

Exam Winter Semester 2022

Student Group

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

Only EEE1-relevant Part

This part is only for about 25 minutes !

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat water in a room pressure of 1 bar. An electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary. Calculate the current I needed to operate it.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \quad \& \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \& \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. A thermistor is a temperature-sensitive resistor. The resistance of a thermistor has a temperature dependence given by the Steinhart-Hart equation:

Its temperature coefficients are: $\alpha = 0.01 \cdot 10^{-6} \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result
The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

The power transfer resistor P is given by $P = \frac{U^2}{R}$ and $U = 20 \text{ V}$. Therefore, a solution is to use a resistor that floats up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$\begin{aligned} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} \quad | \quad R = 10 \text{ k}\Omega \quad | \\ &\left(1 + 0.01 \cdot 10^{-6} \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2\right) \quad | \\ &\end{aligned}$$

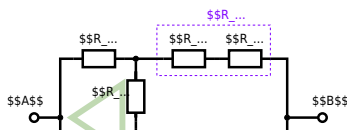
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be calculated: $R_{\text{eq}} = R_1 + R_2 + R_3 + R_4$ and the voltage U_{B} across R_4 .

Solution

$$R_{\text{eq}} = 132.8 \text{ k}\Omega$$

Now a wye-delta transformation is necessary.



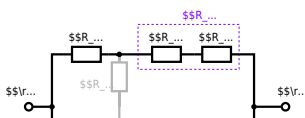
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



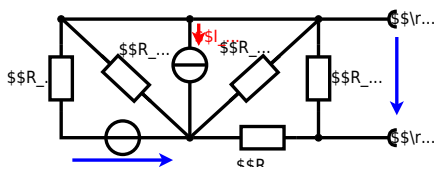
The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega}$$

Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

$$U_{\text{s}} = U_{\text{AB}} = 4.5 \, \text{V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \, \Omega$$



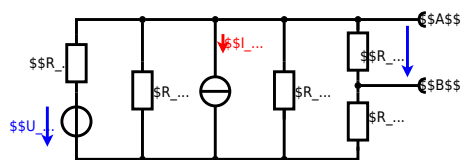
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B.

$R_1 = 5.0 \, \Omega$, $U_2 = 6.0 \, \text{V}$, $R_3 = 10 \, \Omega$, $I_4 = 4.2 \, \text{A}$, $R_5 = 10 \, \Omega$, $R_6 = 7.5 \, \Omega$, $R_7 = 15 \, \Omega$

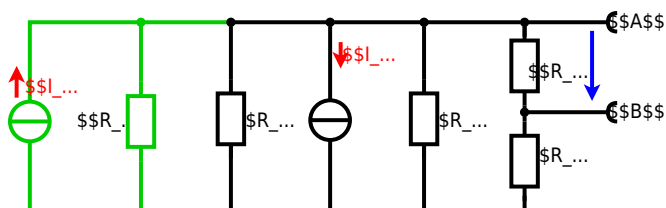
Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{AB} = U_{24} \cdot \left(\frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - I_4 \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \left(\frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) - \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($= 0 \Omega$, so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with $R_1 || R_3 || R_5 = 5 \Omega || 10 \Omega || 10 \Omega = 5 \Omega || 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \left(\frac{6.0 \text{ V}}{5.0 \Omega} \right) - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega}$$

$$R_{AB} = 15 \Omega || (7.5 \Omega + 2.5 \Omega)$$

Full Exam

These is the full exam

Full exam

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

2. The heating element made of Nichrome wire with a cross-section of 1.80 mm^2 and a length of 3 m is used for heating. A power dissipation (= heat flow) of $P = 40 \text{ W}$ is necessary. Calculate the current I needed to operate for heating elements. The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \Omega \text{ m}$. The heating element is 3 m long and has a diameter of 3.57 mm .
Solution: $R = \frac{\rho \cdot l}{A}$

Solution

$$P = U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40 \text{ W}}{0.33 \Omega}}$$

$$R = \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \quad || \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad || \quad R = 1.10 \cdot 10^{-6} \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \text{ mm})^2 \cdot \pi}$$

$$3 \sim \mathrm{m}} \} \} (3.57 \cdot 10^{-3} \sim \mathrm{m})^2 \cdot \pi \} \&\& \\\end{align*}$$

[electrical_engineering_and_electronics:task_rj0r6j4apumukrj6_with_calculation](#)
[resistivity, power, exam ee1 ws2022](#)

Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

A. The diagram explains a thermistor's resistance temperature characteristic. The thermistor's resistance is 100 Ω at 25 $^{\circ}\mathrm{C}$. Its temperature coefficients are: $\alpha = 0.01 \sim \{1\} \over \{\mathrm{K}\}$ and $\beta = 71 \cdot 10^{-6} \sim \{1\} \over \{\mathrm{K}^2\}$.

