

Exam Winter Semester 2022

Student Group

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Table of Contents

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E1 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)	4
Exercise E1 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)	5
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)	6
Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)	8
Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)	12
Exercise E1 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)	16
Exercise E5 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)	17
Exercise E1 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)	19
Exercise E6 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)	19
Exercise E1 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)	20
Exercise E7 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)	20
Exercise E1 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written	

test, WS2022)	21
Exercise E8 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written	
test, WS2022)	24

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

A heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 is used. Electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Determine the current I linked to the power supply for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \text{and } R = \\ 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

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Solution

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Exercise E1 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A digital display shows a temperature coefficient of resistance of a thermistor. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$

The power transfer resistor P is the output of the circuit and generates heat. Therefore, a solution is to use a heat sink to cool the heat up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right)$$

Exercise E2 Temperature-dependent Resistance**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. A digital display shows a temperature coefficient of resistance of a thermistor. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$

The power transfer resistor P is the output of the circuit and generates heat. Therefore, a solution is to use a heat sink to cool the heat up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right)$$

Exercise E1 Pure Resistor Network Simplification

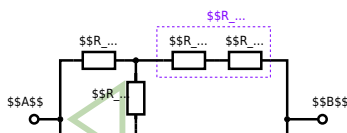
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be closed and integrated, $R_2 = R_3 = 100 \Omega$ and the switch between R_1 and R_2 shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{\text{eq}} = 133.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

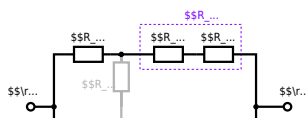
$$R_Y = \frac{R_2 \cdot R_3}{R_2 + R_3} = \frac{100 \cdot 100}{100 + 100} = 50 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) = 50 + (50 + 100 + 100) \parallel (50 + 100)$$

.. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{eq} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega}$$

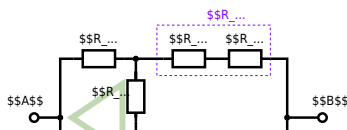
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved with $R_1 = 200 \, \Omega$, $R_2 = 100 \, \Omega$, $R_3 = 150 \, \Omega$, $R_4 = 100 \, \Omega$, and the voltage $U_{SV} = 10 \, V$.
Result given: $R_{eq} = 132.8 \, \Omega$.

Solution

$$R_{eq} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.



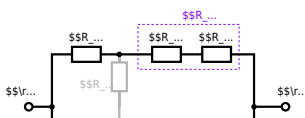
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega) \parallel$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



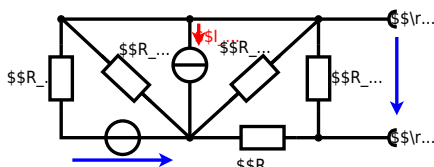
The equivalent resistor is given by a parallel configuration of resistors in series:

$$\begin{aligned} R_{\text{eq}} &= (R_2 + R_1 + R_3) \parallel (R_4 + R_5) \\ R_{\text{eq}} &= (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \\ R_{\text{eq}} &= (500 \, \Omega) \parallel (200 \, \Omega) \\ R_{\text{eq}} &= \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \end{aligned}$$

Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

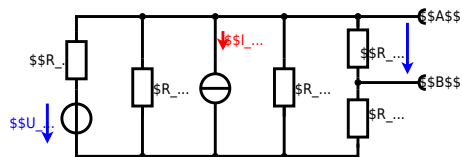
$$\begin{aligned} U_s &= U_{\text{AB}} = 4.5 \, \text{V} \\ R_i &= R_{\text{AB}} = 6 \, \Omega \end{aligned}$$



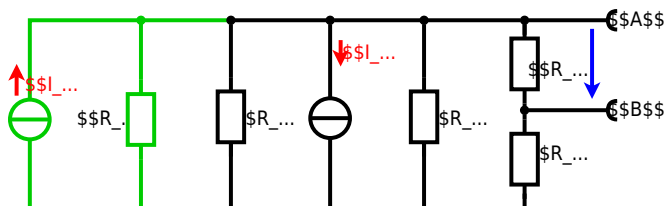
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $R_1=5.0 \, \Omega$, $U_2=6.0 \, \text{V}$, $R_3=10 \, \Omega$, $I_4=4.2 \, \text{A}$, $R_5=10 \, \Omega$, $R_6=7.5 \, \Omega$, $R_7=15 \, \Omega$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_{23} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \quad R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

