

Exam Summer Semester 2022

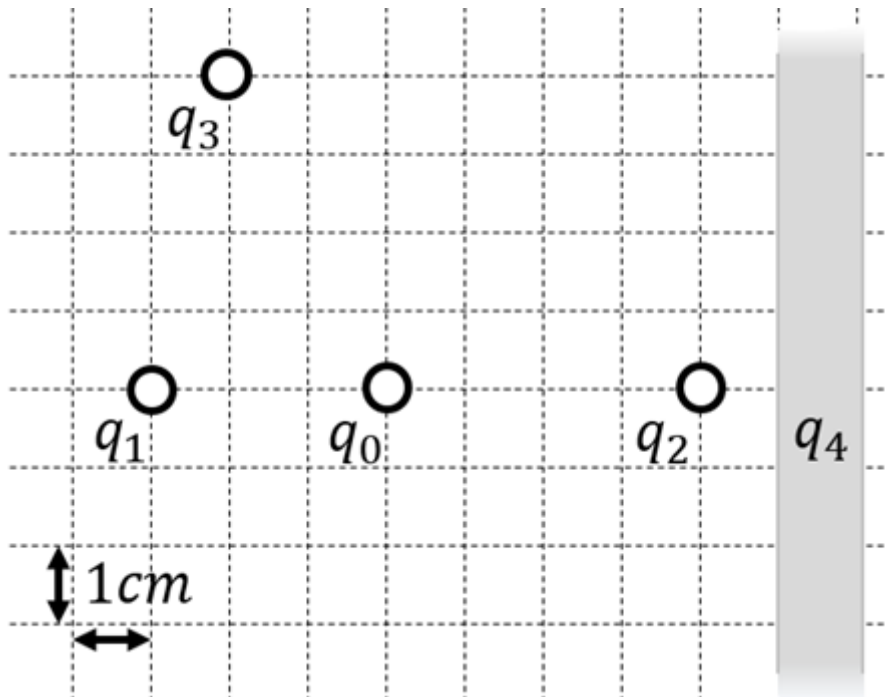
Student Group

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Table of Contents

Exam Summer Semester 2022	3
Additional permitted Aids	3
Hits	3
Tasks	3
Exercise E1 Electrostatics I (written test, approx. 10 % of a 120-minute written test, SS2022)	3
Exercise E2 Electrostatics I (written test, approx. 10 % of a 120-minute written test, SS2022)	5
Exercise E3 Electrostatics II (written test, approx. 10 % of a 120-minute written test, SS2022)	6
Exercise E4 Electrostatics II (written test, approx. 10 % of a 120-minute written test, SS2022)	7
Exercise E5 Electron Velocity in Semiconductors (written test, approx. 6 % of a 120-minute written test, SS2022)	8
Exercise E6 Electron Velocity in Semiconductors (written test, approx. 6 % of a 120-minute written test, SS2022)	8
Exercise E7 Capacitor (written test, approx. 7 % of a 120-minute written test, SS2022)	9
Exercise E8 Capacitor (written test, approx. 7 % of a 120-minute written test, SS2022)	10
Exercise E9 Magnetic Circuit (written test, approx. 7 % of a 120-minute written test, SS2022)	12
Exercise E10 Magnetic Circuit (written test, approx. 7 % of a 120-minute written test, SS2022)	13
Exercise E1 Self Induction (written test, approx. 8 % of a 120-minute written test, SS2022)	14
Exercise E11 Self Induction (written test, approx. 8 % of a 120-minute written test, SS2022)	15
Exercise E12 Series Resonant Circuit (written test, approx. 10 % of a 120-minute written test, SS2022)	16
Exercise E13 Series Resonant Circuit (written test, approx. 10 % of a 120-minute written test,	

SS2022) 18



1. Calculate the single forces $\vec{F}_{01}$, $\vec{F}_{02}$, $\vec{F}_{03}$, on the charge q_0 !

Path

First, calculate the magnitude of the forces, like $\vec{F}_{01}$.

