

Exam Winter Semester 2022

Student Group

First Name	Surname	Matrikel Nr.

Table of Contents

Exam Winter Semester 2022	3
Additional permitted Aids	3
Hits	3
Tasks	3
Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)	3
Exercise E1 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)	4
Exercise E2 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)	4
Exercise E1 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)	5
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)	7
Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)	9
Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)	13
Exercise E1 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)	17
Exercise E5 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)	18
Exercise E1 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)	20
Exercise E6 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)	20
Exercise E1 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute	

written test, WS2022)	21
Exercise E7 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022)	21
Exercise E1 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)	22
Exercise E8 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)	25

Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

Tasks

Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wire even to a temperature of 1800°C . Electric power dissipation (= heat flow) of $P=40\text{ W}$ is necessary.

Calculate the current I needed to operate for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6}\text{ }\Omega\text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40\text{ W}}{0.33\text{ }\Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad | \text{ with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad \& \quad R = 1.10 \cdot 10^{-6}\text{ }\Omega\text{ m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wire even to a temperature of 1800°C . Electric

Result power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Calculate the current I linked to the power P for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

2. Calculate the resistance R (W) needed at length l .

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ R &= \frac{P}{I^2} = \frac{40 \text{ W}}{(0.33 \text{ A})^2} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad | \quad A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad | \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E1 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator is equipped with a thermistor to monitor the temperature inside the refrigerator. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result The temperature inside the refrigeration system can reach down to -40°C .

1. Calculate the resistance of the thermistor at -40°C .

$$R = 6.5 \text{ k}\Omega$$

Solution The resistance of the thermistor decreases as the temperature decreases. Therefore, a thermistor can be used to monitor the temperature inside the refrigerator.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$\begin{aligned} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R &= 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ \text{C} - 25^\circ \text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ \text{C} - 25^\circ \text{C})^2\right) \end{aligned}$$

Exercise E2 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A refrigerator, which has a temperature coefficient of performance of 2.5, has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ } ^\circ\text{C}^{-1}$ and $\beta = 71 \text{ } ^\circ\text{C}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: The temperature inside the refrigeration system can reach down to -40°C .

$$R = 65 \text{ k}\Omega$$

The power transfer resistor R is a part of the circuit and generates heat. Therefore, a solution is to use a heat sink to cool the resistor.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot \left((1 + 0.01 \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2) \right)$$

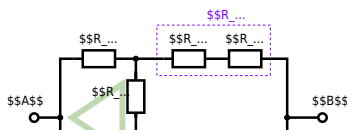
Exercise E1 Pure Resistor Network Simplification**(written test, approx. 13 % of a 60-minute written test, WS2022)**

The following shall be calculated: R_{eq} at 10°C , R_{eq} at 25°C , and the power P at 10°C .
Result: $R_{\text{eq}} = 10 \text{ k}\Omega$.

Solution

$$R_{\text{eq}} = 10 \text{ k}\Omega$$

Now a wye-delta transformation is necessary.



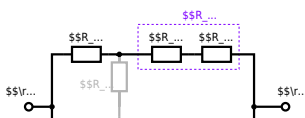
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega) \parallel$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{eq} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega}$$

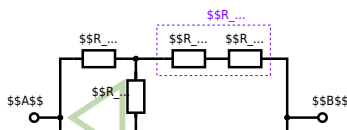
Exercise E3 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be solved with $R_1 = 200 \, \Omega$, $R_2 = 100 \, \Omega$, $R_3 = 150 \, \Omega$, $R_4 = 100 \, \Omega$ and the voltage $U_{SV} = 10 \, \text{V}$.
Result given: $R_{eq} = 132.8 \, \Omega$.

Solution

$$R_{eq} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.



