

Exam Winter Semester 2022

Student Group

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Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

2. For heating elements made of solid nichrome wire with a cross-section of 1.80 mm^2 , an electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.
 Determine the current I needed for heating elements.
 The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.
 The heating element is 3 m long and has a diameter of 3.57 mm .
 Solution in align^* $R = 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$ align^*
 2. Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad | \text{ with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad \& \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \& \quad R = \\ 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \quad \& \quad \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

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Exercise E1 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. Additionally, explain why the effect of constant temperature inside the refrigeration system can be identified. Result: The resistance of the thermistor is $R = 10 \cdot 10^3 \cdot \Omega$ at $T = 25^\circ\text{C}$ for your answer.

Its temperature coefficients are: $\alpha = 0.01 \cdot 10^{-6} \cdot 1/\text{K}$ and $\beta = 71 \cdot 10^{-6} \cdot 1/\text{K}^2$

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

The resistance of the thermistor is $R = 10 \cdot 10^3 \cdot \Omega$ at $T = 25^\circ\text{C}$. Therefore, a solution is to use a float up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \cdot 10^3 \cdot \Omega \cdot \left(1 + 0.01 \cdot 10^{-6} \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2 \right)$$

Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. Additionally, explain why the effect of constant temperature inside the refrigeration system can be identified. Result: The resistance of the thermistor is $R = 10 \cdot 10^3 \cdot \Omega$ at $T = 25^\circ\text{C}$ for your answer.

Its temperature coefficients are: $\alpha = 0.01 \cdot 10^{-6} \cdot 1/\text{K}$ and $\beta = 71 \cdot 10^{-6} \cdot 1/\text{K}^2$

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$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \cdot 10^3 \cdot \Omega \cdot \left(1 + 0.01 \cdot 10^{-6} \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2 \right)$$

Exercise E1 Pure Resistor Network Simplification

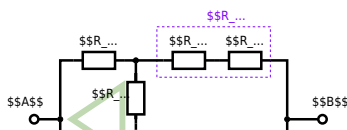
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be closed and integrated, $R_2 = R_3 = 100 \Omega$ and the switch between R_3 and R_4 shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{\text{eq}} = 133.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

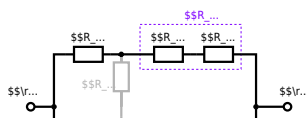
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega}$$

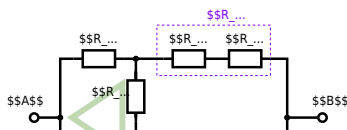
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved with \$R_1 = 200 \, \Omega\$, \$R_2 = 100 \, \Omega\$, \$R_3 = 150 \, \Omega\$, \$R_4 = 100 \, \Omega\$, and the source \$U_{SV} = 10 \, \text{V}\$. The result shall be given in \$\Omega\$.

Solution

$$R_{\text{eq}} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.



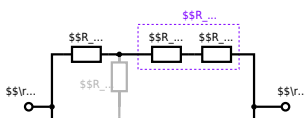
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega) \parallel$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



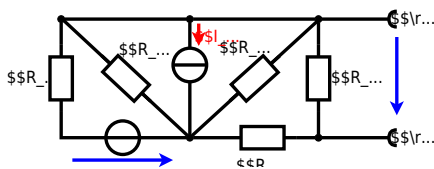
The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel R_{\text{eq}} = (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \parallel R_{\text{eq}}$$

Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

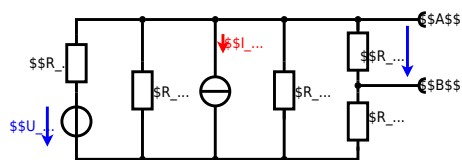
$$U_{\text{s}} = U_{\text{AB}} = 4.5 \, \text{V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \, \Omega$$