The force $\vec{F}_{01}$ is purely on the x -axis and therefore equal to

$$\begin{aligned} F_{01,x} &= \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 \cdot q_0}{r_{01}^2} = \\ &= \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \text{ As/Vm}} \cdot \frac{1 \cdot 10^{-9} \text{ C} \cdot 2 \cdot 10^{-9} \text{ C}}{(3 \cdot 10^{-2} \text{ m})^2} = 19.97... \cdot 10^{-6} \text{ Nm} \\ &= 19.97... \cdot 10^{-6} \text{ Nm} \quad \text{(to the right)} \end{aligned}$$

Similarly, we get for $\vec{F}_{02}$ and $\vec{F}_{03}$

$$\begin{aligned} \vec{F}_{02} &= F_{02,x} = -28.09... \text{ Nm} \quad \text{(to the right)} \\ \vec{F}_{03} &= -22.47... \text{ Nm} \quad \text{(to the top left)} \end{aligned}$$

For $\vec{F}_{03}$, we have to calculate the x - and y -component.

This is possible, by using the angle α between the line through q_0 and q_3 and the positive x -axis (pointing to the right).

So, α has to be between 90° and 180° . It can be calculated by:

$$\begin{aligned} \alpha &= \arctan\left(\frac{-4 \text{ cm}}{+2 \text{ cm}}\right) = \pi - 1.1071... \\ &= 180^\circ - 63.4...^\circ = 116.6...^\circ \end{aligned}$$

Based on this, the x - and y -component is:

$$\begin{aligned} |\vec{F}_{03}| \cdot \cos \alpha &= 10.05... \text{ Nm} \quad \text{(to the left)} \\ F_{03,y} &= |\vec{F}_{03}| \cdot \sin \alpha = 20.10... \text{ Nm} \quad \text{(to the top)} \end{aligned}$$

top}} \end{align*}

Exercise E2 Electrostatics I

(written test, approx. 10 % of a 120-minute written test, SS2022)

2. What is the magnitude of the electric force on the charge q_0 ? The picture below shows the values of the point charges q_1, q_2, q_3 and q_4 . Which value needs E_4 to have to get a resulting force of 0 N on q_0 ?

Path:

- $q_0 = -1 \text{ nC}$

- $q_1 = -2 \text{ nC}$

Path: $E_4 = 2310.97 \text{ V/m}$

- $\vec{F}_{01} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

With the given data and the position of the charges, we cannot calculate the resulting magnitude of the electric force on q_0 .

The electric field E_4 is the electric field of the charge q_4 at the position of q_0 .

- $E_4 = 2310.97 \text{ V/m}$

- $\vec{F}_{01} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{02} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{03} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{04} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{05} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{06} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{07} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{08} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{09} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{10} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{11} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{12} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{13} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{14} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{15} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{16} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{17} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{18} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{19} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{20} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{21} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{22} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{23} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{24} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{25} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{26} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{27} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{28} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{29} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{30} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{31} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{32} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{33} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{34} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{35} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{36} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

- $\vec{F}_{37} = \left(\begin{array}{c} 19.97 \\ 0 \end{array} \right) \text{ nN}$

1. Calculate the single forces $\vec{F}_{01}$, $\vec{F}_{02}$, $\vec{F}_{03}$, on the charge q_0 !

Path

First, calculate the magnitude of the forces, like $\vec{F}_{01}$.

The force $\vec{F}_{01}$ is purely on the x -axis and therefore equal to

$F_{01,x}$. $\begin{array}{l} \vec{F}_{01} = F_{01,x} \end{array}$

$$\frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 \cdot q_0}{r_{01}^2} \parallel \&= \frac{1}{4\pi \cdot 8.854 \cdot 10^{-12} \cdot \text{As/Vm}} \cdot \frac{1 \cdot 10^{-9} \cdot \text{C} \cdot 2 \cdot 10^{-9} \cdot \text{C}}{(3 \cdot 10^{-2} \cdot \text{m})^2} \parallel \&= 19.97... \cdot 10^{-6} \cdot \frac{(\text{As})^2 \cdot \text{Vm}}{\text{As} \cdot \text{m}^2} = 19.97... \cdot 10^{-6} \cdot \frac{\text{VAs}}{\text{m}} = 19.97... \cdot 10^{-6} \cdot \frac{\text{Ws}}{\text{m}} \parallel \&= 19.97... \cdot \mu\text{N} \quad \text{(to the right)} \quad \text{\textbackslash end\{align*\}}$$

Similarly, we get for $\vec{F}_{02}$ and $\vec{F}_{03}$

$$\vec{F}_{02} = F_{02,x} \&= -28.09... \mu\text{N} \quad \text{(to the right)} \parallel \vec{F}_{03} \&= -22.47... \mu\text{N} \quad \text{(to the top left)} \parallel \text{\textbackslash end\{align*\}}$$

For $\vec{F}_{03}$, we have to calculate the x - and y -component.

