

Exam Winter Semester 2022

Student Group

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Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

2. For heating elements made of Nichrome wire with a diameter of $d = 1.80 \text{ mm}$, an electric power dissipation (= heat flow) of $P = 40 \text{ W}$ is necessary.

Determine the current I needed for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \cdot \text{m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ I &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \text{ with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad | \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \cdot \text{m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

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Exercise E1 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. Additionally, explain why the effect of constant temperature inside the refrigeration system can be identified. Result: The resistance of the thermistor is $R = 10 \cdot 10^3 \Omega$ at $T = 25^\circ\text{C}$ for your answer.

Its temperature coefficients are: $\alpha = 0.01 \cdot 10^{-6} \cdot 10^3 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \cdot 10^3 \text{ K}^{-2}$

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

The resistance of the thermistor is $R = 10 \cdot 10^3 \Omega$ at $T = 25^\circ\text{C}$. Therefore, a solution is to use a float up the refrigeration system. Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \cdot 10^3 \Omega \cdot \left(1 + 0.01 \cdot 10^{-6} \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2 \right)$$

Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)

2. Additionally, explain why the effect of constant temperature inside the refrigeration system can be identified. Result: The resistance of the thermistor is $R = 10 \cdot 10^3 \Omega$ at $T = 25^\circ\text{C}$ for your answer.

Its temperature coefficients are: $\alpha = 0.01 \cdot 10^{-6} \cdot 10^3 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \cdot 10^3 \text{ K}^{-2}$

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

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$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \cdot 10^3 \Omega \cdot \left(1 + 0.01 \cdot 10^{-6} \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2 \right)$$

Exercise E1 Pure Resistor Network Simplification

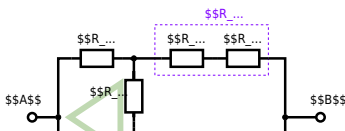
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be closed and integrated, $R_2 = R_3 = 100 \Omega$ and the switch between R_1 and R_2 shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{\text{eq}} = 133.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

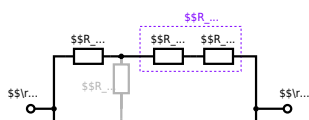
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega) \parallel (500 \, \Omega \cdot 200 \, \Omega) / (500 \, \Omega + 200 \, \Omega)$$

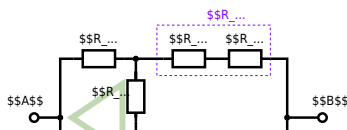
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved with $R_1 = 200 \, \Omega$, $R_2 = 100 \, \Omega$, $R_3 = 150 \, \Omega$, $R_4 = 100 \, \Omega$, and the voltage $U_{SV} = 10 \, V$.
Result given: $R_{eq} = 132.8 \, \Omega$.

Solution

$$R_{eq} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.



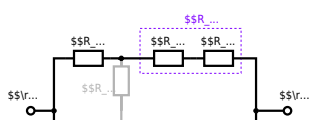
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



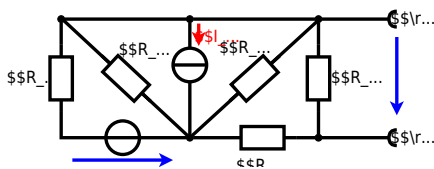
The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel R_{\text{eq}} = (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \parallel R_{\text{eq}}$$

Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

$$U_{\text{s}} = U_{\text{AB}} = 4.5 \, \text{V} \parallel R_{\text{i}} = R_{\text{AB}} = 6 \, \Omega$$



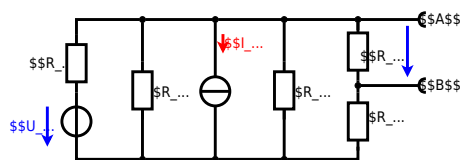
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B.

$R_1 = 5.0 \, \Omega$, $U_2 = 6.0 \, \text{V}$, $R_3 = 10 \, \Omega$, $I_4 = 4.2 \, \text{A}$, $R_5 = 10 \, \Omega$, $R_6 = 7.5 \, \Omega$, $R_7 = 15 \, \Omega$

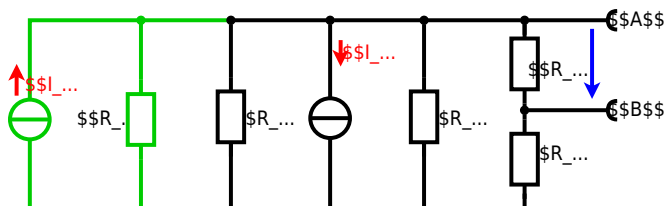
Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_{23} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_2 - U_4) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