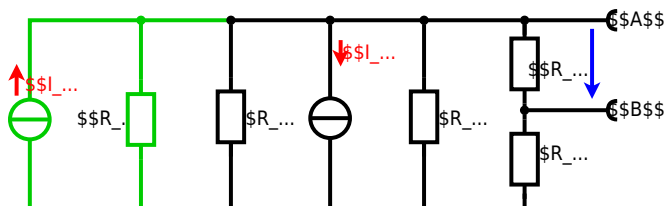
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_{24} and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_{24} - I_4 = \frac{U_{24}}{R_1} - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_{23} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

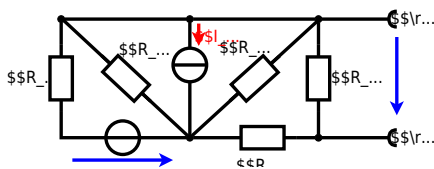
with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \parallel R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

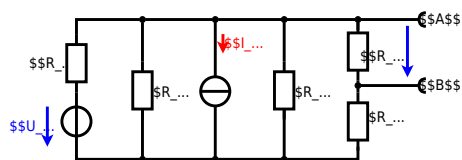
$$U_s = U_{AB} = 4.5\text{V} \parallel R_i = R_{AB} = 6\Omega$$



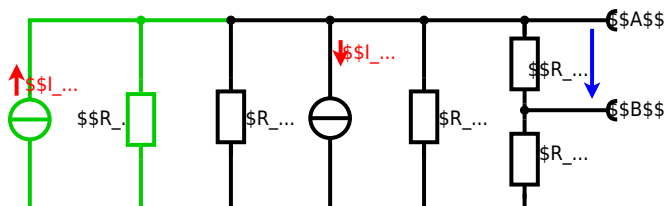
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{AB} = U_{24} \cdot \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

$$U_{AB} = U_{24} \cdot \left(\frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} \right) \cdot \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \left(\frac{6.0\text{V}}{5.0\Omega} - 4.2\text{A} \right) \cdot \left(\frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \right) \cdot R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E1 Charging Capacitors

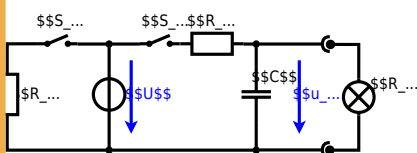
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit below is a fully charged circuit with a DC voltage source $U = 12\text{V}$, a resistor $R_1 = 10\Omega$, a capacitor $C = 2\mu\text{F}$, and a switch S_1 . The voltage across the capacitor is again 0V at the moment $t_0 = 0\text{s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1\text{ms}$ after closing the switch.

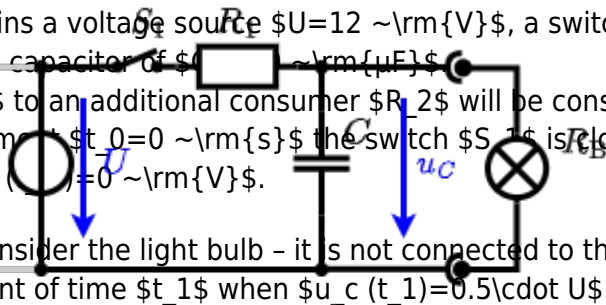
Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

$$U_{\text{eq}} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{12\text{V} \cdot 10\Omega}{10\Omega + 10\Omega} = 6\text{V}$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