This is possible, by using the angle α between the line through q_0 and q_3 and the positive x -axis (pointing to the right).

So, α has to be between 90° and 180° . It can be calculated by:

$$\begin{aligned} \alpha &= \arctan\left(\frac{-4\text{ cm}}{+2\text{ cm}}\right) = \pi - 1.1071... = 180^\circ - 63.4...^\circ = 116.6...^\circ \end{aligned} \quad \text{\textbackslash end\{align*\}}$$

Based on this, the x - and y -component is:

$$\begin{aligned} F_{03,x} &= |\vec{F}_{03}| \cdot \cos \alpha = 10.05... \mu\text{N} \quad \text{(to the left)} \parallel \\ F_{03,y} &= |\vec{F}_{03}| \cdot \sin \alpha = 20.10... \mu\text{N} \quad \text{(to the top)} \parallel \end{aligned} \quad \text{\textbackslash end\{align*\}}$$

Exercise E3 Electrostatics II

(written test, approx. 10 % of a 120-minute written test, SS2022)

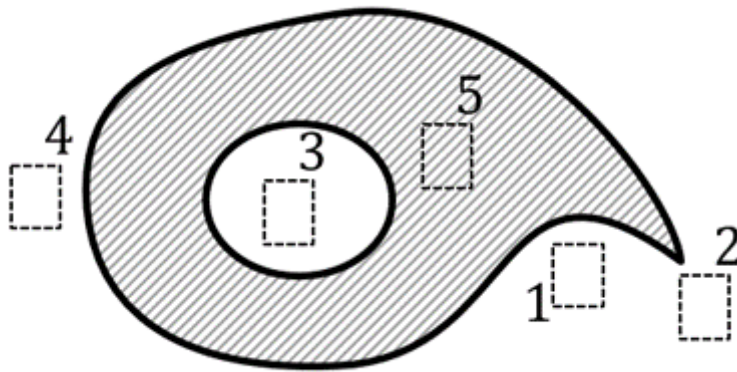
The figure below shows an arrangement of ideal metallic conductors (gray hatched) charged up to $q = +1 \text{ nC}$.

In white a dielectric (e.g. vacuum) is shown.

Several designated areas are shown by dashed frames and numbers x , which are partly inside the object.

Arrange the designated areas clearly according to ascending field strengths $|\vec{E}_x|$ (absolute magnitude)!

Indicate also, if designated areas have quantitatively the same field strength.



Result

$$|E_3| = |E_5| = 0 < |E_1| < |E_4| < |E_2|$$

Exercise E4 Electrostatics II

(written test, approx. 10 % of a 120-minute written test, SS2022)

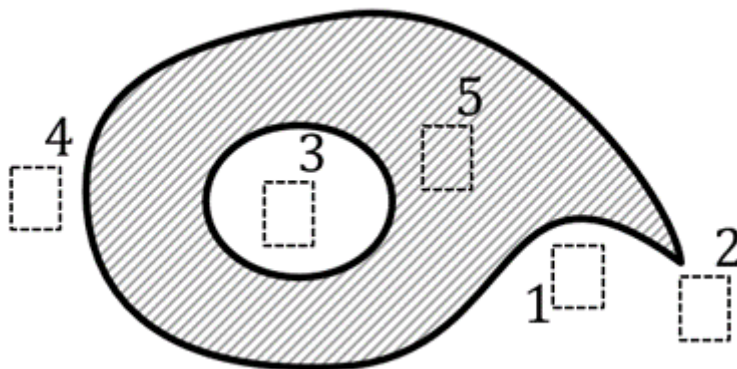
The figure below shows an arrangement of ideal metallic conductors (gray hatched) charged up to $q = +1 \text{ nC}$.

In white a dielectric (e.g. vacuum) is shown.

Several designated areas are shown by dashed frames and numbers x , which are partly inside the object.

Arrange the designated areas clearly according to ascending field strengths $|\vec{E}_x|$ (absolute magnitude)!

Indicate also, if designated areas have quantitatively the same field strength.



Result

$$|E_3| = |E_5| = 0 < |E_1| < |E_4| < |E_2|$$

Exercise E5 Electron Velocity in Semiconductors (written test, approx. 6 % of a 120-minute written test, SS2022)

A current of $I = 1 \text{ mA}$ flows through a cross-sectional area $A = 10 \text{ } \mu\text{m}^2$ in a semiconductor.

