

Exam Winter Semester 2022

Student Group

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

Tasks

Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wires with a temperature of 180°C . The electric

power dissipation (= heat flow) of $P=40\text{ W}$ is necessary.

Calculate the current I needed to operate for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6}\ \Omega\text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ &= \sqrt{\frac{P}{R}} = \sqrt{\frac{40\text{ W}}{0.33\ \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad A = r^2 \cdot \pi = \\ &= \frac{1}{4} d^2 \cdot \pi \quad \& \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \& \quad R = \\ &= 1.10 \cdot 10^{-6}\ \Omega\text{ m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

electrical_engineering_and_electronics:task_rj0r6j4apumukrj6_with_calculation
resistivity, power, exam ee1 ws2022

Exercise E2 Temperature-dependent Resistance
(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A thermistor is used as a temperature sensor in a refrigerator. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Result: Calculate the resistance of the thermistor at -40°C .

Solution: The resistance of the thermistor at -40°C is $R = 6.5 \text{ k}\Omega$.

Therefore, a solution is to use a heat sink to cool the thermistor and prevent it from overheating.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

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```
\begin{align*} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) && | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} && \\ R &= 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right) && \\ &= 6.5 \text{ k}\Omega && \end{align*}
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[electrical_engineering_and_electronics:task_70jg4yzznocarsq_with_calculation](#)
[temperature dependent resistance, power, heat, exam ee1 ws2022](#)

Exercise E3 Pure Resistor Network Simplification
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following circuit is shown. The resistors are $R_1 = 10 \text{ }\Omega$, $R_2 = 20 \text{ }\Omega$, $R_3 = 30 \text{ }\Omega$, $R_4 = 40 \text{ }\Omega$, $R_5 = 50 \text{ }\Omega$, $R_6 = 60 \text{ }\Omega$, $R_7 = 70 \text{ }\Omega$, $R_8 = 80 \text{ }\Omega$, $R_9 = 90 \text{ }\Omega$, $R_{10} = 100 \text{ }\Omega$. The voltage source is $U = 100 \text{ V}$. Calculate the current I through the resistor R_5 .

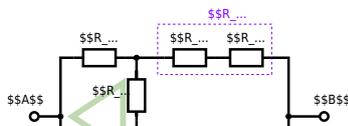
Result: $I = 1.33 \text{ A}$.

Solution:

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\begin{align*} R_{\text{eq}} &= 133.3 \text{ }\Omega && \end{align*}
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Now a wye-delta transformation is necessary.

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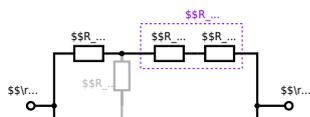


Since $R_2=R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:
$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{eq} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B.

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

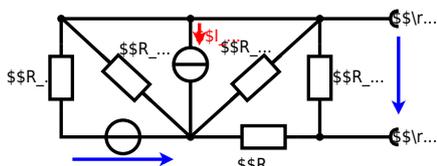
$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \Omega + 200 \Omega + 200 \Omega) \parallel (100 \Omega + 100 \Omega) \parallel R_{\text{eq}} = (500 \Omega) \parallel (200 \Omega) \parallel R_{\text{eq}} = \frac{500 \Omega \cdot 200 \Omega}{500 \Omega + 200 \Omega} \parallel$$

[electrical_engineering_and_electronics:task_x357drkaqv84jnsc_with_calculation](#)
[network simplification, exam ee1 ws2022](#)

Exercise E4 Equivalent linear Source
(written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
 Result

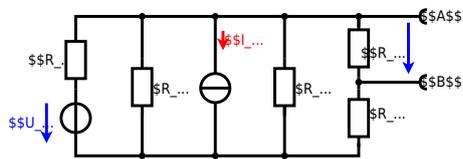
$$U_{\text{S}} = U_{\text{AB}} = 4.5 \text{ V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \Omega$$



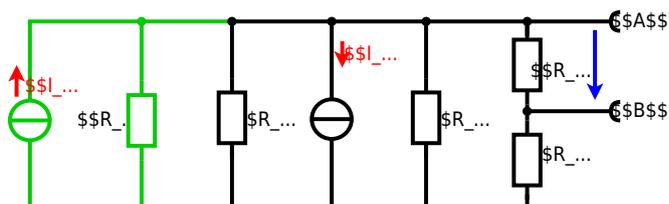
Calculated the internal resistance R_{int} and the source voltage U_{oc} of an equivalent linear voltage source on the connectors A and B .
$$R_1=5.0 \text{ } \Omega, \quad U_2=6.0 \text{ V}, \quad R_3= 10 \text{ } \Omega, \quad I_4=4.2 \text{ A}, \quad R_5=10 \text{ } \Omega, \quad R_6=7.5 \text{ } \Omega, \quad R_7=15 \text{ } \Omega$$
 Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{35} + I_{24} \cdot R_4 + I_{24} \cdot R_6$$

$$U_{24} = R_{135} \cdot I_{24} \quad \&= \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \left\{ \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} \right\} \quad \&= \left(\frac{U_2}{R_1} - I_4 \right) \cdot \left\{ \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} \right\}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \left(\frac{6.0\text{V}}{5.0\Omega} - 4.2\text{A} \right) \cdot \left\{ \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \right\} \quad R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