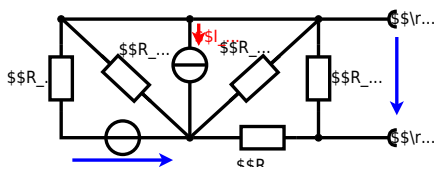
Exercise E4 Equivalent linear Source

(written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.

Result

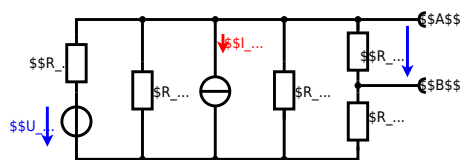
$$U_s = U_{AB} = 4.5\text{V} \quad R_i = R_{AB} = 6\Omega$$



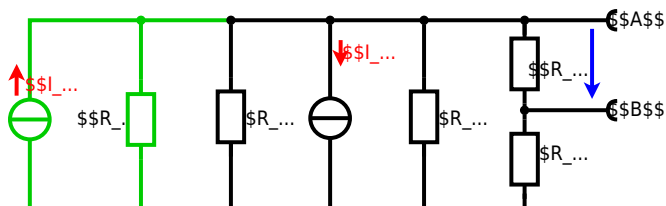
Calculate the internal resistance R_{int} and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24}$$

$$I_{24} = \frac{U_{24}}{R_1 + R_3 + R_5} = \frac{(U_1 - U_4) \cdot R_1}{R_1 + R_3 + R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 + R_3 + R_5} = (U_1 - U_4) \cdot \frac{R_7 \cdot R_1}{R_6 + R_7 + R_1 + R_3 + R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 + R_3 + R_5)$$

with $R_1 + R_3 + R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} \cdot 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \parallel R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E1 Charging Capacitors

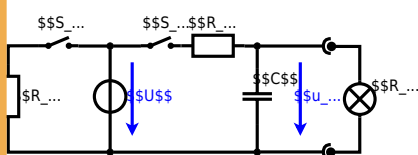
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit below is a simplified model of a battery with an internal resistance R_1 and a capacitor C connected in parallel. The voltage across the capacitor is again U_0 at the moment $t_0=0$ s when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1$ ms after closing the switch.

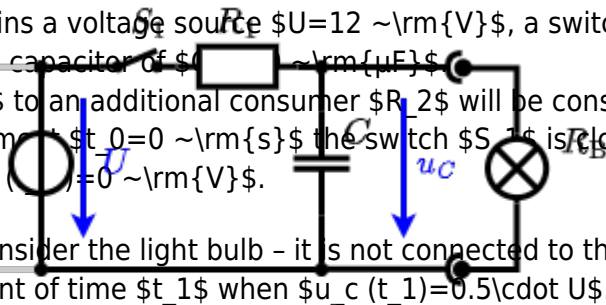
Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

Solution: The equivalent circuit is shown below. The ideal voltage source U_{eq} is given by $U_{eq} = \frac{U \cdot R_2}{R_1 + R_2}$ and the internal resistance $R_{eq} = R_1 \parallel R_2$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

