

ws2022_exam

Student Group

First Name	Surname	Matrikel Nr.

Table of Contents

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E1 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)	4
Exercise E1 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)	5
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)	6
Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)	8
Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)	12
Exercise E1 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)	16
Exercise E5 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)	17
Exercise E1 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)	19
Exercise E6 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)	19
Exercise E1 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)	20
Exercise E7 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)	20
Exercise E1 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)	

test, WS2022)	21
Exercise E8 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)	24

Exercise E1 Resistance of a Wire by Resistivity**(written test, approx. 6 % of a 60-minute written test, WS2022)**

A heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 is used for electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Determine the current I needed to operate the heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad \& \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity**(written test, approx. 6 % of a 60-minute written test, WS2022)**

A heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 is used for electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Determine the current I needed to operate the heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad \& \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, as shown in the figure, has a temperature coefficient of resistance $\alpha = 0.01 \text{ K}^{-1}$ and a temperature coefficient of resistance $\beta = 71 \text{ K}^{-2}$. Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: The temperature inside the refrigeration system can reach down to -40°C .

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 (1 + \alpha \Delta T + \beta \Delta T^2) \quad \text{with } \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot \left((1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2) \right)$$

Exercise E2 Temperature-dependent Resistance**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. A refrigerator, as shown in the figure, has a temperature coefficient of resistance $\alpha = 0.01 \text{ K}^{-1}$ and a temperature coefficient of resistance $\beta = 71 \text{ K}^{-2}$. Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: The temperature inside the refrigeration system can reach down to -40°C .

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 (1 + \alpha \Delta T + \beta \Delta T^2) \quad \text{with } \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot \left((1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2) \right)$$

Exercise E1 Pure Resistor Network Simplification

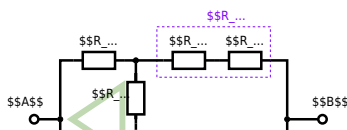
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be solved: A circuit with a switch and a resistor network is shown. The switch shall now be open. Calculate the equivalent resistance R_{eq} between terminals A and B.

Solution

$$R_{\text{eq}} = 133.8 \, \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

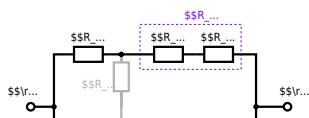
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

The switch shall now be open. Calculate the equivalent resistance R_{eq} between terminals A and B.

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_3) \parallel (R_2 + R_4) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega)$$

$$R_{eq} = \frac{(500 \, \Omega \cdot 200 \, \Omega)}{500 \, \Omega + 200 \, \Omega}$$

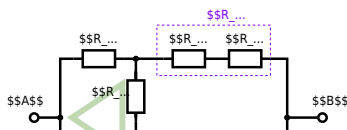
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be simplified with $R_1 = 200 \, \Omega$, $R_2 = 100 \, \Omega$, $R_3 = 150 \, \Omega$, $R_4 = 100 \, \Omega$ and the voltage source $U_{SV} = 10 \, \text{V}$.
Result given: $R_{eq} = 132.8 \, \Omega$.

Solution

$$R_{eq} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.

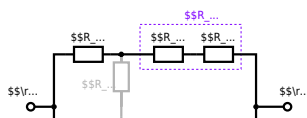


Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:
$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



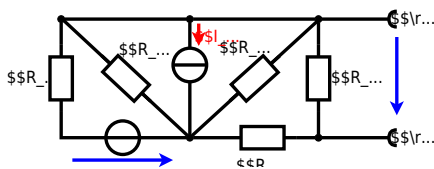
The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \{ \{ 500 \, \Omega \cdot 200 \, \Omega \} \over {500 \, \Omega + 200 \, \Omega} \} \parallel$$

Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

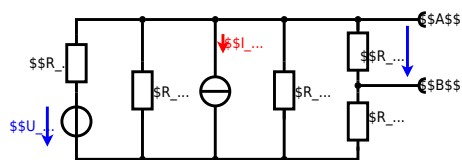
$$U_{\text{s}} = U_{\text{AB}} = 4.5 \, \text{V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \, \Omega$$