Result
The temperature inside the refrigeration system can reach down to $-40 \sim ^{\circ}\mathrm{C}$.

Result
Calculate the resistance of the thermistor at $-40 \sim ^{\circ}\mathrm{C}$.

The power of the resistor P_{resistor} is the product of the current I and the voltage U .
Solution
The current I is constant. Therefore, the power P decreases with increasing resistance R .

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$\begin{aligned} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \text{with } \Delta T = T_{\mathrm{end}} - T_{\mathrm{start}} \\ R &= 100 \sim \Omega \cdot \left(1 + 0.01 \sim \{1\} \over \{\mathrm{K}\} \cdot (-40 \sim ^{\circ}\mathrm{C} - 25 \sim ^{\circ}\mathrm{C}) + 71 \cdot 10^{-6} \sim \{1\} \over \{\mathrm{K}^2\} \cdot (-40 \sim ^{\circ}\mathrm{C} - 25 \sim ^{\circ}\mathrm{C})^2 \right) \end{aligned}$$

[electrical_engineering_and_electronics:task_70jg4yzznocarsq_with_calculation](#)
[temperature dependent resistance, power, heat, exam ee1 ws2022](#)

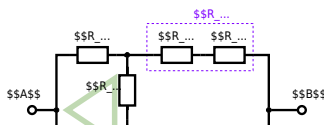
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved: Calculate the equivalent resistance R_{eq} and the source current I_{A} and I_{B} .

Solution

$$\begin{aligned} R_{\mathrm{eq}} &= 132.8 \sim \Omega \end{aligned}$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

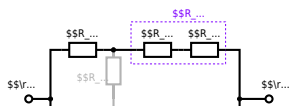
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B.

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$\begin{aligned} R_{\text{eq}} &= (R_2 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = \\ &= (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel R_{\text{eq}} = \\ &= (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \left\{ \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \right\} \parallel R_{\text{eq}} \end{aligned}$$

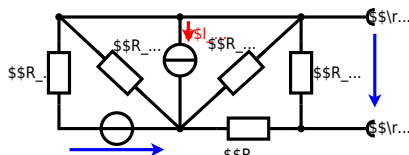
[electrical_engineering_and_electronics:task_x357drkaqv84jnsj_with_calculation](#)
network simplification, exam ee1 ws2022

Exercise E4 Equivalent linear Source

(written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

$$\begin{aligned} U_{\text{s}} &= U_{\text{AB}} = 4.5 \, \text{V} \\ R_{\text{AB}} &= 6 \, \Omega \end{aligned}$$



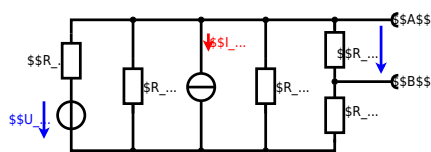
Calculate the internal resistance R_{int} and the source voltage U_{src} of an equivalent linear voltage source on the connectors A and B.

$R_1 = 5.0 \, \Omega$, $U_2 = 6.0 \, \text{V}$, $R_3 = 10 \, \Omega$, $I_4 = 4.2 \, \text{A}$,
 $R_5 = 10 \, \Omega$, $R_6 = 7.5 \, \Omega$, $R_7 = 15 \, \Omega$

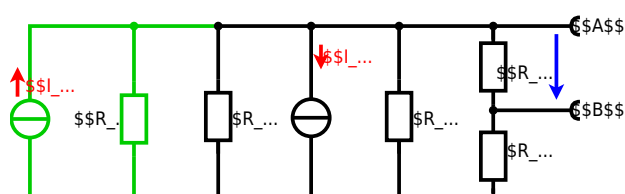
Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:

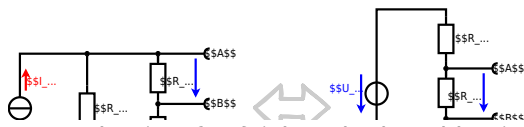


The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in

parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5 || I_{24} = I_2 - I_4 = \left\{ \frac{U_2}{R_1} \right\} - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = R_{135} \cdot I_{24} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:
$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):
$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with $R_1 || R_3 || R_5 = 5\Omega || 10\Omega || 10\Omega = 5\Omega || 5\Omega = 2.5\Omega$:

$$U_{AB} = \left(\frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \right) \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} || R_{AB} = 15\Omega || (7.5\Omega + 2.5\Omega)$$

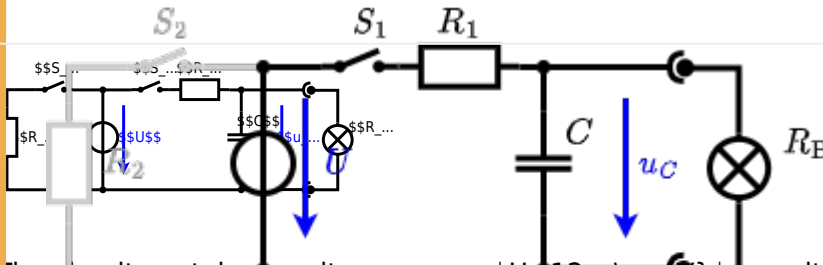
electrical_engineering_and_electronics:task_6tttque1e2nf2c7_with_calculation
dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1
ws2022

Exercise E5 Charging Capacitors**(written test, approx. 16 % of a 60-minute written test, WS2022)**

The capacitor becomes fully charged at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. The voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Hint! To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

Solution: The internal voltage source is $U_{\text{int}} = U \cdot \frac{R_B}{R_1 + R_B} = 12 \text{ V} \cdot \frac{10 \Omega}{20 \Omega + 10 \Omega} = 4 \text{ V}$. The internal resistance is $R_{\text{int}} = R_1 \parallel R_B = 6.67 \Omega$. On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

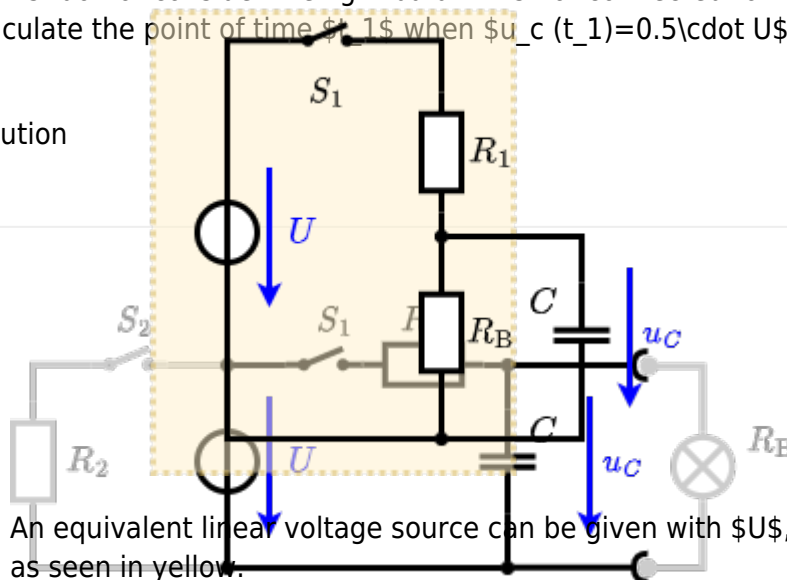


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \Omega$ and a capacitor of $C = 100 \mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.

Solution



An equivalent linear voltage source can be given with U , R_1 , and R_B as seen in yellow.

The equivalent voltage of the equivalent linear source is $U_{\text{int}} = U \cdot \frac{R_B}{R_1 + R_B} = 12 \text{ V} \cdot \frac{10 \Omega}{20 \Omega + 10 \Omega} = 4 \text{ V}$. The internal resistance is given by $R_{\text{int}} = R_1 \parallel R_B = 6.67 \Omega$. The following formula describes the time course of $u_c(t)$ which has to be rearranged to t .
$$u_c(t) = U_{\text{int}} \cdot (1 - e^{-t/\tau}) = 4 \text{ V} \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U = 6 \text{ V}$$
 It has to be rearranged to t
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = 6.67 \Omega \cdot 100 \mu\text{F} \cdot \ln(2) = 0.462 \text{ ms}$$

$$\frac{\{1\}}{2} \cdot U \cdot (1 - e^{\frac{1}{10} \cdot \Omega \cdot 100 \cdot \mu F})) \end{align*}$$

electrical_engineering_and_electronics:task_tb6pi8dgh0m2e2pw_with_calculation
charging capacitors, dc network analysis, pure resistor network simplification, delta wye
transformation, exam ee1 ws2022