The electron density in the semiconductor is given by the number of dopant atoms per volume.

The doping shall provide 1 donor atom (= one electron) per 10^{10} silicon atoms. The elementary charge is $e = 1.602 \cdot 10^{-19} \text{ As}$ (about $41 \text{ } \mu\text{eV}$ of the speed of light). The molar volume of silicon is $V_{\text{mol,Si}} = 12 \cdot 10^{-6} \text{ m}^3/\text{mol}$, with $N_{\text{A}} = 6.022 \cdot 10^{23}$ silicon atoms per 1 mol .

The elementary charge is given as: $e = 1.602 \cdot 10^{-19} \text{ As}$

What is the average electron velocity v_e in this semiconductor?

Path

The following formula gives the speed, where n_e is the number of electrons per volume.
$$v_e = \frac{I}{n_e \cdot e \cdot A}$$

n_e can be derived from the overall number of Si-atoms per volume ($\frac{N_{\text{A}}}{V_{\text{mol,Si}}}$) and the fraction k_{Donators} of these atoms, which got substituted by donators.
$$n_e = \frac{N_{\text{A}}}{V_{\text{mol,Si}}} \cdot k_{\text{Donators}}$$

Putting in the numbers:
$$v_e = \frac{1 \cdot 10^{-3} \text{ A}}{6.022 \cdot 10^{23} \text{ 1/mol} \cdot 12 \cdot 10^{-6} \text{ m}^3/\text{mol} \cdot 10^{-10} \cdot 1.602 \cdot 10^{-19} \text{ As} \cdot 10 \cdot (10^{-6} \text{ m})^2}$$

Exercise E6 Electron Velocity in Semiconductors (written test, approx. 6 % of a 120-minute written test, SS2022)

Result Current of $I=1\text{~}\text{mA}$ flows through a cross-sectional area $A=10\text{~}\mu\text{m}^2$ in a semiconductor.

The electron density in the semiconductor is given by the number of dopant atoms per volume.

The doping shall provide $5\text{~}\text{donator/s}$ (about $41\text{~}\%$ of the speed of light) silicon atoms.

The molar volume of silicon is $V_{\text{mol,Si}} = 12\cdot 10^{-6}\text{~}\text{m}^3/\text{mol}$, with $N_{\text{A}} = 6.022\cdot 10^{23}$ silicon atoms per $1\text{~}\text{mol}$.

The elementary charge is given as: $e_0 = 1.602\cdot 10^{-19}\text{~}\text{As}$

What is the average electron velocity v_e in this semiconductor?

Path

The following formula gives the speed, where n_e is the number of electrons per volume.
$$v_e = \frac{I}{n_e \cdot e_0 \cdot A}$$

n_e can be derived from the overall number of Si-atoms per volume ($\frac{N_{\text{A}}}{V_{\text{mol,Si}}}$) and the fraction k_{Donators} of these atoms, which got substituted by donators.
$$v_e = \frac{I}{\left(\frac{N_{\text{A}}}{V_{\text{mol,Si}}}\right) \cdot k_{\text{Donators}} \cdot e_0 \cdot A}$$

Putting in the numbers:
$$v_e = \frac{1\cdot 10^{-3}\text{~}\text{A}}{\left(\frac{6.022\cdot 10^{23}}{12\cdot 10^{-6}\text{~}\text{m}^3}\right) \cdot 10^{-10}\text{~}\text{m} \cdot 1.602\cdot 10^{-19}\text{~}\text{As} \cdot 10\cdot (10^{-6}\text{~}\text{m})^2}$$

Exercise E7 Capacitor

(written test, approx. 7 % of a 120-minute written test, SS2022)

Given: The multiple capacitor in the left-side picture, with the following dimensions: $\epsilon_{\text{r,c}}=0.1\text{~}\text{mm}$

Result: $\epsilon_{\text{r,c}}$ of air ($\epsilon_{\text{r,c}}=1$), while the thickness of the dielectric material remains the same

Path: Length of layer overlap: $l=1.5\text{~}\text{mm}$

Distance between single layers: $d=1.0\text{~}\mu\text{m}$

• Depth of component: $w=0.7\text{~}\text{mm}$

$\epsilon_{\text{r,c}}$ (only $10\text{~}\mu\text{m}$ in the picture): 3 left-side and 3 right-side layers.