[electrical_engineering_and_electronics:task_6tqtqtque1e2nf2c7_with_calculation](#)
[dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022](#)

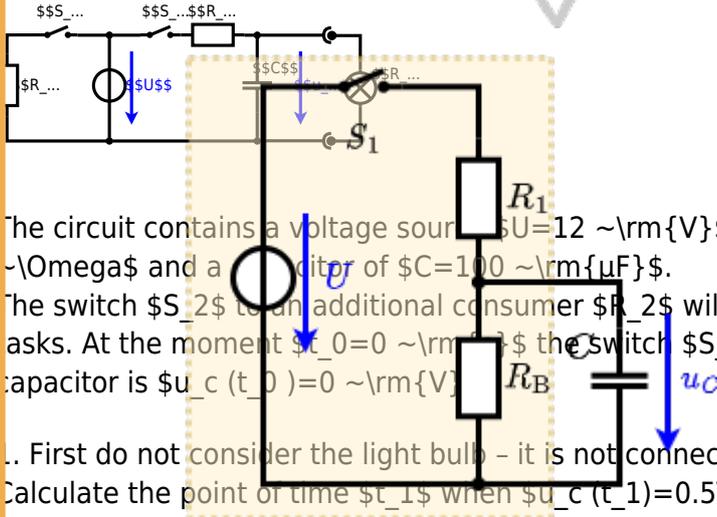
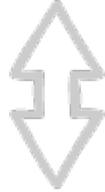
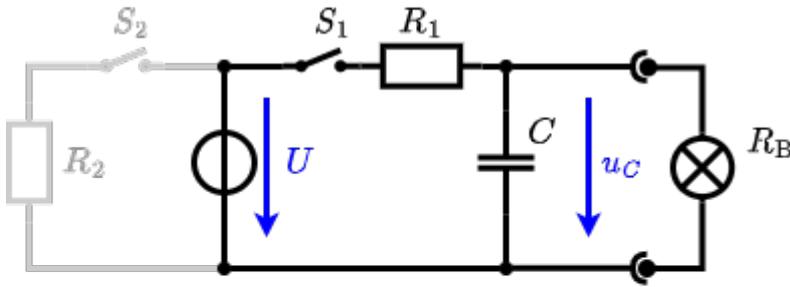
Exercise E5 Charging Capacitors
(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit below (real battery) also consists of $R_1 = 6\Omega$, $R_2 = 20\Omega$ and a capacitor $C = 2\mu\text{F}$ as indicated in the figure. The switch S_1 is open. The voltage across the capacitor is again 0V at the moment $t_0 = 0\text{s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1\text{ms}$ after closing the switch.

Result: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

$$U_{\text{del}} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{12\text{V} \cdot 20\Omega}{6\Omega + 20\Omega} = 4.76\text{V}$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



The circuit contains a voltage source $U=12 \text{ V}$, a switch S_1 , a resistor of $R_1=20 \text{ }\Omega$ and a capacitor of $C=100 \text{ }\mu\text{F}$.
 The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0=0 \text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0 \text{ V}$.
 ... First do not consider the light bulb - it is not connected to the RC circuit.
 Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = 1/2 \cdot U$
 The internal resistance is given by substituting the ideal voltage source with its resistance ($R=0 \text{ }\Omega$, short-circuit).
 $R_i = R_1 \parallel R_B = 10 \text{ }\Omega$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:
 $u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$
 $e^{-t/\tau} = 0.5 \implies t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$

charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

Exercise E6 Analyzing complex Impedances
(written test, approx. 14 % of a 60-minute written test, WS2022)

2. A circuit has the nodes and impedances shown in the figure. The voltage U is applied through the terminals A and B . The current I is the current through the resistor R_1 . The voltage U and the current I shall be given.

After analysis, the full bidirectional complex impedance values extracted and digitized in the table below. The voltage U and the current I shall be given.

.. Calculate the physical values of the two components.
Solution
$$R_1 = 10 \Omega, C_1 = 100 \text{ nF}$$

Solution
$$\underline{I} = \frac{\underline{U}}{\underline{Z}} \quad \underline{Z} = \{50 - j4.68 \Omega\}$$

The voltage U is the voltage across the capacitor C_1 . The current I is the current through the resistor R_1 . The voltage U and the current I shall be given.
Therefore, the component values are $R_1 = 10 \Omega$ and $C_1 = 100 \text{ nF}$.
The phase φ can be calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right)$.
With the complex part comes the physical values $R_1 = 10 \Omega$ and $C_1 = 100 \text{ nF}$.
The phase φ shall be calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right)$.

electrical_engineering_and_electronics:task_jti0uzudcmg4u22t_with_calculation
complex impedance, exam ee1 ws2022

Exercise E7 Impedances at different Frequencies
(written test, approx. 18 % of a 60-minute written test, WS2022)

2. A circuit has the resistors and impedances shown in the figure. The voltage U is applied through the terminals A and B . The current I is the current through the resistor R_1 . The voltage U and the current I shall be given.