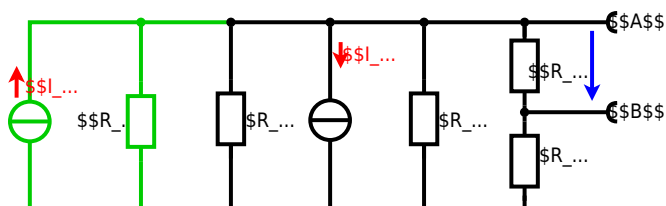
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \left\{ \frac{U_2}{R_1} \right\} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_2 \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} - I_4 \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} - (U_2 \cdot \frac{R_7}{R_1 || R_3 || R_5} - I_4) \cdot \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with $R_1 || R_3 || R_5 = 5\Omega || 10\Omega || 10\Omega = 5\Omega || 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0V}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \\ R_{AB} = 15\Omega || (7.5\Omega + 2.5\Omega)$$

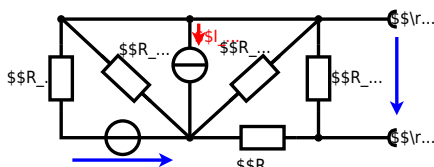
Exercise E4 Equivalent linear Source

(written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.

Result

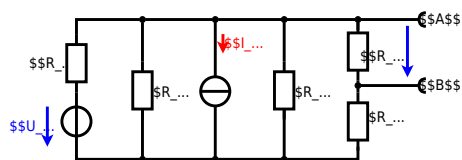
$$U_s = U_{AB} = 4.5V \\ R_i = R_{AB} = 6\Omega$$



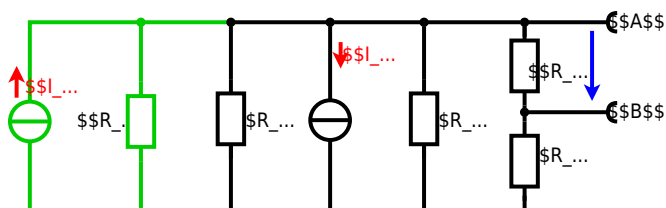
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_{24} and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_{24} - I_4 = \frac{U_{24}}{R_1} - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{135}$$

$$\&= R_{135} \cdot I_{24} \quad \&= \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:
$$U_{\rm AB}$$

$$\begin{aligned} &= U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \parallel &= \\ &(\frac{U_2}{R_1}) - I_4 \cdot \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5} \parallel \end{aligned}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($\mathcal{E}=0\Omega$, so a short-circuit):

$$R_{\text{AB}} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 || R_3 || R_5 = 5 \sim \Omega || 10 \sim \Omega || 10 \sim \Omega = 5 \sim \Omega || 5 \sim \Omega = 2.5 \sim \Omega$:

$$\begin{aligned} U_{\rm AB} &= \left(\frac{6.0 \, \rm V}{5.0 \, \Omega} - 4.2 \, \Omega \right) \\ &\cdot \left(\frac{15 \, \Omega \cdot 2.5 \, \Omega}{7.5 \, \Omega + 15 \, \Omega + 2.5 \, \Omega} \right) \\ R_{\rm AB} &= 15 \, \Omega \parallel (7.5 \, \Omega + 2.5 \, \Omega) \end{aligned}$$

Exercise E1 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (with one real battery) dissipates no power in the $20\text{-}\mu\text{F}$ capacitor, so the voltage across the capacitor is again 0 V at the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

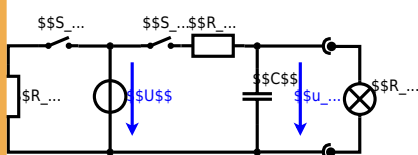
```

% To solve this, first create an equivalent linear voltage source from $U$, $R_1$, and
% $R_2$.
\begin{align*} U_{\text{eq}} &= \frac{U}{1 + \frac{R_1}{R_2}} \\ R_{\text{eq}} &= \frac{R_1 R_2}{R_1 + R_2} \end{align*}

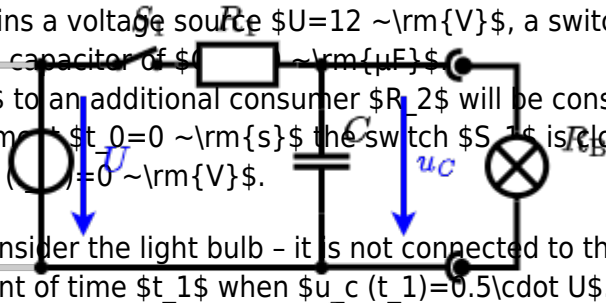
```

$$\text{The ideal voltage source } V_0 \text{ is independent of } V$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_{25} .