Path

The capacity can be derived from the geometry by:
$$C = \epsilon_0 \epsilon_{\text{r,c}} \frac{A}{d}$$

The air builds another capacitor in series to the dielectric material. Therefore, the capacity can be calculated as
$$C_{\text{Air}} = \frac{C \cdot C_{\text{Air}}}{C + C_{\text{Air}}}$$

The capacity of air is
$$C_{\text{Air}} = \frac{\epsilon_0 \epsilon_r N \cdot l \cdot w}{d} \quad \epsilon_r = 8.854 \cdot 10^{-12} \text{ ~\rm As/Vm}$$

By this the overall capacity is
$$C_{\text{r}} = \frac{0.139... \text{ ~\rm nF} \cdot 0.465... \text{ ~\rm nF}}{0.139... \text{ ~\rm nF} + 0.465... \text{ ~\rm nF}}$$

How many "multiple plates" N do we have to consider?

For this, we have to count facing areas A_0 . There are $N=5$.

The material shall have a dielectric permittivity of $\epsilon_r=3$.

The following calculations shall ignore boundary effects on the end of the layers.

$\epsilon_0 = 8.854 \cdot 10^{-12} \text{ ~\rm As/Vm}$

.. What is the field strength in the dielectric material between the layer, when a voltage of $U=6.3 \text{ ~\rm V}$ is applied?

Path

The electric field strength E is given by:
$$E = \frac{U}{d} \quad = \frac{6.3 \text{ ~\rm V}}{1 \cdot 10^{-6} \text{ ~\rm m}}$$

Therefore, the formula is
$$C = \frac{\epsilon_0 \epsilon_r \{N \cdot l \cdot w\}}{d} \quad = \frac{8.854 \cdot 10^{-12} \text{ ~\rm As/Vm} \cdot 3 \cdot \{5 \cdot 1.5 \cdot 10^{-3} \text{ ~\rm m} \cdot 0.7 \cdot 10^{-3} \text{ ~\rm m}\}}{1 \cdot 10^{-6} \text{ ~\rm m}}$$

Exercise E8 Capacitor

(written test, approx. 7 % of a 120-minute written test, SS2022)

6. Calculate the multiple capacitance of the shown device, with the following dimensions: $\epsilon_r=3$, $\epsilon_0=8.854 \cdot 10^{-12} \text{ ~\rm As/Vm}$

Result: $\epsilon_r = 1.5$, while the thickness of the dielectric material remains constant between single layers: $d = 1.0 \text{ ~}\mu\text{m}$

What is the capacitance C ?

- Number of layers (as shown in the picture): 3 left-side and 3 right-side layers.

$$E = \frac{U}{d} = \frac{6.3 \text{ V}}{1.0 \cdot 10^{-6} \text{ m}} = 6.3 \cdot 10^6 \text{ V/m}$$

The capacity can be derived from the geometry by:
$$C = \frac{\epsilon_0 \epsilon_r N A}{d}$$

For the area A we have multiple plates with the area $A_0 = l \cdot w$ facing each other builds another capacitor in series to the dielectric material. Therefore, the capacity can be calculated as
$$C_{\text{Air}} = \frac{\epsilon_0 A_0}{d} \quad C = \frac{C_{\text{Air}}}{N}$$

The capacity of air is
$$C_{\text{Air}} = \frac{\epsilon_0 N A_0}{d} = 8.854 \cdot 10^{-12} \text{ As/Vm} \cdot 1 \cdot 10^{-3} \cdot 1.5 \cdot 10^{-3} \cdot 0.7 \cdot 10^{-3} = 9.165 \cdot 10^{-18} \text{ F}$$

The material shall have a dielectric permittivity of $\epsilon_r = 1.5$

The following calculations shall ignore boundary effects on the end of the layers.

By this the overall capacity is
$$C = \frac{C_{\text{Air}}}{N} = \frac{9.165 \cdot 10^{-18} \text{ F}}{5} = 1.833 \cdot 10^{-18} \text{ F}$$

For this, we have to count facing areas A_0 . There are $N = 5$.

What is the field strength in the dielectric material between the layer, when a voltage of $U = 6.3 \text{ V}$ is applied?