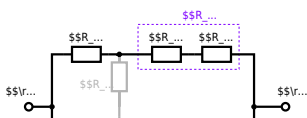
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega) \parallel$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



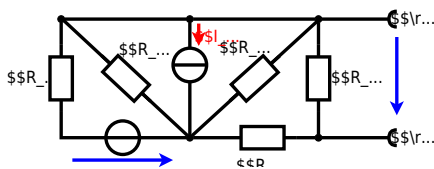
The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 || R_3) || R_4 = (100 \, \Omega + 200 \, \Omega || 200 \, \Omega) || (100 \, \Omega + 100 \, \Omega) = (500 \, \Omega) || (200 \, \Omega) = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega}$$

Exercise E1 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

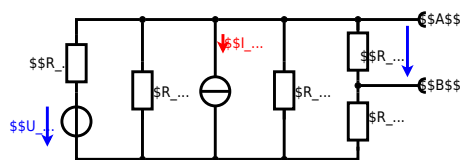
$$U_s = U_{AB} = 4.5 \, \text{V} \quad R_i = R_{AB} = 6 \, \Omega$$



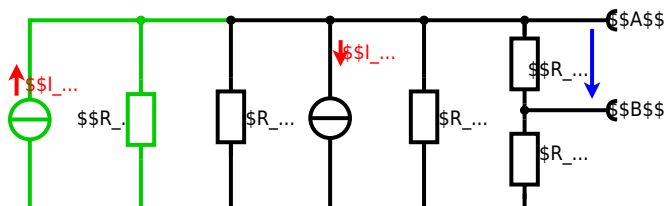
Calculate the internal resistance R_s and the source voltage U_s of an equivalent linear voltage source on the connectors A and B.
$$R_1 = 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \quad R_5 = 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega$$
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_2 \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} = (U_2 - I_4 \cdot R_1 || R_3 || R_5) \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} = (U_2 - I_4 \cdot R_1 || R_3 || R_5) \cdot \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($= 0 \Omega$, so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

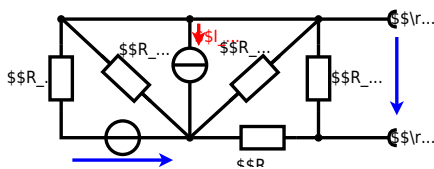
with $R_1 || R_3 || R_5 = 5 \Omega || 10 \Omega || 10 \Omega = 5 \Omega || 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \\ R_{AB} = 15 \Omega || (7.5 \Omega + 2.5 \Omega)$$

Exercise E4 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

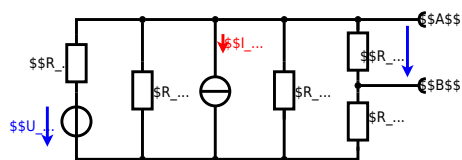
$$U_s = U_{AB} = 4.5 \text{ V} \\ R_i = R_{AB} = 6 \Omega$$



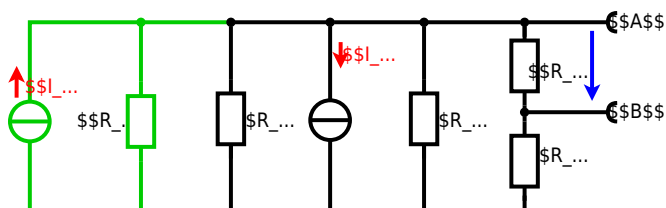
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $\begin{aligned} R_1 &= 5.0 \, \Omega, \quad U_2 = 6.0 \, \text{V}, \quad R_3 = 10 \, \Omega, \quad I_4 = 4.2 \, \text{A}, \\ R_5 &= 10 \, \Omega, \quad R_6 = 7.5 \, \Omega, \quad R_7 = 15 \, \Omega \end{aligned}$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{AB} = R_{135} \cdot I_{24} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} \cdot 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \quad R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E1 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit below is a fully charged circuit with a 10V DC voltage source, a 2Ω resistor, a 2F capacitor, and a 2V DC voltage source. The voltage across the capacitor is again 0V at the moment $t_0=0\text{s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ms}$ after closing the switch.