After analysis, the full bidirectional complex impedance values extracted and digitized in the table below. The voltage U and the current I shall be given.

Solution
Solution
$$R_1 = 1.00 \Omega$$

Solution
$$R_2 = 10.0 \Omega$$

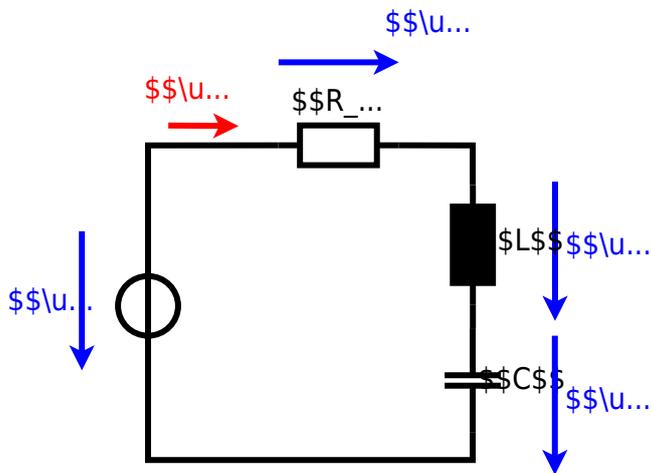
A series circuit means that the current is constant on every component.
 The equivalent resistance for the parallel combination is given by $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$.
 Since the current is constant, the voltage across each component is the same. The voltage across the parallel combination is $V_{parallel} = I \cdot R_{eq}$.
 The voltage across the series combination is $V_{series} = I \cdot R_{series}$.
 The total voltage is $V_{total} = V_{parallel} + V_{series} = I \cdot (R_{eq} + R_{series})$.
 Therefore, the resulting current of the parallel circuit is given as: $I = \frac{V_{total}}{R_{eq} + R_{series}}$.
 The power dissipated in the parallel combination is $P_{parallel} = I^2 \cdot R_{eq}$.
 The power dissipated in the series combination is $P_{series} = I^2 \cdot R_{series}$.
 The total power dissipated is $P_{total} = P_{parallel} + P_{series} = I^2 \cdot (R_{eq} + R_{series})$.
 Back to the first formula: $R_{eq} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$.
 The voltage across the parallel combination is $V_{parallel} = I \cdot R_{eq}$.
 The voltage across the series combination is $V_{series} = I \cdot R_{series}$.
 The total voltage is $V_{total} = V_{parallel} + V_{series} = I \cdot (R_{eq} + R_{series})$.

electrical_engineering_and_electronics:task_pdkggyexxy1ktu3_with_calculation
 complex impedance, exam ee1 ws2022

Exercise E8 Complex Impedance Circuit
 (written test, approx. 15 % of a 60-minute written test, WS2022)

2. Consider the circuit with the following parameters: $R = 10 \Omega$, $C = 10 \mu F$, $L = 10 mH$, and $V_s(t) = 3.0 \sin(2\pi \cdot 15 \cdot t)$ V.
 (a) Determine the complex impedance Z of the circuit.
 (b) Determine the magnitude of the current I through the circuit.
 (c) Determine the phase angle ϕ of the current I relative to the voltage V_s .
 (d) Determine the real power P dissipated in the circuit.
 (e) Determine the reactive power Q in the circuit.
 (f) Determine the complex power S in the circuit.

Solution
 Result: $Z = 10 - j31.8 \Omega$, $I = 0.096 \text{ A}$, $\phi = -72.9^\circ$, $P = 0.28 \text{ W}$, $Q = -0.91 \text{ var}$, $S = 0.96 \text{ VA}$.
 Draw the circuit diagram of the given circuit with all components, voltages, and currents.
 $Z = \frac{V}{I}$
 $Z_C = \frac{1}{j\omega C} = \frac{1}{j2\pi \cdot 15 \cdot 10 \cdot 10^{-6}} = -j1061 \Omega$
 $Z_L = j\omega L = j2\pi \cdot 15 \cdot 10 \cdot 10^{-3} = j0.94 \Omega$
 $Z = R + Z_L + Z_C = 10 + j0.94 - j1061 = 10 - j1060.06 \Omega$
 $I = \frac{V}{Z} = \frac{3.0 \sin(2\pi \cdot 15 \cdot t)}{10 - j1060.06} = 0.096 \sin(2\pi \cdot 15 \cdot t - 72.9^\circ) \text{ A}$
 $P = I^2 R = (0.096)^2 \cdot 10 = 0.28 \text{ W}$
 $Q = I^2 X = (0.096)^2 \cdot (-1060.06) = -0.91 \text{ var}$
 $S = P + jQ = 0.28 - j0.91 \text{ VA}$



electrical_engineering_and_electronics:task_kricv9fh7haauo6q_with_calculation
complex impedance, exam ee1 ws2022

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