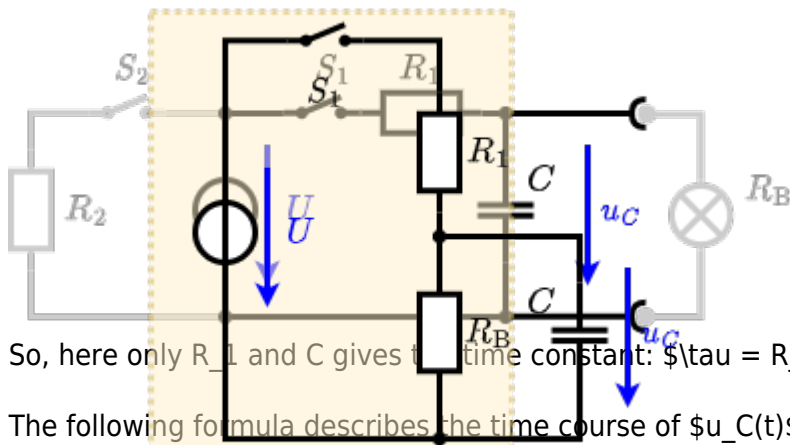


The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$

$$e^{-t/\tau} = 0.5 \quad t/\tau = \ln(0.5) \quad t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$
 An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V DC voltage source, a switch S_1 and a switch S_2 in series with a $20\text{ }\Omega$ resistor, a $100\text{ }\mu\text{F}$ capacitor, and a $10\text{ }\Omega$ resistor. At the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

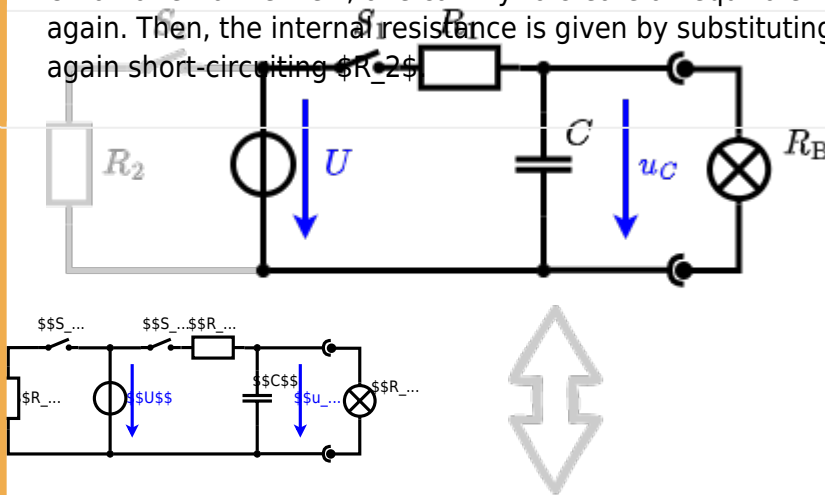
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

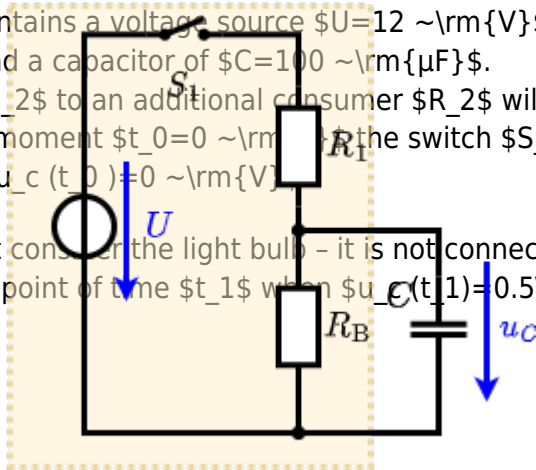


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$

It has to be rearranged to t :

$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$

Exercise E1 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (R and X_L) shall be given.

After analysis, the full bridge dimensioned impedance can be extracted and the phase angle in phase with the voltage $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components.

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.42 \angle 87.96^\circ$ A

The current and voltage are in phase with the voltage $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components.

Therefore, the component 0.24Ω is a resistor with the same absolute value of 0.24Ω impedance. $\underline{X}_L = -j4.68 \Omega$ is an inductor with the same absolute value of 4.68Ω impedance. $\underline{X}_L = -j4.68 \Omega$ is an inductor with the same absolute value of 4.68Ω impedance.

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.96^\circ$

With the complex part $0.24 - j4.68$ in both the components, $\underline{I} = 10.42 \angle 87.96^\circ$ A

$\underline{I} = 10.42 \angle 87.96^\circ$ A

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.96^\circ$

Exercise E6 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (R and X_L) shall be given.

After analysis, the full bridge dimensioned impedance can be extracted and the phase angle in phase with the voltage $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components.