Path

The electric field strength E is given by:
$$E = \frac{U}{d} = \frac{6.3 \text{ V}}{1 \cdot 10^{-6} \text{ m}} = 6.3 \cdot 10^6 \text{ V/m}$$

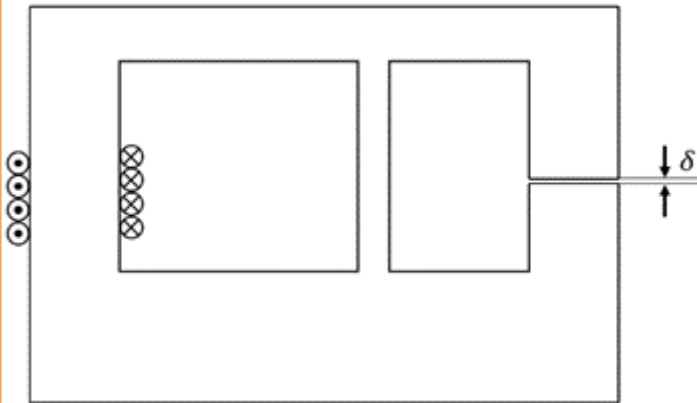
Therefore, the formula is
$$C = \frac{\epsilon_0 \epsilon_r N A_0}{d} = 8.854 \cdot 10^{-12} \text{ As/Vm} \cdot 3 \cdot 10^{-3} \cdot 1.5 \cdot 10^{-3} \cdot 0.7 \cdot 10^{-3} \cdot 5}{1 \cdot 10^{-6} \text{ m}} = 1.833 \cdot 10^{-18} \text{ F}$$

Exercise E9 Magnetic Circuit**(written test, approx. 7 % of a 120-minute written test, SS2022)**

The magnetic setup below shall be given. Draw the equivalent magnetic circuit to represent the setup fully. Name all the necessary magnetic resistances, fluxes, and voltages.

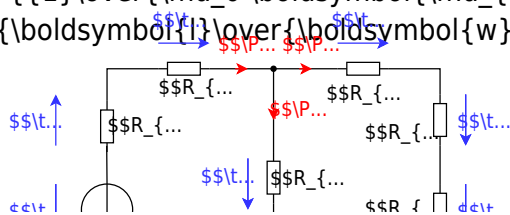
The components shall be designed in such a way, that the magnetic resistance is constant in it.

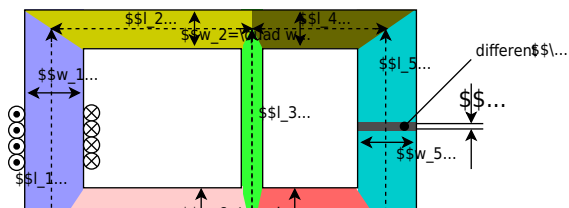
Formulas are not necessary.



Path

Watch for parts of the magnetic circuit, where the width and material are constant. These parts represent the magnetic resistors which have to be calculated individually. Be aware, that every junction creates a branch with a new resistor, like for an electrical circuit - there must be a node on each "diversion".

$$R_{\text{m}} = \frac{1}{\mu_0 \mu_{\text{r}}} \frac{l}{w \cdot h}$$




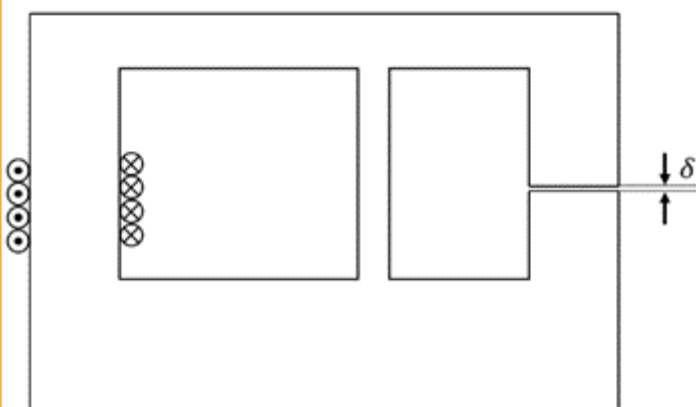
Exercise E10 Magnetic Circuit

(written test, approx. 7 % of a 120-minute written test, SS2022)

The magnetic setup below shall be given. Draw the equivalent magnetic circuit to represent the setup fully. Name all the necessary magnetic resistances, fluxes, and voltages.

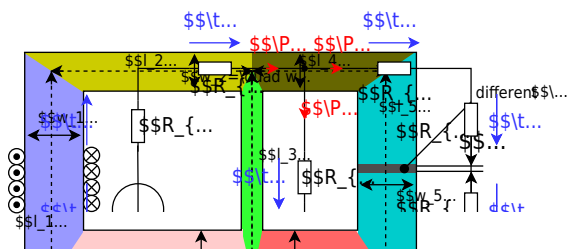
The components shall be designed in such a way, that the magnetic resistance is constant in it.

