

Exam Winter Semester 2022

Student Group

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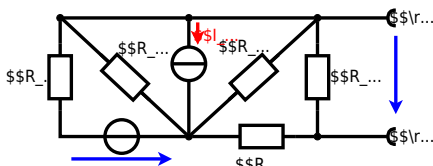
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Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

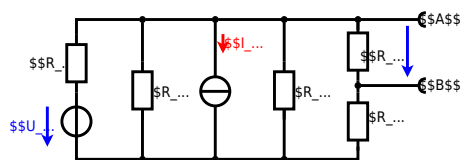
$$\begin{aligned} U_{\text{rs}} &= U_{\text{AB}} = 4.5 \text{ V} \\ R_{\text{i}} &= R_{\text{AB}} = 6 \text{ } \Omega \end{aligned}$$



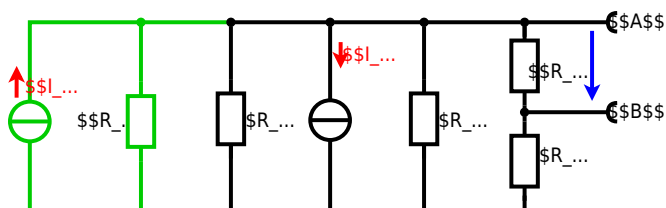
Calculated the internal resistance R_{i} and the source voltage U_{rs} of an equivalent linear voltage source on the connectors A and B .
$$\begin{aligned} R_1 &= 5.0 \text{ } \Omega, \quad U_2 = 6.0 \text{ V}, \quad R_3 = 10 \text{ } \Omega, \quad I_4 = 4.2 \text{ A}, \\ R_5 &= 10 \text{ } \Omega, \quad R_6 = 7.5 \text{ } \Omega, \quad R_7 = 15 \text{ } \Omega \end{aligned}$$
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24}$$

$$U_{24} = U_{23} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

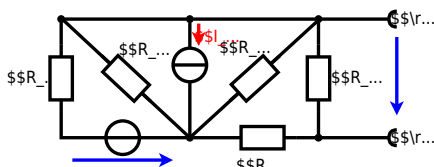
with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \parallel R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

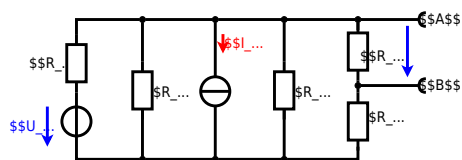
$$U_s = U_{AB} = 4.5\text{V} \parallel R_i = R_{AB} = 6\Omega$$



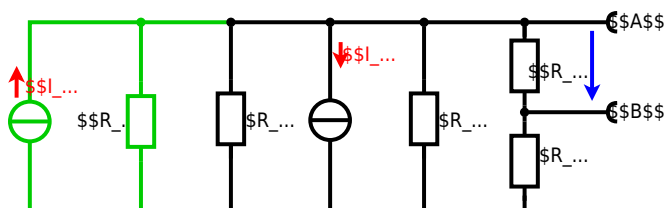
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

The phase φ can be calculated as
$$\varphi_i = \arctan \left(\frac{\operatorname{Im}(\underline{Z})}{\operatorname{Re}(\underline{Z})} \right) = \arctan \left(\frac{-4.68 \sim \Omega}{0.24 \sim \Omega} \right)$$

Exercise E6 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. A circuit has been analyzed and the following values have been determined: $\underline{U} = 50 \text{ V}$ and $\underline{Z} = 0.24 - j4.68 \sim \Omega$. The current $\underline{I}$ through the components ($\$R\$ and $\$X_L\$$) shall be given.$

After analysis, the full complex impedance has been extracted and the magnitude in phase (calculated as $\sqrt{0.24^2 + 4.68^2} = 4.72 \sim \Omega$) and the phase angle $\varphi = \arctan(-4.68/0.24) = -87.06^\circ$ have been determined.

3. Calculate the physical values of the components.

Solution:
$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \text{ V}}{4.72 \sim \Omega \angle -87.06^\circ} = 10.61 \text{ A} \angle 87.06^\circ$$

Solution

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \text{ V}}{0.24 - j4.68 \sim \Omega} = 10.61 \text{ A} \angle 87.06^\circ$$

The current and voltage are in phase since the impedance is purely real.

resulting in $\underline{I} = 10.61 \text{ A} \angle 87.06^\circ$ and $\underline{U} = 50 \text{ V} \angle 0^\circ$.

The magnitude of the current is $I = 10.61 \text{ A}$ and the phase angle is $\varphi = 87.06^\circ$.