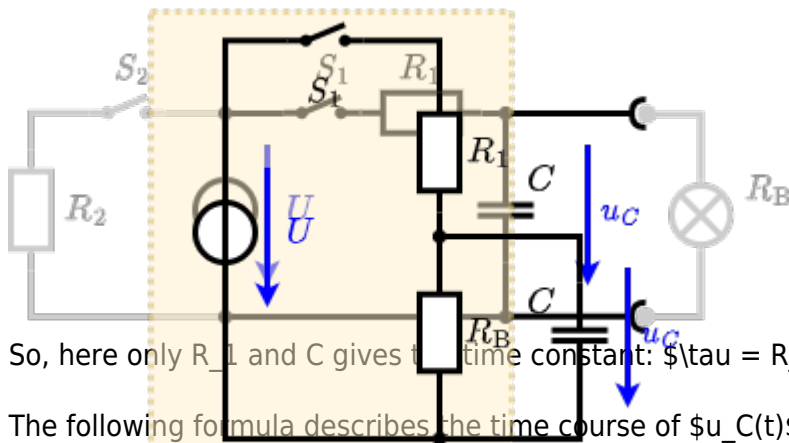


The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$. An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V voltage source, a $20\text{ }\Omega$ resistor, a $100\text{ }\mu\text{F}$ capacitor, a switch S_1 and a switch S_2 . The voltage across the capacitor is again 0 V at the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

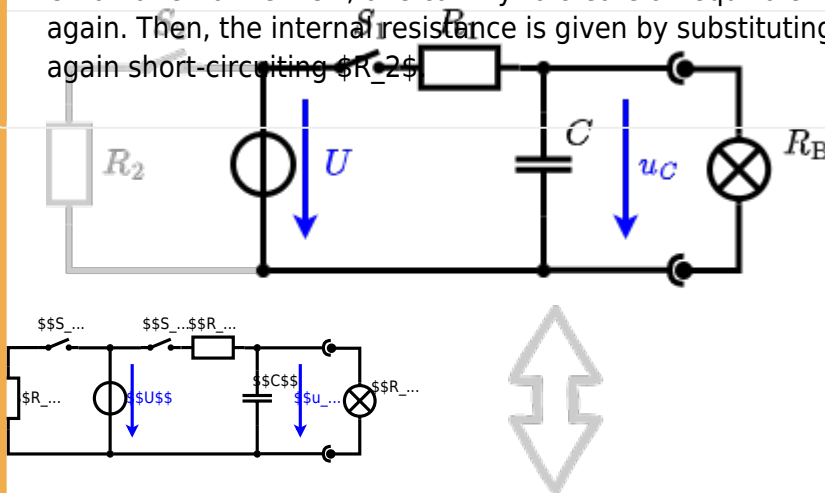
Solution

To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

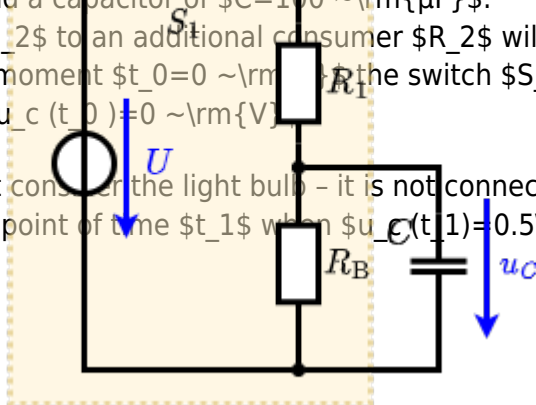


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$

It has to be rearranged to t :

$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$

Exercise E1 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ V and $\underline{Z} = 0.24 + j4.68 \Omega$ in both the components. ($\$R\$$ and $\underline{X}_L$) shall be given.

After analysis, the full bridge dimensioned circuit impedance can be extracted and the phase angle φ in phase (calculated) is $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 + j4.68} = 10.42 \angle -87.06^\circ$ A

The current and voltage are in phase since the impedance is purely real (resistive) and the voltage is the reference. The resulting impedance is $\underline{Z} = 0.24 + j4.68 \Omega$.

Therefore, the component 0.24Ω is a resistor with the same absolute value of 0.24Ω and the component $j4.68 \Omega$ is an inductor with the same absolute value of 4.68Ω .

Impedance $\underline{Z} = R + jX_L = 0.24 + j4.68 \Omega$

Phase angle $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

The phase angle φ is calculated as $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

With the complex part (complex value) $\underline{Z} = 0.24 + j4.68 \Omega$ and $\underline{U} = 50 \angle 0^\circ$ V

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 + j4.68} = 10.42 \angle -87.06^\circ$ A

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

Exercise E6 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ V and $\underline{Z} = 0.24 + j4.68 \Omega$ in both the components. ($\$R\$$ and $\underline{X}_L$) shall be given.