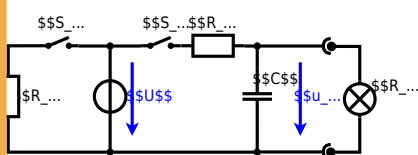
Result

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

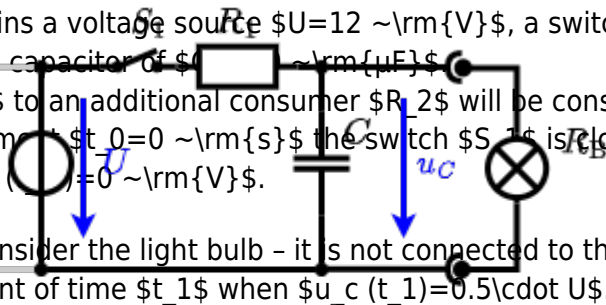
$$U_{\text{eq}} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{10\text{V} \cdot 2\Omega}{2\Omega + 2\Omega} = 5\text{V}$$

Solution The circuit is a series circuit. The total voltage is 5V and the total resistance is 4Ω . The voltage across the capacitor is $u_c(t) = 5\text{V} \cdot (1 - e^{-t/2\text{ms}})$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

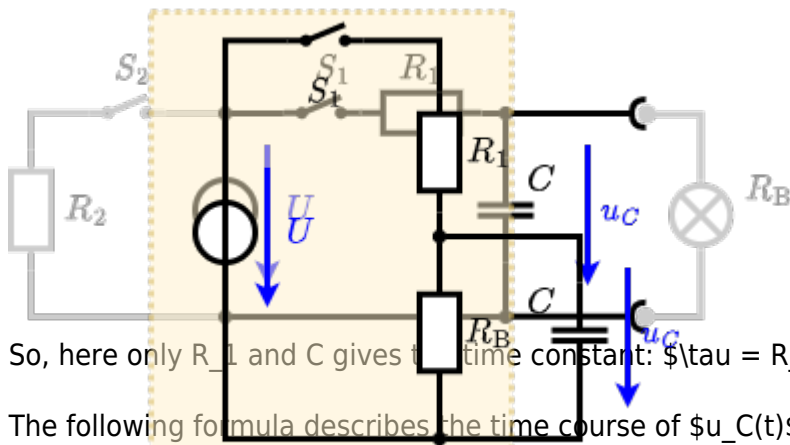


The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$

$$e^{-t/\tau} = 0.5 \quad t/\tau = \ln(0.5) \quad t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$
 An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$ The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E5 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V DC voltage source, a switch S_1 and a switch S_2 in series with a $20\text{ }\Omega$ resistor, a $100\text{ }\mu\text{F}$ capacitor and a $10\text{ }\Omega$ resistor. The voltage across the capacitor is again 0 V at the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

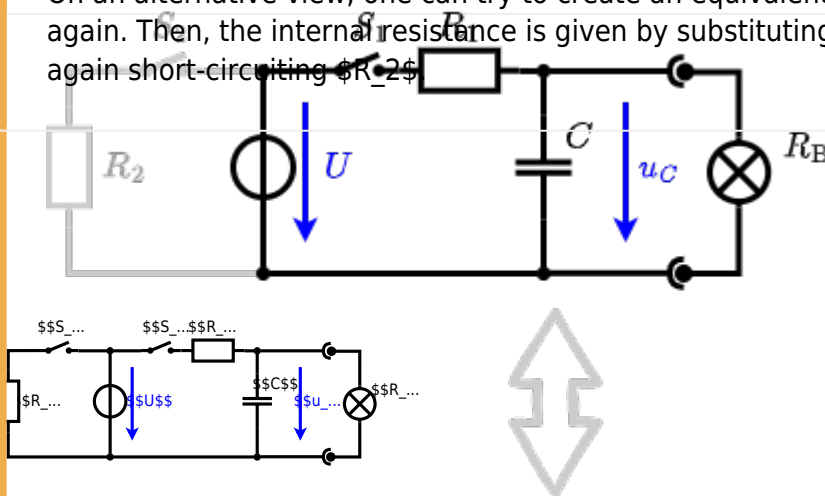
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

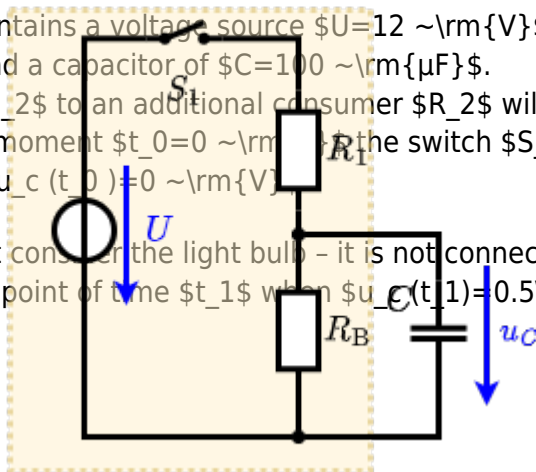


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1) = 0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$

It has to be rearranged to t :

$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$

Exercise E1 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV, $\underline{Z} = 0.24 \angle 60^\circ \Omega$ and $\underline{Z} = 4.68 \angle -20^\circ \Omega$ through the components. (R and X_L) shall be given.