Impedance $\underline{Z} = 0.24 - j4.68 \sim \Omega$ can be written as $\underline{Z} = 4.72 \sim \Omega \angle -87.06^\circ$.

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \text{ V}}{4.72 \sim \Omega \angle -87.06^\circ} = 10.61 \text{ A} \angle 87.06^\circ$$

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Exercise E1 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)

2. A circuit has been analyzed and the following values have been determined: $\underline{U} = 50 \text{ V}$ and $\underline{Z} = 0.24 - j4.68 \sim \Omega$. The current $\underline{I}$ through the components ($\$R\$ and $\$X_L\$$) shall be given.$

After analysis, the full complex impedance has been extracted and the magnitude in phase (calculated as $\sqrt{0.24^2 + 4.68^2} = 4.72 \sim \Omega$) and the phase angle $\varphi = \arctan(-4.68/0.24) = -87.06^\circ$ have been determined.

3. Calculate the physical values of the components.

Solution:
$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \text{ V}}{4.72 \sim \Omega \angle -87.06^\circ} = 10.61 \text{ A} \angle 87.06^\circ$$

Solution

Solution

A series circuit means that the current is constant on every component.

The equivalent impedance for R_2 and L combined is given by

$$\underline{Z} = R_2 + j\omega L$$

Since $j\omega L$ is perpendicular to R_2 , this can be simplified to

$$|\underline{Z}|^2 = R_2^2 + (\omega L)^2$$

So it gets clear that $\underline{Z}$ is perpendicular to $\underline{I}$ (It has to, since R_2 is perpendicular to $j\omega L$, too).

Therefore the resulting current of the parallel circuit is given as:

$$|\underline{I}| = \frac{|\underline{U}|}{\sqrt{R_2^2 + (\omega L)^2}}$$

Back to the first formula:

$$R_3 \cdot |\underline{I}| = |\underline{X}| \cdot |\underline{I}| \Rightarrow R_3 = |\underline{X}| \cdot \frac{|\underline{I}|}{|\underline{I}|} = |\underline{X}| \cdot \frac{|\underline{U}|}{\sqrt{R_2^2 + (\omega L)^2}}$$

Exercise E7 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A series circuit with $R_1 = 1.00 \text{ } \Omega$, $R_2 = 10.0 \text{ } \Omega$, $L = 4.7 \text{ } \mu\text{H}$, and $C = 40 \text{ nF}$ is connected to a voltage source $\underline{U} = 10 \text{ V}$. The frequency $f = 450 \text{ kHz}$ is high enough to neglect the inductance of the capacitor C . The resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution

$$R_1 = 1.00 \text{ } \Omega$$

$$R_2 = 10.0 \text{ } \Omega$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R_2 and L combined is given by

$$\underline{Z} = R_2 + j\omega L$$

Since $j\omega L$ is perpendicular to R_2 , this can be simplified to

$$|\underline{Z}|^2 = R_2^2 + (\omega L)^2$$

So it gets clear that $\underline{Z}$ is perpendicular to $\underline{I}$ (It has to, since R_2 is perpendicular to $j\omega L$, too).

Therefore the resulting current of the parallel circuit is given as:

$$|\underline{I}| = \frac{|\underline{U}|}{\sqrt{R_2^2 + (\omega L)^2}}$$

Back to the first formula:

$$R_3 \cdot |\underline{I}| = |\underline{X}| \cdot |\underline{I}| \Rightarrow R_3 = |\underline{X}| \cdot \frac{|\underline{I}|}{|\underline{I}|} = |\underline{X}| \cdot \frac{|\underline{U}|}{\sqrt{R_2^2 + (\omega L)^2}}$$

$$\frac{|I_{3R}|^2}{|I_{3R}|} \quad \quad \quad \end{align*}$$

Exercise E1 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

[illegible]

Solution
This linear source is connected with an inductor of $330 \sim \{\rm \mu H\}$ and a capacitor of $0.22 \sim \{\rm \mu F\}$, all in series.

