_2}$ $Z = \frac{10 \cdot 10}{10 + 10} = 5 \Omega$

Back to the first formula: $Z = R + j\omega L$ $5 = R + j \cdot 2\pi \cdot 4 \cdot 10^6 \cdot L$

$5 = R + j \cdot 25.13 \cdot L$ $R = 5 - j \cdot 25.13 \cdot L$

$R = 5 - j \cdot 25.13 \cdot L$ $R = 5 - j \cdot 25.13 \cdot L$

$R = 5 - j \cdot 25.13 \cdot L$ $R = 5 - j \cdot 25.13 \cdot L$

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Exercise E1 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the following diagram (of 3S) 21.B.0
 The linear source is connected with an inductor of $L = 330 \text{ } \mu\text{H}$ and a capacitor of $C = 0.22 \text{ } \mu\text{F}$, all in series.
 Result: $Z = 19.8 \text{ } \Omega$

Solution: $Z = 19.8 \text{ } \Omega$

Result

$Z = 19.8 \text{ } \Omega$

Draw the circuit diagram of the given circuit.

$Z = \frac{V}{I} = \frac{3.0}{0.15} = 20 \text{ } \Omega$

$Z = \frac{V}{I} = \frac{3.0}{0.15} = 20 \text{ } \Omega$

Result: $Z = 19.8 \text{ } \Omega$

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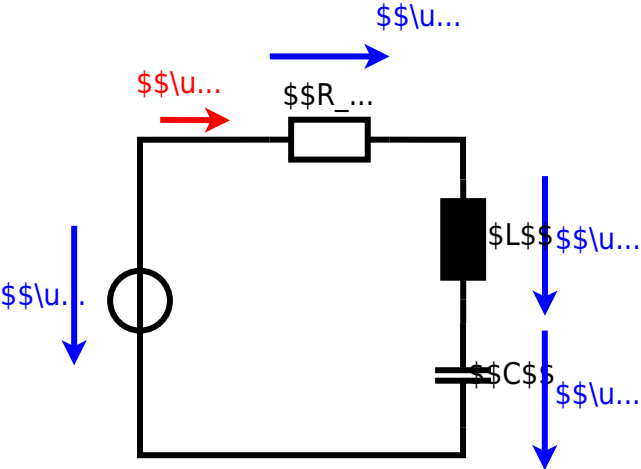
$Z = 19.8 \text{ } \Omega$

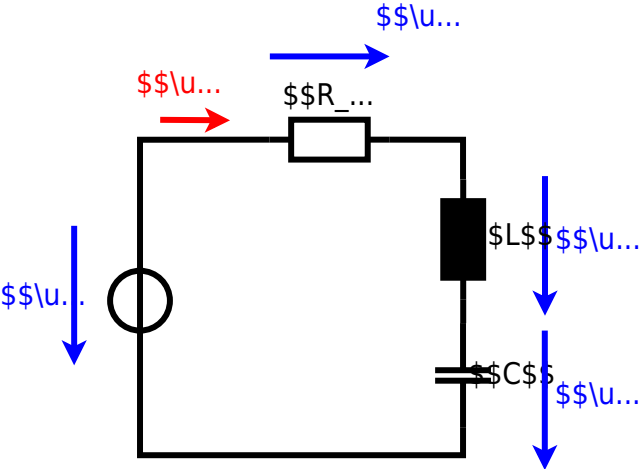
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