Exercise E6 Analyzing complex Impedances

(written test, approx. 14 % of a 60-minute written test, WS2022)

2. Given circuit diagram below, calculate the effective value $\underline{U}$ of the voltage $\underline{u}$ across the load resistor R_L and the effective value $\underline{I}$ of the current i through the load resistor R_L . (R and X_1) shall be given.

After analysis, the following information should be extracted and documented in phase diagram (Z) and the effective value $\underline{U}$ and $\underline{I}$ shall be given.

.. Calculate the physical values of the two components.

$$\begin{aligned} \underline{U} &= \sqrt{0.24^2 + 4.68^2} = 4.72 \text{ V} \\ \underline{I} &= \sqrt{0.24^2 + 4.68^2} = 4.72 \text{ A} \end{aligned}$$

Solution

$$\begin{aligned} \underline{U} &= \sqrt{0.24^2 + 4.68^2} = 4.72 \text{ V} \\ \underline{I} &= \sqrt{0.24^2 + 4.68^2} = 4.72 \text{ A} \end{aligned}$$

$$\underline{U} = \sqrt{0.24^2 + 4.68^2} = 4.72 \text{ V}$$

$$\underline{I} = \sqrt{0.24^2 + 4.68^2} = 4.72 \text{ A}$$

$$\underline{U} = \sqrt{0.24^2 + 4.68^2} = 4.72 \text{ V}$$

electrical_engineering_and_electronics:task_jti0uzudcmg4u22t_with_calculation
complex impedance, exam ee1 ws2022

Exercise E7 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A series circuit consists of a resistor with $R_1 = 1.00 \text{ k}\Omega$, an inductor with $L = 4.7 \text{ mH}$, and a capacitor with $C = 10 \text{ nF}$. The voltage source is $u(t) = 3.0 \text{ V} \cdot \sin(2\pi \cdot 15 \text{ kHz} \cdot t)$. Calculate the effective value of the voltage across the resistor U_R and the effective value of the current I in the circuit.

Solution

$$R_1 = 1.00 \text{ k}\Omega$$

$$L = 4.7 \text{ mH}$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by

$$Z_{RL} = \sqrt{R^2 + X_L^2}$$

$$Z_{RL} = \sqrt{(1.00 \text{ k}\Omega)^2 + (2\pi \cdot 15 \text{ kHz} \cdot 4.7 \text{ mH})^2} = 10.0 \text{ k}\Omega$$

The voltage across the resistor is $U_R = I \cdot R$. It has to, since R and L are in series, be perpendicular to the voltage across the inductor U_L .

$$U_R = I \cdot R = I \cdot 1.00 \text{ k}\Omega$$

$$U_L = I \cdot X_L = I \cdot 2\pi \cdot 15 \text{ kHz} \cdot 4.7 \text{ mH}$$

$$U = \sqrt{U_R^2 + U_L^2} = I \cdot \sqrt{R^2 + X_L^2} = I \cdot Z_{RL}$$

$$I = \frac{U}{Z_{RL}} = \frac{3.0 \text{ V}}{10.0 \text{ k}\Omega} = 0.30 \text{ mA}$$

$$U_R = I \cdot R = 0.30 \text{ mA} \cdot 1.00 \text{ k}\Omega = 0.30 \text{ V}$$

$$U_L = I \cdot X_L = 0.30 \text{ mA} \cdot 2\pi \cdot 15 \text{ kHz} \cdot 4.7 \text{ mH} = 4.24 \text{ V}$$

$$U = \sqrt{U_R^2 + U_L^2} = \sqrt{0.30^2 + 4.24^2} = 4.25 \text{ V}$$

$$I = \frac{U}{Z_{RL}} = \frac{4.25 \text{ V}}{10.0 \text{ k}\Omega} = 0.425 \text{ mA}$$

$$U_R = I \cdot R = 0.425 \text{ mA} \cdot 1.00 \text{ k}\Omega = 0.425 \text{ V}$$

$$U_L = I \cdot X_L = 0.425 \text{ mA} \cdot 2\pi \cdot 15 \text{ kHz} \cdot 4.7 \text{ mH} = 4.74 \text{ V}$$

$$U = \sqrt{U_R^2 + U_L^2} = \sqrt{0.425^2 + 4.74^2} = 4.76 \text{ V}$$

electrical_engineering_and_electronics:task_pdkgtyexxy1ktu3_with_calculation
complex impedance, exam ee1 ws2022