Result

Draw the circuit diagram of the given circuit.

label all components, voltages, and currents.

$$\begin{aligned} \begin{aligned} \text{\texttt{\textbackslash begin{align*}}} \quad Z &= \left\{ \frac{\text{\texttt{\textbackslash that\{U\}}}}{\text{\texttt{\textbackslash hat\{I\}}}} \right\} \quad \text{\texttt{\textbackslash \hat{I}}} &= \left\{ \frac{\text{\texttt{\textbackslash hat\{U\}}}}{\text{\texttt{\textbackslash Z\}}} \right\} \quad \text{\texttt{\textbackslash end{align*}}} \\ Z \quad C &= \left\{ \frac{1}{2\pi \cdot f \cdot C} \right\} \quad \text{\texttt{\textbackslash \&}} = \left\{ \frac{1}{2\pi \cdot 15} \right\} \end{aligned} \end{aligned}$$

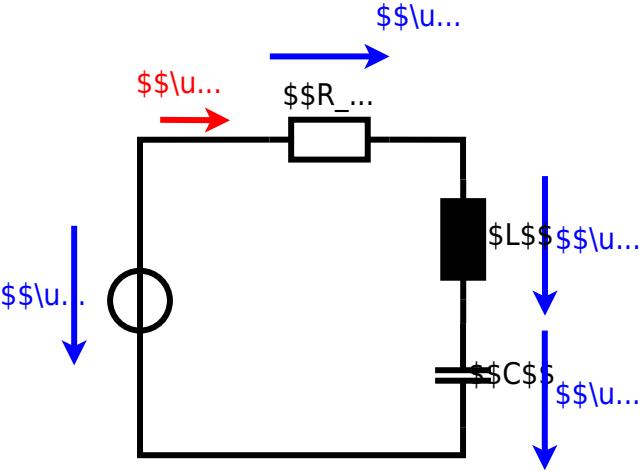
$$\text{sat}\{\text{rm kHz}\} \cdot 0.22 \sim \{\text{rm }\mu\text{F}\}\}\end{align*}$$

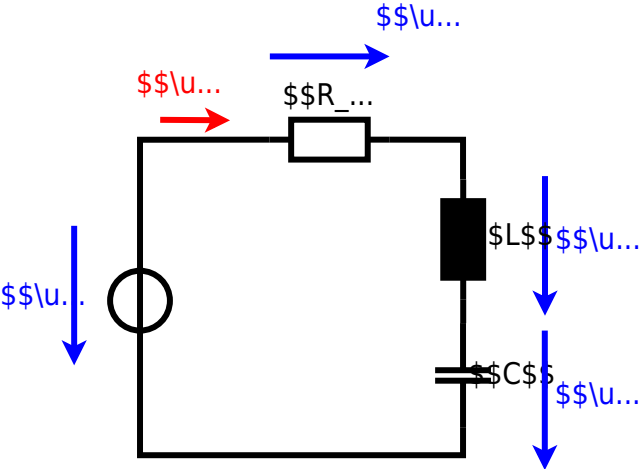
With $\{align* \} \overline{v_L} = \sqrt{p^2 + q^2} \exp(i \phi)$ & $\{align* \} \overline{v_R} = \sqrt{p^2 + q^2} \exp(i \phi)$.

$$\{1\} \bmod \{\sqrt{2}\} \text{ aligned with } \{\hat{U}\} \text{ over } \{Z\} \quad \&= \quad \{1\} \text{ over } \{\sqrt{2}\} \cdot$$

$$\nu_{\text{eg}} = \frac{1}{2\pi} \left(\frac{1}{\tau_{\text{eg}}} + \frac{1}{\tau_{\text{eg}}'} \right) \approx 15 \text{ kHz} \cdot 330 \text{ }\mu\text{H}$$

$$\begin{aligned} \underline{Z} &= R + \underline{Z}_L + \underline{Z}_C \\ \underline{Z}_L - j &= R + j \underline{Z}_C \\ \underline{Z}_L - \underline{Z}_C &= \sqrt{R^2 + (\underline{Z}_L - \underline{Z}_C)^2} \end{aligned}$$





Exercise E1 Pure Resistor Network Simplification

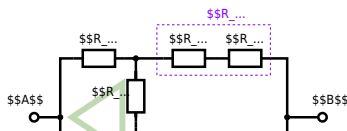
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be closed and integrated, $R_2 = R_3 = 100 \Omega$ and the switch between R_3 and R_4 shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{\text{eq}} = 133.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

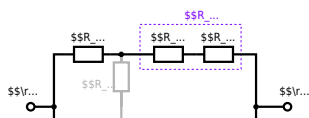
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

.. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim \Omega + 200 \sim \Omega + 200 \sim \Omega) \parallel (100 \sim \Omega + 100 \sim \Omega) \parallel R_{\text{eq}} = (500 \sim \Omega) \parallel (200 \sim \Omega) \parallel R_{\text{eq}} = \{ \{ 500 \sim \Omega \cdot 200 \sim \Omega \} \over {500 \sim \Omega + 200 \sim \Omega} \} \parallel$$