Formulas are not necessary.



Path

Watch for parts of the magnetic circuit, where the width and material are constant. These parts represent the magnetic resistors which have to be calculated individually. Be aware, that every junction creates a branch with a new resistor, like for an electrical circuit - there must be a node on each "diversion".

$$R_m = \frac{l}{\mu_0 \mu_r w h}$$


Exercise E1 Self Induction

(written test, approx. 8 % of a 120-minute written test, SS2022)

2. What is the maximum magnitude of the induced voltage, which the circuit breaker has to withstand, which is fused with a circuit breaker.

Sketch the diagram of the circuit with the current $I(t) = 0$ with the percentage value of the induced voltage linearly down to 0 A within 1 ms .

(The inner resistance of the motor shall be neglected.)

$$u_{\text{ind}}(t) = 3150 \text{ V}$$

Path

.. Draw the circuit (the circuit breaker can be drawn as a switch), with all voltage and current arrows.

For the maximum voltage on the circuit breaker one has to consider the following:

Result

- external voltage of the voltage source U_{S}
- voltage $u_{\text{ind}}(t)$ induced by the change of the current

The first one is not given in the exercise, and therefore not considered here.

The induced voltage can be calculated by linearizing the following:

$$u_{\text{ind}}(t) = -L \frac{di}{dt} \rightarrow u_{\text{ind}}(t) = -L \frac{\Delta i}{\Delta t}$$

With the given details:

$$u_{\text{ind}}(t) = -L \frac{0 - I}{t_1 - t_0} = 50 \cdot 10^{-6} \text{ H} \cdot \frac{63 \text{ A}}{1 \cdot 10^{-6} \text{ s}} = 3150 \frac{\text{Vs}}{\text{A}} \cdot \frac{\text{A}}{\text{s}}$$

$u_{\text{ind}}(t) = \dots$



Exercise E11 Self Induction

(written test, approx. 8 % of a 120-minute written test, SS2022)

2. A motor with an inductance of $L = 50 \mu\text{H}$, which is connected to a DC voltage source and which is fused with a circuit breaker.

Sketch the break curve $i(t)$ and $u_{\text{ind}}(t)$ with a current of $I = 63 \text{ A}$ of the induced current is reduced linearly down to 0 A within $1 \mu\text{s}$.

(The inner resistance of the motor shall be neglected.)

$$u_{\text{ind}}(t) = 3150 \text{ V}$$

Path

.. Draw the circuit (the circuit breaker can be drawn as a switch), with all voltage and current arrows.

For the maximum voltage on the circuit breaker one has to consider the following:

Result

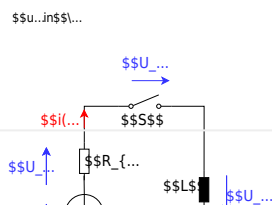
- external voltage of the voltage source U_{S}
- voltage $u_{\text{ind}}(t)$ induced by the change of the current

The first one is not given in the exercise, and therefore not considered here.

The induced voltage can be calculated by linearizing the following:

$$u_{\text{ind}}(t) = -L \frac{di}{dt} \rightarrow u_{\text{ind}}(t) = -L \frac{\Delta i}{\Delta t}$$

With the given details:
$$u_{\text{ind}}(t) = -L \frac{dI}{dt} = 50 \cdot 10^{-6} \cdot \frac{63 \cdot 10^{-6}}{1 \cdot 10^{-6}} = 3150 \frac{\text{Vs}}{\text{A}} \cdot \frac{\text{A}}{\text{s}}$$



Exercise E12 Series Resonant Circuit (written test, approx. 10 % of a 120-minute written test, SS2022)

2. What is the resonance frequency of the circuit shown in the diagram? What is the value of the resonance impedance Z_{RLC} ?

And in this case, what is the value of the resonance voltage U_{C0} would be $X_{\text{C0}} = Z_{\text{RLC}}$. Which value would C_0 have for the given f_0 ?