Exercise E8 Complex Impedance Circuit**(written test, approx. 15 % of a 60-minute written test, WS2022)**

1. Calculate the effective value of the voltage across the resistor U_R and the effective value of the current I in the circuit. The voltage source is $u(t) = 3.0 \text{ V} \cdot \sin(2\pi \cdot 15 \text{ kHz} \cdot t)$. The circuit consists of a resistor with $R = 1.00 \text{ k}\Omega$, an inductor with $L = 4.7 \text{ mH}$, and a capacitor with $C = 10 \text{ nF}$.

Solution
This linear source is connected with an inductor of $L = 4.7 \text{ mH}$ and a capacitor of $C = 10 \text{ nF}$, all in series.

Result

$$Z = \sqrt{R^2 + X_L^2 + X_C^2} = \sqrt{(1.00 \text{ k}\Omega)^2 + (2\pi \cdot 15 \text{ kHz} \cdot 4.7 \text{ mH})^2 + (1/(2\pi \cdot 15 \text{ kHz} \cdot 10 \text{ nF}))^2} = 19.8 \text{ k}\Omega$$

Label the components with voltages and currents.

$$Z = \sqrt{R^2 + X_L^2 + X_C^2} = \sqrt{(1.00 \text{ k}\Omega)^2 + (2\pi \cdot 15 \text{ kHz} \cdot 4.7 \text{ mH})^2 + (1/(2\pi \cdot 15 \text{ kHz} \cdot 10 \text{ nF}))^2} = 19.8 \text{ k}\Omega$$

$$U_R = I \cdot R = 0.30 \text{ mA} \cdot 1.00 \text{ k}\Omega = 0.30 \text{ V}$$

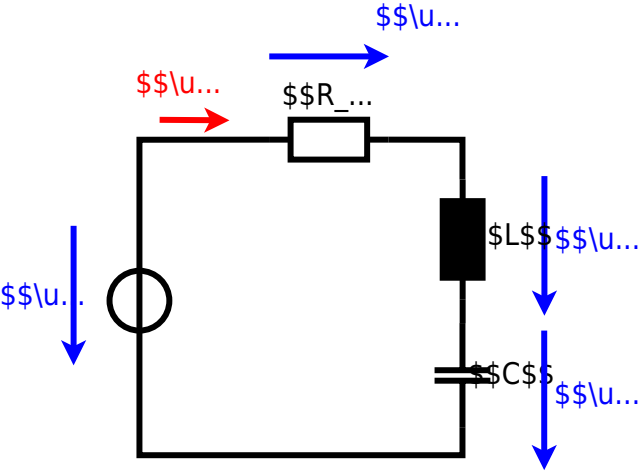
$$U_L = I \cdot X_L = 0.30 \text{ mA} \cdot 2\pi \cdot 15 \text{ kHz} \cdot 4.7 \text{ mH} = 4.24 \text{ V}$$

$$U_C = I \cdot X_C = 0.30 \text{ mA} \cdot 1/(2\pi \cdot 15 \text{ kHz} \cdot 10 \text{ nF}) = 0.30 \text{ V}$$

$$U = \sqrt{U_R^2 + U_L^2 + U_C^2} = \sqrt{0.30^2 + 4.24^2 + 0.30^2} = 4.25 \text{ V}$$

$$\begin{aligned} \underline{Z}_C &= \frac{1}{2\pi \cdot f \cdot C} \quad \&= \frac{1}{2\pi \cdot 15 \sim \{\rm kHz\} \cdot 330 \sim \{\rm \mu H\}} \\ \underline{Z} &= R + \underline{Z}_L + \underline{Z}_C \quad \&= R + j \cdot \underline{Z}_L - j \cdot \underline{Z}_C \\ &= R + j \cdot (\underline{Z}_L - \underline{Z}_C) \quad \&= \sqrt{R^2 + (\underline{Z}_L - \underline{Z}_C)^2} \end{aligned}$$

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