Exercise E1 Charging Capacitors

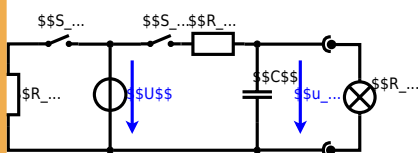
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit below is a simple RC circuit. It consists of a DC voltage source U , a resistor R_1 , a capacitor C , and a switch S . The switch S is initially open. The voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

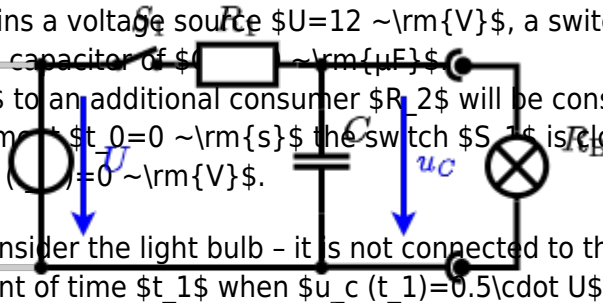
Solution
To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

$$U_{\text{eq}} = \frac{U \cdot R_2}{R_1 + R_2} \quad R_{\text{eq}} = R_1 \parallel R_2 = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



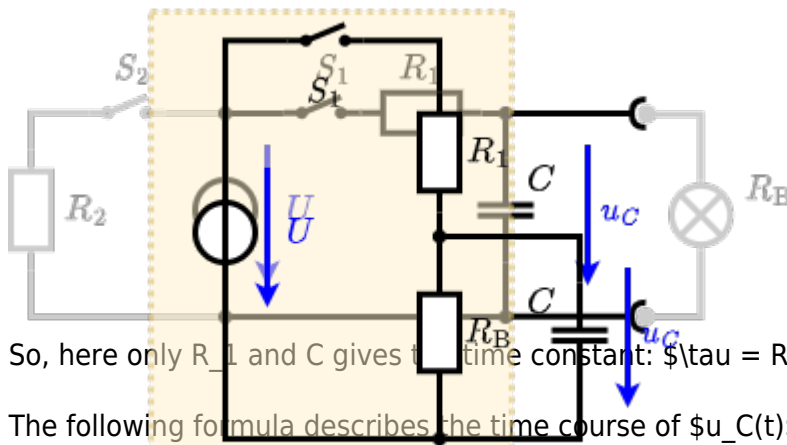
The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$. An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit diagram shows a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution

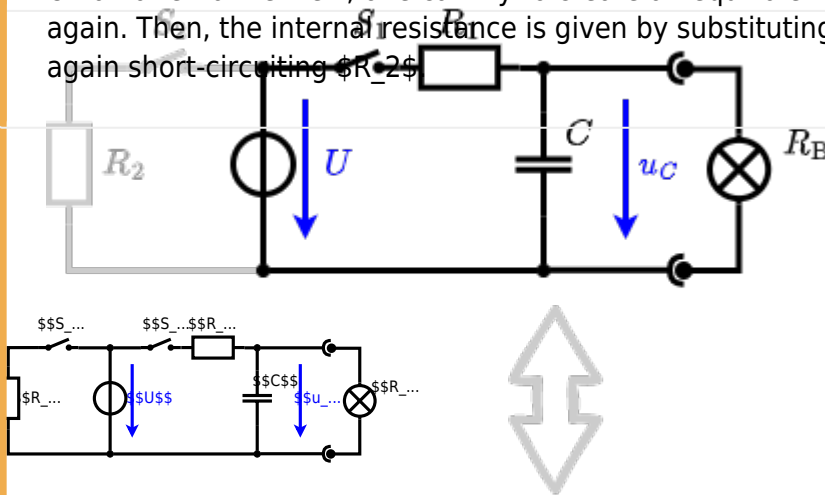
To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

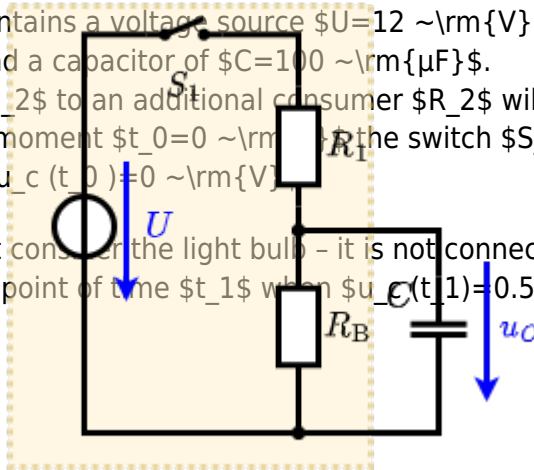


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$

It has to be rearranged to t :