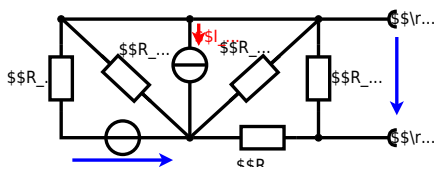
with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \parallel R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

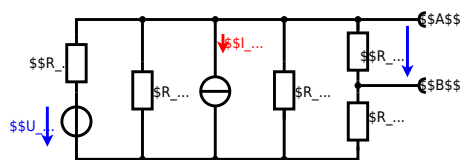
$$U_s = U_{AB} = 4.5\text{V} \parallel R_i = R_{AB} = 6\Omega$$



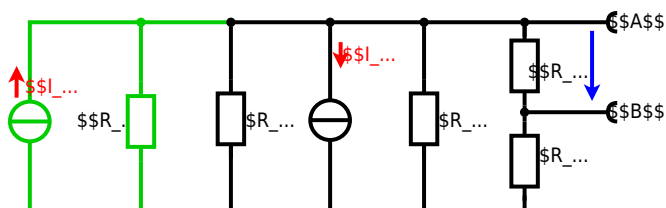
Calculate the internal resistance R_{int} and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$\&= R_{135} \cdot I_{24} \quad \&= \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:
$$U_{\rm AB}$$

$$\begin{aligned} &= U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \parallel &= \\ &(\frac{U_2}{R_1}) - I_4 \cdot \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5} \parallel \end{aligned}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($\mathcal{E}=0\Omega$, so a short-circuit):

$$R_{\text{AB}} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 || R_3 || R_5 = 5 \sim \Omega || 10 \sim \Omega || 10 \sim \Omega = 5 \sim \Omega || 5 \sim \Omega = 2.5 \sim \Omega$:

$$\begin{aligned} U_{\rm AB} &= \left(\frac{6.0 \, \rm V}{5.0 \, \Omega} - 4.2 \, \Omega \right) \\ &\cdot \left(\frac{15 \, \Omega \cdot 2.5 \, \Omega}{7.5 \, \Omega + 15 \, \Omega + 2.5 \, \Omega} \right) \\ R_{\rm AB} &= 15 \, \Omega \parallel (7.5 \, \Omega + 2.5 \, \Omega) \end{aligned}$$

Exercise E1 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit will be in the following states: (a) At $t_0 = 0$ s, the switch S_1 is opened. Regularly, $U_c(t_0) = 5$ V. (b) At $t_1 = 2$ ms, the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1$ ms after closing the switch.

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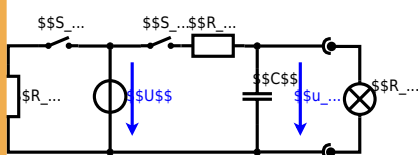
% To solve this, first create an equivalent linear voltage source from $U$, $R_1$, and
% $R_2$.
\begin{align*} U_{\text{eq}} &= \frac{U}{1 + \frac{R_1}{R_2}} \\ R_{\text{eq}} &= \frac{R_1 R_2}{R_1 + R_2} \end{align*}

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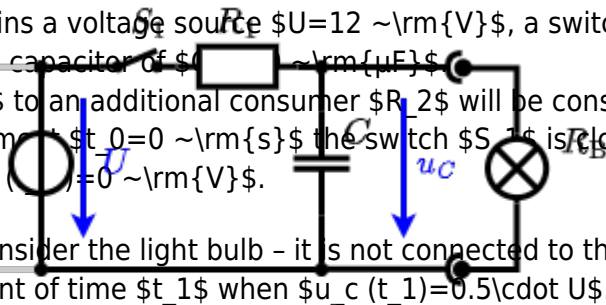
$$\Delta I_{B(2)} = \frac{I_{B(2)}}{\beta} \approx \frac{I_{C(2)}}{\beta}$$

$$V_{\text{th}} = \frac{V_{\text{oc}}}{1 + \frac{R_{\text{oc}}}{R_{\text{L}}}}$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_{25} .