- Path:
- $C = 10 \text{ nF}$
 - $R = 88.6 \text{ m}\Omega$
 - $L = 60 \text{ mH}$
 - $f_0 = 205.5 \text{ kHz}$

The resonance frequency is given as
$$f_0 = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{60 \cdot 10^{-6} \cdot 10 \cdot 10^{-9}}} = 205.5 \text{ kHz}$$

At resonance, the impedance is given purely by the resistor.
$$Z_{\text{RLC}} = X_{\text{C0}} = \frac{1}{2\pi f_0 C} = 88.6 \text{ m}\Omega$$

With values:
$$C = \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot 10.6 \cdot 10^{-9}} = 0.1500 \text{ nF}$$

Exercise E13 Series Resonant Circuit**(written test, approx. 10 % of a 120-minute written test, SS2022)**

2. What is the magnitude of the RMS voltage U_{eff} for the given capacitor and inductor? Result in Ω and V . Inductance L .

At resonance, the magnitude of the impedance Z_{RLC} would be $Z_{\text{RLC}} = Z_{\text{RLC}}$. Which value would C have for the given f_0 ?

Path: $C = 10 \text{ nF}$
 $R = 88 \text{ m}\Omega$
 $f_0 = 100 \text{ MHz}$
 $L = 60 \text{ nH}$
 $C = 10 \text{ nF}$

The resonance frequency is given as $f_{\text{r}} =$

$$\frac{1}{2\pi\sqrt{LC}} \quad \&= \quad \frac{1}{2\pi\sqrt{60 \cdot 10^{-12} \cdot 10 \cdot 10^{-9}}} \quad \&= \quad 205 \text{ MHz}$$

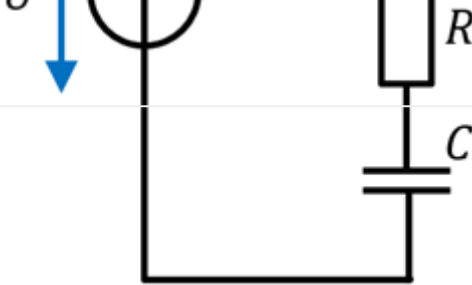
The calculated frequency of $f_{\text{r}} = 205 \text{ MHz}$ has to be set equal to the f_0 .

$$\begin{aligned} Z_{\text{RLC}} &= R + j\omega L - \frac{j}{\omega C} \quad \&= \quad R \quad \&= \quad 88 \text{ m}\Omega \\ \&= \quad \frac{1}{2\pi f \cdot C} \quad \&= \quad \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot C} \end{aligned}$$

At resonance the impedance Z_{RLC} is purely real, only by the resistor.

$$\begin{aligned} \&= \quad \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot C} \quad \&= \quad 10.6 \text{ nF} \end{aligned}$$

With values: $C = 10.6 \text{ nF}$



1. What is the impedance $\underline{Z}_{\text{RLC}}$ of this real capacitor for $f_0 = 100 \text{ MHz}$? (Phase and magnitude)

Path

The impedance $\underline{Z}_{\text{RLC}}$ is given by: $\underline{Z}_{\text{RLC}} =$

$$\begin{aligned} \underline{Z}_{\text{RLC}} &= R + j\omega L - \frac{j}{\omega C} \quad \&= \quad R + j\omega L - \frac{j}{\omega C} \\ &= R + j\omega L - \frac{j}{\omega C} \quad \&= \quad R + j\omega L - \frac{j}{\omega C} \end{aligned}$$

Putting in the numbers, only for the reactive part $\underline{X}_{\text{LC}}$: $\underline{X}_{\text{LC}} =$

$$\begin{aligned} \underline{X}_{\text{LC}} &= j\omega L - \frac{j}{\omega C} \quad \&= \quad j\omega L - \frac{j}{\omega C} \\ &= j\omega L - \frac{j}{\omega C} \quad \&= \quad j\omega L - \frac{j}{\omega C} \\ &= j\omega L - \frac{j}{\omega C} \quad \&= \quad j\omega L - \frac{j}{\omega C} \end{aligned}$$

With the real and imaginary parts, we can derive the magnitude and phase:

$$\begin{aligned} Z_{\text{RLC}} &= \sqrt{R^2 + \underline{X}_{\text{LC}}^2} \quad \&= \quad \sqrt{88^2 + (-121.45)^2} \\ &= \sqrt{88^2 + (-121.45)^2} \quad \&= \quad 150.0 \text{ m}\Omega \end{aligned}$$

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\begin{align*} \varphi &= \arctan \left( \frac{X_{LC}}{R} \right) \quad \&= \arctan \\ &\left( \frac{-121.45 \sim \rm m\Omega}{88 \sim \rm m\Omega} \right) \quad \&= -0.9437... \\ &= -54.07...^\circ \end{align*}
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