After analysis, the full bridge dimensioned circuit impedance can be extracted and the phase angle φ in phase (calculated) is $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 + j4.68} = 10.42 \angle -87.06^\circ$ A

The current and voltage are in phase since the impedance is purely real (resistive) and the voltage is the reference. The resulting impedance is $\underline{Z} = 0.24 + j4.68 \Omega$.

Therefore, the component 0.24Ω is a resistor with the same absolute value of 0.24Ω and the component $j4.68 \Omega$ is an inductor with the same absolute value of 4.68Ω .

Impedance $\underline{Z} = R + jX_L = 0.24 + j4.68 \Omega$

Phase angle $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

The phase angle φ is calculated as $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

$$\begin{aligned} X_L &= \frac{1}{\sqrt{(0.24 \sim \Omega)^2 + (4.68 \sim \Omega)^2}} \\ \phi &= \arctan \left(\frac{-4.68 \sim \Omega}{0.24 \sim \Omega} \right) \end{aligned}$$

Exercise E1 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)

2. A capacitor \$C_1\$ shall have the same absolute value of the impedance as a capacitor \$C_2=40 \sim \{\rm nF\}\$ at \$f_1=4 \sim \{\rm MHz\}\$.

Solution

$$\text{Solution} \quad R_1 = 1.00 \sim \Omega$$

$$\text{solution} \begin{array}{l} \begin{array}{l} \text{begin}\{align*\} \\ R \geq 10.0 \end{array} \end{array} \quad \Omega$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $\begin{aligned} & \end{aligned}$

Parallel circuit means that the voltage is the same on \$B-P\$ and \$C-Q\$ \$\therefore R_2 + R_3 = R_2 + R_3\$

\$\{ \sqrt{L_2^2 + X^2} \}^2\$ can be simplified to: $\text{begin}\{\text{align} \; \text{left} \}$
 $\{\sqrt{L_2^2 + X^2}\}^2 \text{ is perpendicular to } \underline{\text{line}}\{\text{R}_1\text{C}\}$ (It has to, since R_3
 is perpendicular to $\{\sqrt{L_2^2 + X^2}\}$ and $\{\text{R}_1\text{C}\}$ is $\text{right}^2 = \{\text{R}_2\}^2 + \{\text{X}\{L_2\}\}^2$

Therefore, the resulting current of the parallel circuit is given as: \begin{align*}

$$\underline{\{3\}} = \underline{\{3R\}} + \underline{\{3C\}} \quad \parallel$$

[illegible]

$$\left. \right)^2 - (2\pi \cdot 450 \sim \{\text{rm kHz}\} \cdot 4.7 \sim \{\text{rm }\mu\text{H}\})^2 \} \quad \end{align*}$$

Back to the first formula:
$$R \cdot 3 \cdot I \cdot 3R = X \cdot 3C \cdot$$

$$\{I\} \setminus \{3C\} \parallel R \text{ } 3 \&= \{X\} \setminus \{3C\} \cdot \frac{\{I\} \setminus \{3C\}}{\{I\} \setminus \{3R\}} \parallel \&=$$

$$\{ \{1\} \over {2\pi} \cdot f \cdot C \} \cdot \{ \sqrt{|I|} \cdot \{3\} \}^2 \cdot$$

$$\frac{|I| \{3R\}^2}{|I| \{3R\}} \quad \end{align*}$$

Exercise E7 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)

Replaces the resistor value of $20 \pm 3\%$ with a 100 nF capacitor in the AC coupling circuit of SS1. $2 \pm 0.05 \text{ B.O.}$ $\sim \text{m A}$, $\text{fitB} = 200 \sim 450 \text{ kHz}$, Hz high-gain test current $\text{fitB} = 50 \text{ (3R)} \sim 1 \text{ A}$ $\sim \text{m A}$ through pA .

A resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

$$\begin{aligned} \text{solution} \quad \begin{aligned} \text{begin}\{align*\} \quad R_1 &= 1.00 \sim \Omega \end{aligned} \\ \text{solution} \quad \begin{aligned} \text{begin}\{align*\} \quad R_2 &= 10.0 \sim \Omega \end{aligned} \\ \text{solution} \end{aligned}$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R_S and L_S combined is given by $\begin{aligned} \text{Parallel circuit means that the voltage is the same on } R_S \text{ and } L_S \\ \text{Since } \underline{I}_S \text{ is perpendicular to } \underline{I}_L \text{, the resulting current } \underline{I}_S \text{ is perpendicular to } \underline{I}_L \text{, thus can be simplified to } \underline{I}_S \text{ gets clean and } \\ \text{is perpendicular to } \underline{I}_L \text{ (It has to, since } R_S \text{ is perpendicular to } \underline{I}_L \text{ and } L_S \text{ is perpendicular to } \underline{I}_L \text{, too)} \\ \text{Therefore, the resulting current of the parallel circuit is given as:} \\ \underline{I}_S = \underline{I}_R + \underline{I}_L \\ \text{This can be rearranged to give } \underline{I}_S = \underline{I}_R \sqrt{1 + \left(\frac{\omega L_S}{R_S} \right)^2} \\ \text{Back to the first formula: } R_S \cdot \underline{I}_S = X_{L_S} \cdot \underline{I}_S \\ \underline{I}_S = \frac{X_{L_S}}{R_S} \cdot \underline{I}_S = \frac{\omega L_S}{R_S} \cdot \underline{I}_S \\ \text{Back to the first formula: } R_S \cdot \underline{I}_S = X_{L_S} \cdot \underline{I}_S \\ \underline{I}_S = \frac{X_{L_S}}{R_S} \cdot \underline{I}_S = \frac{\omega L_S}{R_S} \cdot \underline{I}_S \end{aligned}$

Exercise E1 Complex Impedance Circuit

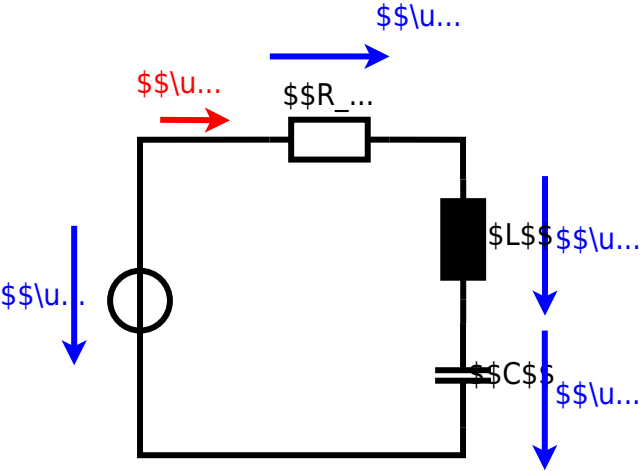
(written test, approx. 15 % of a 60-minute written test, WS2022)

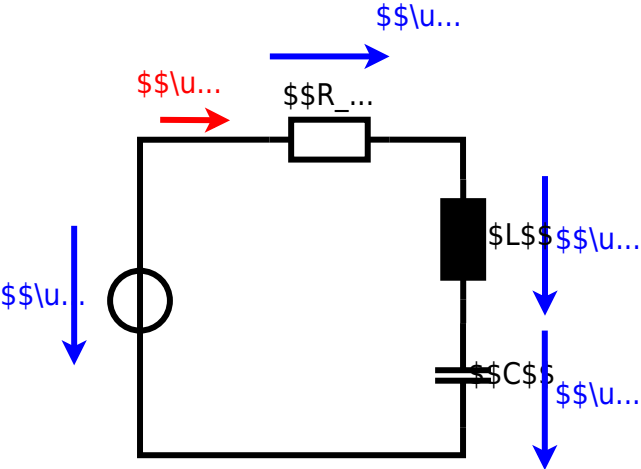
[illegible]

Solution
This linear source is connected with an inductor of $330 \sim \{\rm \mu H\}$ and a capacitor of $0.22 \sim \{\rm \mu F\}$, all in series.

$$\begin{aligned} Z &= 107.3 \, \Omega \parallel (48.2 \, \Omega + j19.8 \, \Omega) \\ Z &= 84.5 \, \Omega - j37.5 \, \Omega \end{aligned}$$
[illegible]







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