$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$

Exercise E1 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

[illegible]

Its temperature coefficients are: $\alpha = 0.01 \text{ } ^\circ\text{C}^{-1}$ and $\beta = 71 \times 10^{-6} \text{ } ^\circ\text{C}^{-2}$

Result The temperature inside the refrigeration system can reach down to $-40 \sim 0^{\circ}\text{C}$.

$$R_s = 65 \sqrt{\frac{1}{\Omega}} \quad (4)$$

The power transfer is too slow, and the efficiency is too low. Therefore, a solution is to use a heat exchanger to pre-heat the refrigerant before it enters the compressor.

Therefore, with constant $\$U\$$ and increasing $\$R\$$ the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad \&\amp; \quad \Delta T = T_{\text{end}} - T_{\text{start}} \quad \&\& \quad R = 10 \sim \text{m}\{\text{k}\} \cdot \Omega \cdot \left((1 + 0.01 \sim \frac{1}{\text{m}\{\text{K}\}}) \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\}) + 71 \cdot 10^{-6} \sim \frac{1}{\text{m}\{\text{K}\}^2} \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\})^2 \right)$$

Exercise E2 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. The grid below expires 24 hours after the test is sent on the date you submit this form. It has a Residual of \$100 per month for 12 months. Give an \$25 donation for your answer.

Its temperature coefficients are: $\alpha = 0.01 \text{ } ^\circ\text{C}^{-1}$ and $\beta = 71 \times 10^{-6} \text{ } ^\circ\text{C}^{-2}$

Result The temperature inside the refrigeration system can reach down to $-40 \sim ^\circ\text{C}$.

$R_s = 65 \, \Omega$ Calculate the resistance of the thermistor at 40°C .

The power transfer ratio is $\frac{P_{\text{out}}}{P_{\text{in}}} = \frac{I_{\text{out}}^2 R_{\text{load}}}{I_{\text{in}}^2 R_{\text{load}} + I_{\text{in}}^2 R_{\text{coil}}}$. The efficiency is $\eta = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{I_{\text{out}}^2 R_{\text{load}}}{I_{\text{in}}^2 R_{\text{load}} + I_{\text{in}}^2 R_{\text{coil}}}$. Therefore, a solution is to use a thermoelectric cooler (TEC) to cool the refrigeration system.

Therefore, with constant $\$U\$$ and increasing $\$R\$$ the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$\begin{aligned} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad \& | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} \quad \& | \\ R &= 10 \sim \text{m}\{\text{k}\} \cdot \Omega \cdot \left((1 + 0.01 \sim \frac{1}{\text{m}\{\text{K}\}}) \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\}) + 71 \cdot 10^{-6} \sim \frac{1}{\text{m}\{\text{K}\}^2} \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\})^2 \right) \end{aligned}$$

Exercise E3 Pure Resistor Network Simplification

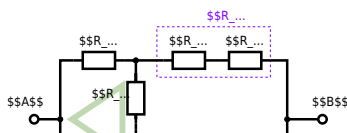
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be closed at 100 Ω and the equivalent resistance R_{eq} between A and B shall be calculated.

Solution

$$R_{\text{eq}} = 133.8 \, \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

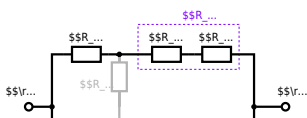
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$\begin{aligned} R_{\text{eq}} &= (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \sim \Omega + 200 \sim \Omega + 200 \sim \Omega) \parallel (100 \sim \Omega + 100 \sim \Omega) \parallel \\ R_{\text{eq}} &= (500 \sim \Omega) \parallel (200 \sim \Omega) \parallel R_{\text{eq}} = \{ \{ 500 \sim \Omega \cdot 200 \sim \Omega \} \over {500 \sim \Omega + 200 \sim \Omega} \} \parallel \\ \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

2. The heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 and an electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Calculate the current I needed to operate it.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \sim \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \parallel R = \\ 1.10 \cdot 10^{-6} \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} & \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. For a heating element is used to heat wire even to a temperature of 180°C . An electric power dissipation (= heat flow) of $P=40\text{ W}$ is necessary.

Calculate the current I needed to operate it.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6}\text{ }\Omega\text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40\text{ W}}{0.33\text{ }\Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad \text{with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad | \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad | \quad R = \\ 1.10 \cdot 10^{-6}\text{ }\Omega\text{ m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

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