After analysis, the full bridge dimensioned impedance can be extracted and the phase angle φ in phase (calculated) is $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 \angle 60^\circ + 4.68 \angle -20^\circ}$

The current and voltage are in phase only if the impedance is purely real. The resulting impedance is $\underline{Z} = 0.24 \angle 60^\circ + 4.68 \angle -20^\circ$.

Therefore, the component $4.68 \angle -20^\circ$ is a capacitor with the same absolute value of $4.68 \angle -20^\circ$.

Impedance $\underline{Z} = R + jX_L = 0.24 + j4.68$

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 + j4.68} = \frac{50 \angle 0^\circ}{4.69 \angle 87.06^\circ} = 10.66 \angle -87.06^\circ$

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

With the complex part $\underline{Z} = 0.24 + j4.68$ we can calculate the phase angle φ as $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

Exercise E6 Analyzing complex Impedances**(written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV, $\underline{Z} = 0.24 \angle 60^\circ \Omega$ and $\underline{Z} = 4.68 \angle -20^\circ \Omega$ through the components. (R and X_L) shall be given.

After analysis, the full bridge dimensioned impedance can be extracted and the phase angle φ in phase (calculated) is $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

.. Calculate the physical values of the two components.

Solution $\begin{aligned} R &= 0.24 \Omega \\ X_L &= 4.68 \Omega \end{aligned}$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 \angle 60^\circ + 4.68 \angle -20^\circ}$

The current and voltage are in phase only if the impedance is purely real. The resulting impedance is $\underline{Z} = 0.24 \angle 60^\circ + 4.68 \angle -20^\circ$.

Therefore, the component $4.68 \angle -20^\circ$ is a capacitor with the same absolute value of $4.68 \angle -20^\circ$.

Impedance $\underline{Z} = R + jX_L = 0.24 + j4.68$

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 + j4.68} = \frac{50 \angle 0^\circ}{4.69 \angle 87.06^\circ} = 10.66 \angle -87.06^\circ$

The phase angle φ can be calculated as $\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{4.68}{0.24}\right) = 87.06^\circ$

The absolute value of the impedance is $\sqrt{(0.24 \sim \Omega)^2 + (4.68 \sim \Omega)^2} = 4.7 \sim \Omega$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.
 With the complex part comes the physical value: $X_L = \omega L = 2\pi f L = 2\pi \cdot 4.7 \sim \Omega \cdot 10^{-6} \text{ s} = 29.4 \sim \mu\text{s}$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.
 The phase φ is $\arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$.

Exercise E1 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.
 The equivalent impedance for R and C combined is given by $Z = \sqrt{R^2 + X_C^2}$.
 The equivalent impedance for R , L and C combined is given by $Z = \sqrt{R^2 + (X_L - X_C)^2}$.
 The equivalent impedance for R , L and C combined is given by $Z = \sqrt{R^2 + (X_L - X_C)^2}$.

Solution

$R_1 = 1.00 \sim \Omega$

$R_2 = 10.0 \sim \Omega$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$.