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.42 \angle 87.96^\circ$ A

The current and voltage are in phase with the voltage $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components.

Therefore, the component 0.24Ω is a resistor with the same absolute value of 0.24Ω impedance. $\underline{X}_L = -j4.68 \Omega$ is an inductor with the same absolute value of 4.68Ω impedance.

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{I})}{\text{Re}(\underline{I})}\right) = \arctan\left(\frac{-4.68}{0.24}\right) = -87.96^\circ$

$$\begin{aligned} \text{The phase } \phi &= \arctan\left(\frac{-4.68 \sim \Omega}{0.24 \sim \Omega}\right) \\ \phi &= \arctan\left(\frac{-4.68 \sim \Omega}{0.24 \sim \Omega}\right) \end{aligned}$$

Exercise E1 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)

2. A capacitor \$C_1\$ shall have the same absolute value of the impedance as a capacitor \$C_2=40 \sim \{\rm nF\}\$ at \$f_1=4 \sim \{\rm MHz\}\$.

Solution

Solution $R_1 = 1.00 \sim \Omega$

$$\text{solution} \begin{array}{l} R_2 \approx 10.0 \sim \Omega \end{array}$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $\begin{aligned} & \end{aligned}$

Parallel circuit means that the voltage is the same on \$B-B_3\$ and \$C-C_3\$.

$$\{ \sqrt{m} \sin(\theta) \}^2 + \{ \sqrt{m} \cos(\theta) \}^2 = m$$

Therefore, the resulting current of the parallel circuit is given as: \begin{align*}

$$\underline{\{3\}} = \underline{\{3R\}} + \underline{\{3C\}}$$

[illegible]

$$\left. \right)^2 - (2\pi \cdot 450 \sim \{\text{rm kHz}\} \cdot 4.7 \sim \{\text{rm }\mu\text{H}\})^2 \} \quad \end{align*}$$

Back to the first formula:
$$R_3 \cdot I_{3R} = X_{3C} \cdot$$

$$\{I\} \setminus \{C\} \cap R \neq \{X\} \setminus \{C\} \cdot \frac{\{\{I\} \setminus \{C\}\}}{\{\{I\} \setminus \{R\}\}} \cap \{C\}$$

$$\left\{ \frac{1}{2\pi} \int_{\mathbb{C}} f \cdot C_3 \right\} \cdot \left\{ \left| \sqrt{|I|} \right| C_3 \right|^2 -$$

$$\frac{\{I\} \{3R\}^2}{\{I\} \{3R\}} \quad \text{\textbackslash\textbackslash end\{align*\}}$$

Exercise E7 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)

Exercise E1 Complex Impedance Circuit
(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the AC network diagram of Fig. 1. The AC voltage source $u(t) = 3.0 \sin(2\pi \cdot 15 \text{ kHz} \cdot t) \text{ V}$ is connected in series with an inductor of $L = 330 \text{ } \mu\text{H}$ and a capacitor of $C = 0.22 \text{ } \mu\text{F}$. All components, voltages, and currents are given in the diagram.

Solution:
Result:
$$Z = 19.8 \text{ } \Omega$$

Draw the circuit diagram of the given circuit. Label all components, voltages, and currents.

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by
$$Z_L = j\omega L = j2\pi \cdot 15 \text{ kHz} \cdot 330 \text{ } \mu\text{H} = j3.16 \text{ } \Omega$$

Parallel circuit means that the voltage is the same on R_1 and R_2
$$\frac{1}{Z} = \frac{1}{R_1} + \frac{1}{R_2}$$

Since R_1 and R_2 are in parallel, the voltage across them is the same. The current through them is the same. The resulting current of the parallel circuit is given as:
$$I = I_1 + I_2$$

This can be simplified to:
$$I = I_1 + I_2 = \frac{U}{R_1} + \frac{U}{R_2} = U \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

Back to the first formula:
$$Z \cdot I = R_1 \cdot I_1 + R_2 \cdot I_2 = R_1 \cdot \frac{U}{R_1} + R_2 \cdot \frac{U}{R_2} = U + U = 2U$$