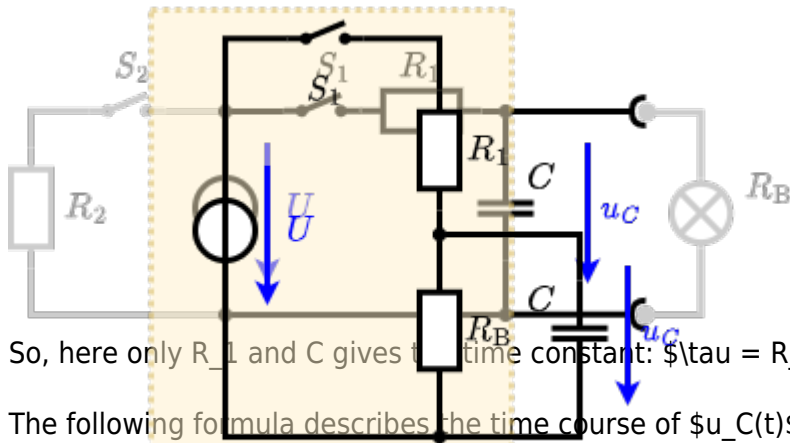
The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$. An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V DC voltage source U , a switch S_1 , a resistor $R_1=20\text{ }\Omega$, a capacitor $C=100\text{ }\mu\text{F}$, and a light bulb $R_B=20\text{ }\Omega$. The switch S_2 is open. At the moment $t_0=0\text{ s}$ when the switch S_1 is closed, the voltage across the capacitor is again 0 V . Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution

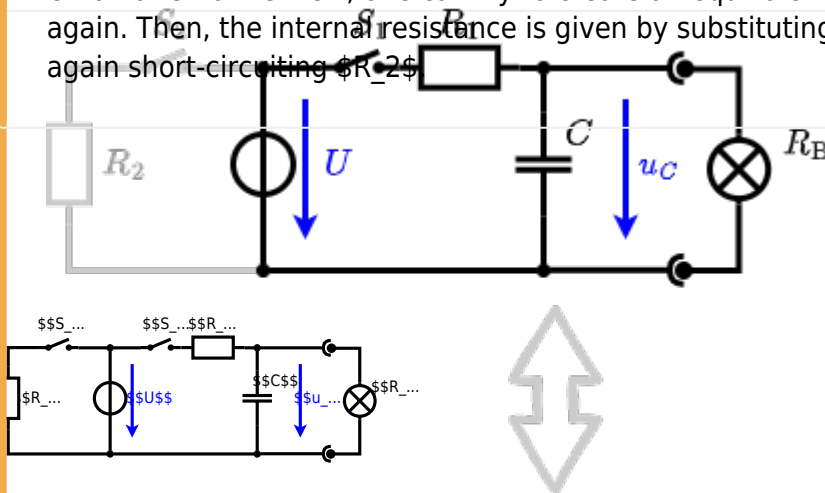
To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

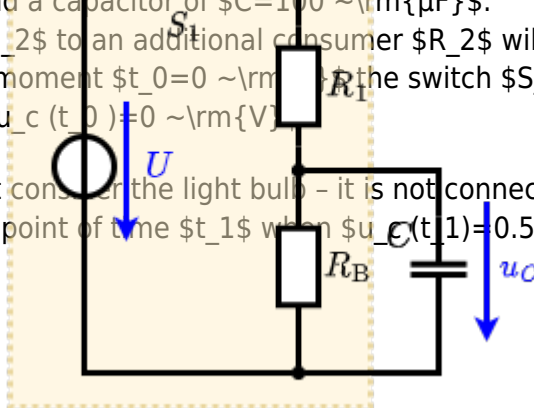


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$

It has to be rearranged to t :

$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) \implies t = R_1 \cdot C \cdot \ln(0.5)$$

Exercise E1 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (φ and φ_L) shall be given.

After analysis, the full bridge dimensioned circuit impedance can be extracted and the phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right)$.

.. Calculate the physical values of the two components.