Parallel circuit means that the voltage is the same on R_1 and R_2 .
 $\frac{1}{Z} = \frac{1}{R_1} + \frac{1}{R_2}$
 $\frac{1}{Z} = \frac{1}{1.00 \sim \Omega} + \frac{1}{10.0 \sim \Omega}$
 $\frac{1}{Z} = \frac{10.0 + 1.00}{10.0 \sim \Omega}$
 $\frac{1}{Z} = \frac{11.00}{10.0 \sim \Omega}$
 $Z = \frac{10.0 \sim \Omega}{11.00}$
 $Z = 0.909 \sim \Omega$

The equivalent impedance for R and C combined is given by $Z = \sqrt{R^2 + X_C^2}$.
 $X_C = \frac{1}{\omega C} = \frac{1}{2\pi \cdot 4.7 \sim \text{MHz} \cdot 40 \sim \text{nF}} = 0.85 \sim \Omega$

Therefore, the resulting current of the parallel circuit is given as: $I = \frac{U}{Z} = \frac{10 \text{ V}}{0.909 \sim \Omega} = 11.0 \text{ A}$

This current is the same on R_1 and R_2 .
 $P_1 = I^2 R_1 = (11.0 \text{ A})^2 \cdot 1.00 \sim \Omega = 121 \text{ W}$
 $P_2 = I^2 R_2 = (11.0 \text{ A})^2 \cdot 10.0 \sim \Omega = 1210 \text{ W}$

Back to the first formula: $Z = \sqrt{R^2 + (X_L - X_C)^2}$

Back to the first formula: $Z = \sqrt{R^2 + (X_L - X_C)^2}$
 $Z = \sqrt{(1.00 \sim \Omega)^2 + (4.68 \sim \Omega - 0.85 \sim \Omega)^2} = 4.7 \sim \Omega$
 $I = \frac{U}{Z} = \frac{10 \text{ V}}{4.7 \sim \Omega} = 2.1 \text{ A}$

Exercise E7 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

Reactive Power The real resistor value is \$R=20\Omega\$ at \$f=1\text{ MHz}\$. A voltage divider is made from AC to have impedance of \$Z_{in}=20\Omega \sim \text{m}\Omega\$, \$\omega R=200-450\text{ m}\Omega\$ at \$f=1\text{ MHz}\$, has higher reactance current \$I_2=\frac{V}{Z_{in}}=1A\$ through capacitor \$C=10\text{ nF}\$ at \$f=1\text{ MHz}\$.

$$\begin{aligned} \text{solution} \quad \begin{aligned} \text{begin}\{align*\} \quad R_1 &= 1.00 \sim \Omega \end{aligned} \\ \text{solution} \quad \begin{aligned} \text{begin}\{align*\} \quad R_2 &= 10.0 \sim \Omega \end{aligned} \\ \text{solution} \end{aligned}$$

A series circuit means that the current is constant on every component.

[illegible]

Exercise E1 Complex Impedance Circuit

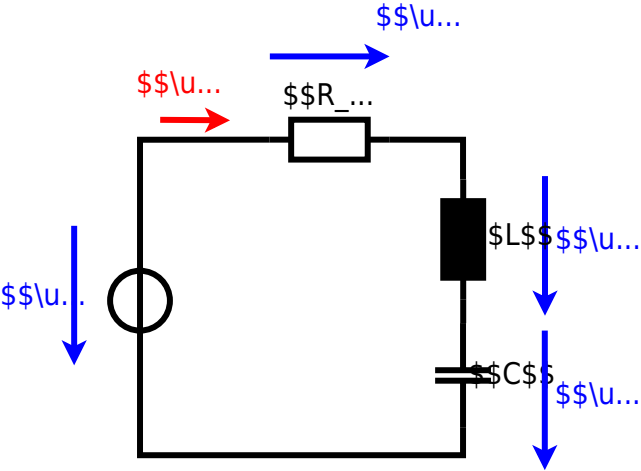
(written test, approx. 15 % of a 60-minute written test, WS2022)

A. On the three European power grids, the series impedance Z_s , shunt impedance Z_p , and R per line (Ω) are, by the average source $u(t) = 3.0 \sim \text{V} \cdot \sin(2\pi \cdot 15 \sim \text{Hz})$ and a synchronous terminal fast source of ω .

Solution
This linear source is connected with an inductor of $330 \sim \{\rm \mu H\}$ and a capacitor of $0.22 \sim \{\rm \mu F\}$, all in series.

$$\begin{aligned} Z &= 107.3 \, \Omega \parallel (48.2 \, \Omega + j19.8 \, \Omega) \\ Z &= 84.5 \, \Omega - j37.5 \, \Omega \end{aligned}$$
[illegible]





Exercise E8 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

A. Can you describe the current dependence of $\langle \mu \rangle$ on $\text{signal}[\text{V}]$, $\text{offset}[\text{V}]$, and $\text{noise}[\text{V}]$ such as $\text{Re}[\text{Bandwidth}[\text{Hz}]]$ of the average source $u(t) = 3.0 \sim \text{V} \cdot \sin(2\pi \cdot 15 \sim \text{Hz})$ set at a position at a distance of $10 \sim \text{cm}$?