Therefore:
$$Z = \frac{2U}{I} = \frac{2 \cdot 3.0 \text{ V}}{0.3 \text{ A}} = 20 \text{ } \Omega$$

Exercise E1 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the AC network diagram of Fig. 1. The AC voltage source $u(t) = 3.0 \sin(2\pi \cdot 15 \text{ kHz} \cdot t) \text{ V}$ is connected in series with an inductor of $L = 330 \text{ } \mu\text{H}$ and a capacitor of $C = 0.22 \text{ } \mu\text{F}$. All components, voltages, and currents are given in the diagram.

Solution:
Result:
$$Z = 19.8 \text{ } \Omega$$

Draw the circuit diagram of the given circuit. Label all components, voltages, and currents.

$$Z = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} = \frac{1}{\frac{1}{10 \text{ } \Omega} + \frac{1}{20 \text{ } \Omega}} = 6.67 \text{ } \Omega$$

$$Z_L = j\omega L = j2\pi \cdot 15 \text{ kHz} \cdot 330 \text{ } \mu\text{H} = j3.16 \text{ } \Omega$$

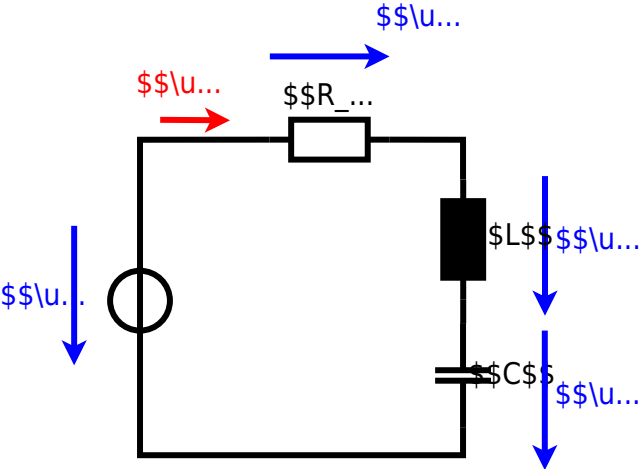
$$Z_C = \frac{1}{j\omega C} = \frac{1}{j2\pi \cdot 15 \text{ kHz} \cdot 0.22 \text{ } \mu\text{F}} = -j1.59 \text{ } \Omega$$

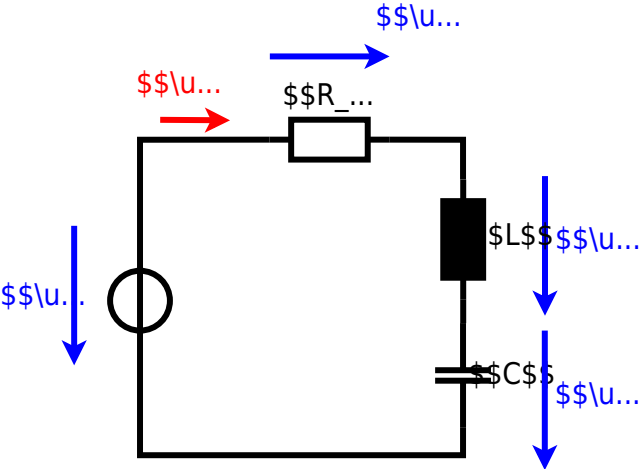
With $Z = 6.67 \text{ } \Omega$, $Z_L = j3.16 \text{ } \Omega$, and $Z_C = -j1.59 \text{ } \Omega$:
$$Z = Z_L + Z_C + Z = j3.16 \text{ } \Omega - j1.59 \text{ } \Omega + 6.67 \text{ } \Omega = 6.67 \text{ } \Omega + j1.57 \text{ } \Omega$$

$$|Z| = \sqrt{6.67^2 + 1.57^2} = 6.85 \text{ } \Omega$$

$$\angle Z = \arctan\left(\frac{1.57}{6.67}\right) = 13.4^\circ$$







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