Solution $\varphi = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.06^\circ$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.42 \angle 87.06^\circ$ A

The current and voltage phase angle difference is $\varphi = 87.06^\circ$ (real) resulting impedance $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 4.68Ω is a capacitor with the same absolute value of 4.68Ω impedance. $\underline{X}_L = j\omega L$ and $\underline{X}_C = -j\omega C$ $\Rightarrow \underline{X}_C = -j4.68 \Omega$ $\Rightarrow C = \frac{1}{\omega \cdot 4.68} = \frac{1}{300 \cdot 4.68} = 0.707 \mu\text{F}$

The physical value φ_L can be calculated as $\varphi_L = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.06^\circ$

With the complex part $\varphi_L = -87.06^\circ$ $\Rightarrow \varphi_L = -87.06^\circ$ $\Rightarrow \varphi_L = -87.06^\circ$ $\Rightarrow \varphi_L = -87.06^\circ$

The phase φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.06^\circ$

Exercise E6 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (φ and φ_L) shall be given.

After analysis, the full bridge dimensioned circuit impedance can be extracted and the phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right)$.

.. Calculate the physical values of the two components.

Solution $\varphi = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.06^\circ$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.42 \angle 87.06^\circ$ A

The current and voltage phase angle difference is $\varphi = 87.06^\circ$ (real) resulting impedance $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 4.68Ω is a capacitor with the same absolute value of 4.68Ω impedance. $\underline{X}_L = j\omega L$ and $\underline{X}_C = -j\omega C$ $\Rightarrow \underline{X}_C = -j4.68 \Omega$ $\Rightarrow C = \frac{1}{\omega \cdot 4.68} = \frac{1}{300 \cdot 4.68} = 0.707 \mu\text{F}$

The physical value φ_L can be calculated as $\varphi_L = \arctan\left(\frac{\text{Im}(\underline{Z})}{\text{Re}(\underline{Z})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.06^\circ$

The absolute value of the impedance is $\sqrt{(0.24 \sim \Omega)^2 + (4.68 \sim \Omega)^2} = 4.7 \sim \Omega$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.
 With the complex part comes the physical value: $X_L = \omega L = 2\pi \cdot 4.7 \sim \Omega$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.

Exercise E1 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.
 Back to the first formula: $R_3 \cdot I_3 = X_{L2} \cdot I_2 = X_{L2} \cdot I_1$.
 Result: $R_3 = \frac{X_{L2} \cdot I_1}{I_3} = \frac{2\pi \cdot 4.7 \sim \Omega \cdot 10 \sim \text{mA}}{1 \sim \text{mA}} = 94 \sim \Omega$.

Solution

$R_1 = 1.00 \sim \Omega$

$R_2 = 10.0 \sim \Omega$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.

Parallel circuit means that the voltage is the same on R_2 and C_2 .
 $\underline{U} = \underline{U}_R = \underline{U}_C$.
 $\underline{U} = \underline{U}_R = \underline{U}_C$.
 $\underline{U} = \underline{U}_R = \underline{U}_C$.

$\underline{U} = \underline{U}_R = \underline{U}_C$.
 $\underline{U} = \underline{U}_R = \underline{U}_C$.
 $\underline{U} = \underline{U}_R = \underline{U}_C$.

Therefore, the resulting current of the parallel circuit is given as:

$\underline{I} = \underline{I}_R + \underline{I}_C$

$\underline{I} = \underline{I}_R + \underline{I}_C$.
 $\underline{I} = \underline{I}_R + \underline{I}_C$.
 $\underline{I} = \underline{I}_R + \underline{I}_C$.

Back to the first formula: $R_3 \cdot I_3 = X_{L2} \cdot I_2 = X_{L2} \cdot I_1$.

Result: $R_3 = \frac{X_{L2} \cdot I_1}{I_3} = \frac{2\pi \cdot 4.7 \sim \Omega \cdot 10 \sim \text{mA}}{1 \sim \text{mA}} = 94 \sim \Omega$.

Back to the first formula: $R_3 \cdot I_3 = X_{L2} \cdot I_2 = X_{L2} \cdot I_1$.

Result: $R_3 = \frac{X_{L2} \cdot I_1}{I_3} = \frac{2\pi \cdot 4.7 \sim \Omega \cdot 10 \sim \text{mA}}{1 \sim \text{mA}} = 94 \sim \Omega$.

Result: $R_3 = \frac{X_{L2} \cdot I_1}{I_3} = \frac{2\pi \cdot 4.7 \sim \Omega \cdot 10 \sim \text{mA}}{1 \sim \text{mA}} = 94 \sim \Omega$.