Solution A linear source is connected with an inductor of $330 \sim \{\rm \mu H\}$ and a capacitor of $30.22 \sim \{\rm \mu F\}$, all in series.

Result

$$\begin{aligned} \text{Decim} &= 9.111 & \text{Gradi} &= 10.000 & \text{Long} &= 10.000 \\ \text{Decim} &= 9.111 & \text{Gradi} &= 10.000 & \text{Long} &= 10.000 \end{aligned}$$

label all components, voltages, and currents.

$$\begin{aligned} Z &= \{ \{ \hat{U} \} \over \{ \hat{I} \} \} \parallel \hat{I} \} \quad \&= \{ \{ \hat{U} \} \over Z \} \parallel \end{aligned}$$

$$\begin{aligned} \{ \{1\} \over {2\pi \cdot f \cdot C} \} \} &= \{ \{1\} \over {2\pi \cdot 15} \} \end{aligned}$$

$$\text{Result} \{ \text{rm kHz} \} \cdot 0.22 \sim \{ \text{rm } \mu\text{F} \} \} \end{align*}$$

Within $\{ \text{aidn}[1] \}$ over $\{ \text{sgr}[2] \}$, $\text{cdot}(\text{cdot}(\text{hat}\{\&\$:\text{begin}\{\text{align}^*\},\downarrow,\text{m kHz}\}) \cdot 0.22$

$$\frac{1}{\sqrt{2}} \cdot \frac{\hat{U}}{Z} = \frac{1}{\sqrt{2}}$$

$$\forall \begin{pmatrix} 3 \\ 0 \end{pmatrix} \in \text{Im}(Y) \quad Z \cdot \overline{\omega} = \frac{19+28\sqrt{-1}}{129}\alpha \cdot \overline{\nu}$$

$$\&= \frac{1}{2\pi} \cdot 15$$

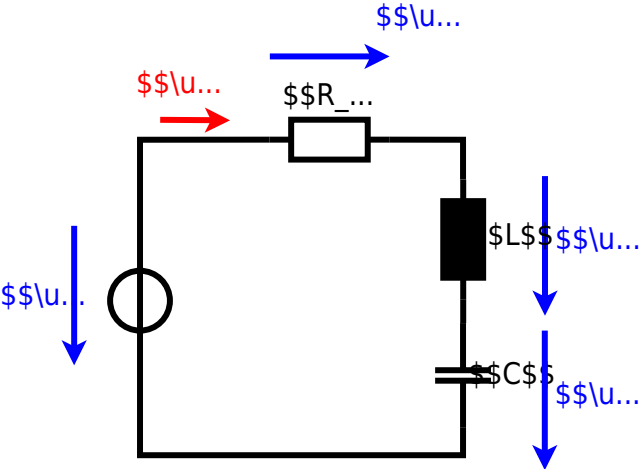
$$\sim \{\mathrm{~\rm kHz}\} \cdot 330 \sim \{\mathrm{~\rm \mu H}\} \} \} \} \end{align*}$$

$$\begin{aligned} \underline{Z} &\equiv B + \underline{Z} \\ L + \underline{Z} &\equiv B + i \end{aligned}$$

$$\cdot \{Z\} \mid - i \cdot \{Z\} C \rangle \&= B \pm i \cdot \{Z\} \mid - \{Z\} C \rangle \backslash \underline{\{Z\}} \&=$$

[illegible]

$$\sqrt{(R - Z + 1) \cdot (\text{undermine}[Z]_E - \text{undermine}[Z]_C - Z)} \cdot (\text{end}[\text{angr}])$$



From:

<https://wiki.mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:

https://wiki.mexle.te.hs-heilbronn.de/electrical_engineering_and_electronics_1/ws2022_exam?rev=1692265397

Last update: **2023/08/17 11:43**