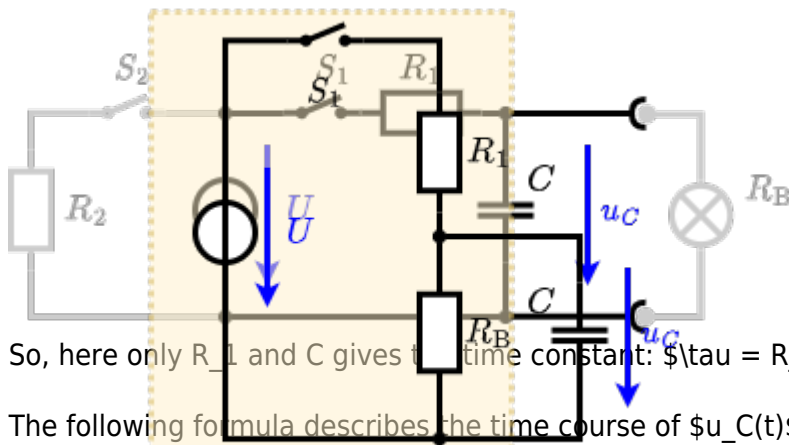


The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$

$$e^{-t/\tau} = 0.5 \quad t/\tau = \ln(0.5) \quad t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$
 An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V DC voltage source U , a switch S_1 , a resistor $R_1=20\text{ }\Omega$, a capacitor $C=100\text{ }\mu\text{F}$, and a light bulb $R_B=20\text{ }\Omega$. The voltage across the capacitor is again 0 V at the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution

To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

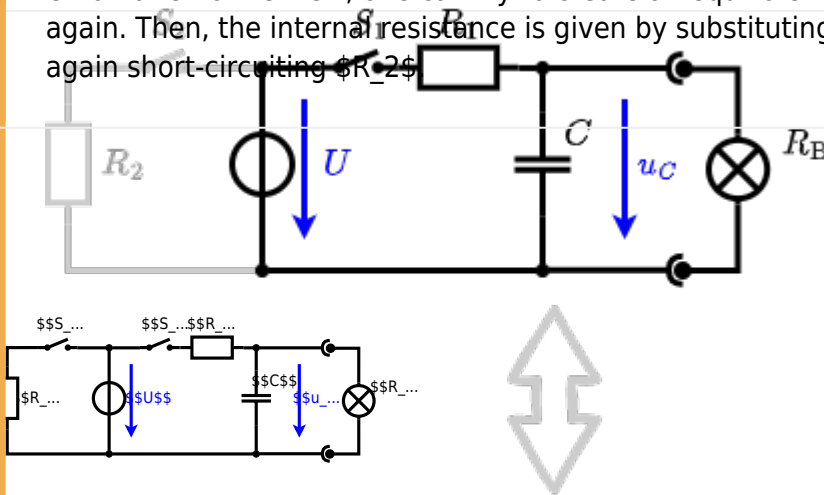
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

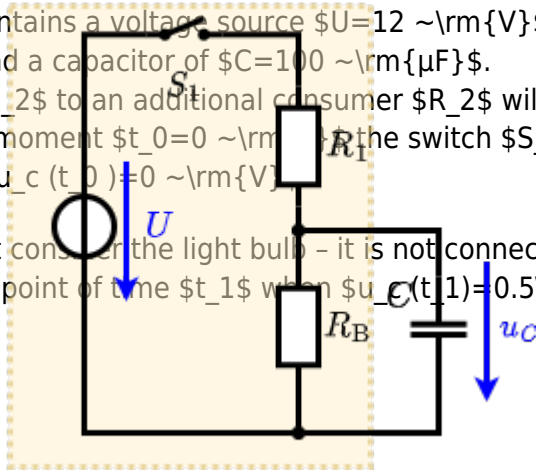


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$U_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$: $u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$. It has to be rearranged to t : $(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$

Exercise E1 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the complex power $\underline{S}$ (W and VA) of the load $\underline{Z}$ through the components ($\$R\$$ and $\$X_L\$$) shall be given.

After analysis, the full bidimensional complex power $\underline{S}$ shall be extracted and φ (deg) in phase (calculated) shall be given.

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.12 \Omega \quad \varphi = 2.26^\circ \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50}{0.24 + j4.68} = 10.67 - j2.26 \text{ A}$

The current and voltage across phase are only across the real resulting impedance 0.24Ω in parallel with $j4.68 \Omega$.

Therefore, the component 0.24Ω is in parallel with the same voltage 4.68 V in parallel with $j4.68 \Omega$ in series with 0.24Ω .

$\underline{S} = \underline{U} \cdot \underline{I}^* = (50 \angle 0^\circ) \cdot (10.67 - j2.26)^* = 530 - j113 \text{ VA}$

$\varphi = \arctan\left(\frac{\text{Im}(\underline{S})}{\text{Re}(\underline{S})}\right) = \arctan\left(\frac{-113}{530}\right) = -12.1^\circ$

With the complex part $\varphi = -12.1^\circ$ is the phase angle of $\underline{S}$.