Exercise E7 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

Exercise E1 Complex Impedance Circuit
(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the following diagram (of 3S) 21.B.0
 $\sim \sqrt{R} \cdot \sin(2\pi \cdot 450 \cdot t) \text{ Hz}$ high-pass filter circuit. $R_1 = 10 \Omega$, $R_2 = 10 \Omega$, $R_3 = 10 \Omega$, $C_1 = 40 \text{ nF}$, $C_2 = 40 \text{ nF}$, $L_1 = 4 \text{ mH}$.
 The resistor R_1 shall have the same absolute value of the impedance as a capacitor

$C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution: $R_1 = 1.00 \Omega$

Solution: $R_2 = 10.0 \Omega$

Solution

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by

Parallel circuit means that the voltage is the same on R_1 and R_2 .
 $R_{\text{parallel}} = R_1 \parallel R_2 = \frac{R_1 \cdot R_2}{R_1 + R_2} = \frac{10 \cdot 10}{10 + 10} = 5 \Omega$
 Since L is in series with R_{parallel} , the total impedance is $Z = R_{\text{parallel}} + j\omega L = 5 + j\omega L$

$Z = 5 + j\omega L$ is perpendicular to R_1 and R_2 . (It has to, since R_1 and R_2 are in parallel and L is in series with them.)

Therefore, the resulting current of the parallel circuit is given as:

$I_{\text{parallel}} = I_{R1} + I_{R2} = \frac{U}{R_1} + \frac{U}{R_2} = \frac{U}{R_{\text{parallel}}}$

This can be rearranged to $I_{\text{parallel}} = \frac{U}{R_{\text{parallel}}}$.
 $I_{\text{parallel}} = \frac{U}{R_{\text{parallel}}} = \frac{U}{5 + j\omega L}$

Back to the first formula: $R_3 \cdot I_{\text{parallel}} = X_{L1} \cdot I_{\text{parallel}}$

$R_3 \cdot I_{\text{parallel}} = X_{L1} \cdot I_{\text{parallel}}$

$R_3 \cdot I_{\text{parallel}} = X_{L1} \cdot I_{\text{parallel}}$

$R_3 \cdot I_{\text{parallel}} = X_{L1} \cdot I_{\text{parallel}}$

$R_3 \cdot I_{\text{parallel}} = X_{L1} \cdot I_{\text{parallel}}$

Exercise E1 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the following diagram (of 3S) 21.B.0
 $\sim \sqrt{R} \cdot \sin(2\pi \cdot 450 \cdot t) \text{ Hz}$ high-pass filter circuit. $R_1 = 10 \Omega$, $R_2 = 10 \Omega$, $R_3 = 10 \Omega$, $C_1 = 40 \text{ nF}$, $C_2 = 40 \text{ nF}$, $L_1 = 4 \text{ mH}$.
 The resistor R_1 shall have the same absolute value of the impedance as a capacitor

Solution: This linear source is connected with an inductor of $330 \mu\text{H}$ and a capacitor of $0.22 \mu\text{F}$, all in series.

Result

$Z = 107.37 \Omega$

Draw the circuit diagram of the given circuit.

$Z = \frac{U}{I} = \frac{U}{I} = \frac{U}{I}$

$Z_C = \frac{1}{j\omega C} = \frac{1}{j\omega C}$

Result: $Z = 107.37 \Omega$

$Z = 107.37 \Omega$

$Z = 107.37 \Omega$

$Z = 107.37 \Omega$

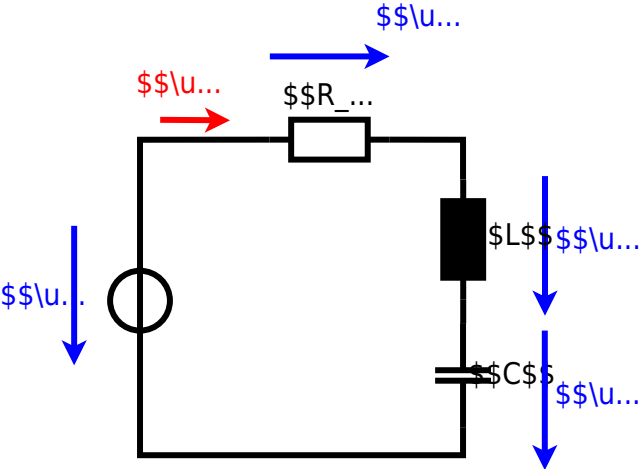
$Z = 107.37 \Omega$

$Z = 107.37 \Omega$

$Z = 107.37 \Omega$

$Z = 107.37 \Omega$





Exercise E8 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

[illegible]

This linear source is connected with an inductor of $330 \sim \{\rm \mu H\}$ and a capacitor of $30.22 \sim \{\rm \mu F\}$, all in series.

Result

$$\begin{aligned} \text{Decline in } \mu_{\text{H}} &= 107.31 \text{ km} \cdot \text{Mpc}^{-1} \text{ and } \sigma_{\text{H}} = 48.2 \sim \Omega_{\text{M}} \parallel Z = 19.8 \sim \Omega_{\text{M}} \end{aligned}$$

label all components, voltages, and currents.

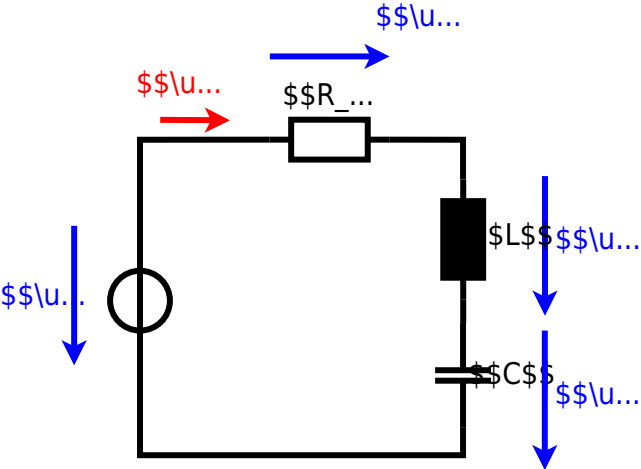
$$\begin{aligned} Z &= \{ \{ \hat{U} \} \over \{ \hat{I} \} \} \parallel \hat{I} = \{ \{ \hat{U} \} \over \{ Z \} \} \parallel \end{aligned}$$
$$\backslash \text{end{ifalldiv}} \} Z \ C \ \&= \ \{ \{ 1 \} \over { 2 \pi \cdot f \cdot C } \} \backslash \backslash \ \&= \ \{ \{ 1 \} \over { 2 \pi \cdot 15}$$
$$\text{Result} \{ \text{rm kHz} \} \cdot 0.22 \sim \{ \text{rm } \mu\text{F} \} \} \} \} \end{align*}$$
$$\text{With } \mathbf{f} = \mathbf{f}(\mathbf{r}) \text{ over } \mathbf{r} \in \mathbb{R}^3 \text{ and } \mathbf{h} \in \mathbb{R}^3, \mathbf{f} \cdot \mathbf{h} = \mathbf{f} \cdot \mathbf{h} \text{ kHz} \cdot 0.22$$
$$\frac{1}{\sqrt{2}} \cdot \frac{\hat{U}}{Z} \parallel = \frac{1}{\sqrt{2}} \cdot$$
$$\frac{\sqrt[3]{0}\sqrt[3]{\rm{m}^*V}}{Z}\overline{\omega}=\frac{19.28}{\Omega}\overline{\omega}\not\equiv\frac{1}{2\pi}\cdot 15$$
$$\sim \{\rm km\ kHz\} \cdot \dot{M} \approx 330 \cdot \dot{M}$$

$$\underline{Z} \equiv B + \underline{Z} \quad I + \underline{Z} \quad C \equiv B + i$$

$$\underline{\delta} := \mathbf{R} + i \underline{\delta} \cdot (\mathbf{I} - \mathbf{C}) \quad \underline{\delta} := \mathbf{R} + i \underline{\delta} \cdot (\mathbf{I} - \mathbf{C})$$

$$\sqrt{B^2 + (\underline{Z} - \underline{Z}_C)^2} \quad \text{end{align*}}$$

$$\sqrt{\{R \mid Z \neq (\underline{Z}_L - \underline{Z}_C) \mid Z\}}$$



From:

<https://wiki.mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:

https://wiki.mexle.te.hs-heilbronn.de/ee1/ws2022_exam

Last update: **2023/04/02 00:45**