The phase φ can be calculated as $\varphi = \arctan\left(\frac{\text{Im}(\underline{S})}{\text{Re}(\underline{S})}\right) = \arctan\left(\frac{-113}{530}\right) = -12.1^\circ$

Exercise E6 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the complex power $\underline{S}$ (W and VA) of the load $\underline{Z}$ through the components ($\$R\$$ and $\$X_L\$$) shall be given.

After analysis, the full bidimensional complex power $\underline{S}$ shall be extracted and φ (deg) in phase (calculated) shall be given.

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.12 \Omega \quad \varphi = 2.26^\circ \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50}{0.24 + j4.68} = 10.67 - j2.26 \text{ A}$

The current and voltage across phase are only across the real resulting impedance 0.24Ω in parallel with $j4.68 \Omega$.

Therefore, the component 0.24Ω is in parallel with the same voltage 4.68 V in parallel with $j4.68 \Omega$ in series with 0.24Ω .

$\underline{S} = \underline{U} \cdot \underline{I}^* = (50 \angle 0^\circ) \cdot (10.67 - j2.26)^* = 530 - j113 \text{ VA}$

$\varphi = \arctan\left(\frac{\text{Im}(\underline{S})}{\text{Re}(\underline{S})}\right) = \arctan\left(\frac{-113}{530}\right) = -12.1^\circ$

The absolute value of the impedance is $\sqrt{(0.24 \sim \Omega)^2 + (4.68 \sim \Omega)^2} = 4.7 \sim \Omega$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.
 With the complex part comes the physical value: $X_L = \omega L = 2\pi \cdot 4.7 \sim \Omega$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.

Exercise E1 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.
 The equivalent impedance for R and C combined is given by $Z = \sqrt{R^2 + X_C^2}$.
 The equivalent impedance for R , L and C combined is given by $Z = \sqrt{R^2 + (X_L - X_C)^2}$.
 The equivalent impedance for R , L and C combined is given by $Z = \sqrt{R^2 + (X_L - X_C)^2}$.

Solution

$R_1 = 1.00 \sim \Omega$

$R_2 = 10.0 \sim \Omega$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.

Parallel circuit means that the voltage is the same on R_1 and R_2 .
 $\frac{1}{Z} = \frac{1}{R_1} + \frac{1}{R_2}$ since $\frac{1}{Z} = \frac{1}{R_1} + \frac{1}{R_2}$ is perpendicular to R_2 this can be simplified to $\frac{1}{Z} = \frac{1}{R_1} + \frac{1}{R_2}$.

$\frac{1}{Z} = \frac{1}{R_1} + \frac{1}{R_2}$ is perpendicular to R_1 (It has to, since R_1 is perpendicular to R_2).

Therefore the resulting current of the parallel circuit is given as:

$\frac{1}{Z} = \frac{1}{R_1} + \frac{1}{R_2}$

This can be rearranged to $Z = \frac{R_1 R_2}{R_1 + R_2}$.

$Z = \frac{1 \cdot 10}{1 + 10} = 0.91 \sim \Omega$

Back to the first formula: $R_3 \cdot \frac{1}{Z} = X_L \cdot \frac{1}{Z}$

$R_3 = X_L \cdot \frac{Z}{1}$

$R_3 = \sqrt{R_1^2 + R_2^2} \cdot \frac{Z}{1}$

$R_3 = \sqrt{1^2 + 10^2} \cdot 0.91 = 9.1 \sim \Omega$

Exercise E7 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

Exercise E1 Complex Impedance Circuit
(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the following diagram (of 3S) 21.B.0
 $\sim \sqrt{2} \cdot 10 \text{ V} \cdot \sin(2\pi \cdot 15 \text{ kHz} \cdot t)$ is the voltage source. $R_1 = 10 \Omega$, $R_2 = 10 \Omega$, $R_3 = 10 \Omega$, $L = 1 \text{ mH}$, $C = 10 \text{ nF}$.
 The resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution:

$$R_1 = 10 \Omega$$

Solution:

$$R_2 = 10 \Omega$$

Solution

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by

Parallel circuit means that the voltage is the same on R_1 and R_2 .

$$\underline{R}_{\text{parallel}} = \frac{R_1 \cdot R_2}{R_1 + R_2} = \frac{10 \Omega \cdot 10 \Omega}{10 \Omega + 10 \Omega} = 5 \Omega$$

Since $\underline{U}_R$ and $\underline{U}_L$ are perpendicular to each other, the resulting current of the parallel circuit is given as:

Therefore, the resulting current of the parallel circuit is given as:

$$\underline{I}_{\text{parallel}} = \sqrt{\underline{I}_R^2 + \underline{I}_L^2} = \sqrt{\left(\frac{\underline{U}}{R_1}\right)^2 + \left(\frac{\underline{U}}{X_L}\right)^2} = \frac{\underline{U}}{R_1} \sqrt{1 + \left(\frac{X_L}{R_1}\right)^2}$$

Back to the first formula:
$$\underline{I}_{\text{parallel}} = \frac{\underline{U}}{Z_{\text{parallel}}} \Rightarrow Z_{\text{parallel}} = \frac{\underline{U}}{\underline{I}_{\text{parallel}}} = \frac{R_1}{\sqrt{1 + \left(\frac{X_L}{R_1}\right)^2}}$$

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Exercise E1 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

1. Calculate the equivalent impedance Z for the circuit shown in the following diagram (of 3S) 21.B.0
 $\sim \sqrt{2} \cdot 10 \text{ V} \cdot \sin(2\pi \cdot 15 \text{ kHz} \cdot t)$ is the voltage source. $R_1 = 10 \Omega$, $R_2 = 10 \Omega$, $R_3 = 10 \Omega$, $L = 1 \text{ mH}$, $C = 10 \text{ nF}$.
 The resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

Solution:
 This linear source is connected with an inductor of 330 nH and a capacitor of 0.22 nF , all in series.

Result

$$Z = 107.37 \Omega$$

Draw the circuit diagram of the given circuit.
 Label all components, voltages, and currents.

$$\underline{Z} = \frac{\underline{U}}{\underline{I}} = \frac{\sqrt{2} \cdot 10 \text{ V}}{\sqrt{2} \cdot 10 \text{ A}} = 1 \Omega$$

$$\underline{Z}_C = \frac{1}{j\omega C} = \frac{1}{j \cdot 2\pi \cdot 15 \text{ kHz} \cdot 0.22 \text{ nF}} = -j1.59 \Omega$$

Result:

$$\underline{Z} = 107.37 \Omega$$

With $\underline{Z} = 107.37 \Omega$ and $\underline{U} = \sqrt{2} \cdot 10 \text{ V}$, the current is:

$$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{\sqrt{2} \cdot 10 \text{ V}}{107.37 \Omega} = 0.14 \text{ A}$$

$$\underline{Z} = 107.37 \Omega$$

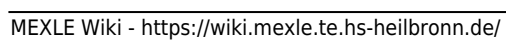
$$\underline{Z} = 107.37 \Omega$$

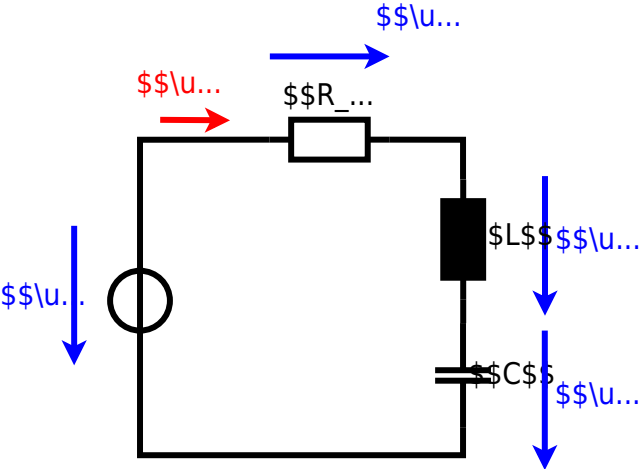
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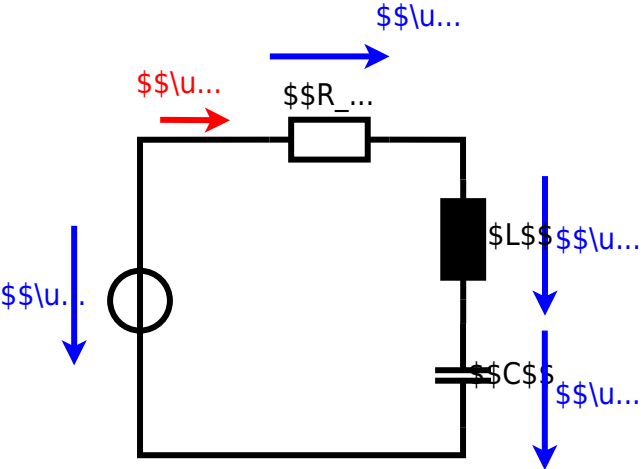
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